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2017-07-25


http://hdl.handle.net/10138/211826
https://doi.org/10.5194/acp-17-8923-2017

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Evaporation of sulfate aerosols at low relative humidity

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Received: 23 November 2016 – Discussion started: 16 December 2016
Revised: 10 May 2017 – Accepted: 12 May 2017 – Published: 25 July 2017

Abstract. Evaporation of sulfuric acid from particles can be important in the atmospheres of Earth and Venus. However, the equilibrium constant for the dissociation of H$_2$SO$_4$ to bisulfate ions, which is the one of the fundamental parameters controlling the evaporation of sulfur particles, is not well constrained. In this study we explore the volatility of sulfate particles at very low relative humidity. We measured the evaporation of sulfur particles versus temperature and relative humidity in the CLOUD chamber at CERN. We modelled the observed sulfur particle shrinkage with the ADCHAM model. Based on our model results, we conclude that the sulfur particle shrinkage is mainly governed by H$_2$SO$_4$ and potentially to some extent by SO$_3$ evaporation. We found that the equilibrium constants for the dissociation of H$_2$SO$_4$ to HSO$_4^-$ (K$_{H2SO4}$) and the dehydration of H$_2$SO$_4$ to SO$_3$ ($^+$K$_{SO3}$) are K$_{H2SO4}$ = 2–4 × 10$^9$ mol kg$^{-1}$ and $^+$K$_{SO3}$ ≥ 1.4 × 10$^{10}$ at 288.8 ± 5 K.

1 Introduction

Suspended particulate matter in the atmosphere plays a key role in Earth’s climate. Atmospheric aerosol particles affect the amount of solar radiation absorbed by the Earth system. This is accomplished either when atmospheric aerosol particles directly absorb or scatter incoming solar energy (causing warming or cooling) or when particles act as cloud condensation or ice nuclei (leading to an increase in cloud albedo, which causes cooling). A substantial fraction of particle number and mass across a wide range of environmental conditions arises from sulfur emissions (Clarke et al., 1998; Turco et al., 1982).

Sulfur in Earth’s atmosphere in turn originates from natural phenomena like volcanic eruptions and biota decomposition. Violent volcanic eruptions can loft sulfur dioxide (SO$_2$) to the stratosphere, which can then form sulfur aerosol particles. Those sulfur aerosols can remain suspended in the stratosphere for ~1–2 years before falling into the troposphere (Wilson et al., 1993; Deshler, 2008). The three main natural agents for sulfate aerosol formation in troposphere are dimethyl sulfide (DMS), which arises from marine phyto-
plankton decomposition (Charlson et al., 1987; Kiene, 1999; Simó and Pedrós-Alió, 1999). SO$_2$, which occurs naturally as a decay product of plant and animal matter (Grädel and Crutzen, 1994; Hübbert, 1999; Capaldo et al., 1999), and carbonyl sulfide (OCS), which is emitted from anaerobic biological activity and provides the main non-volcanic flux of sulfur into the stratosphere (Galloway and Rodhe, 1991; Rhode, 1999).

The atmospheric sulfate burden is substantially perturbed by sulfur emissions associated with anthropogenic activities. The largest anthropogenic source of sulfur is fossil-fuel combustion; coal is the predominant source, but also heavy fuel oil is important (Öm et al., 1996; Smith et al., 2001). Fossil-fuel combustion constitutes ~ two-thirds of the total global sulfur flux to the atmosphere (Rhode, 1999; Wen and Carignan, 2007) and dominates emissions in most populated regions. Other anthropogenic factors also affect the sulfuric acid (H$_2$SO$_4$) budget, notably sulfur aerosol formation in aircraft plumes (Fahey et al., 1995; Curtius et al., 1998), and extensive sulfur use in industry with a direct environmental impact on local scale. However, on a regional to global scale the acidification of fresh water and forest ecosystems is mainly caused by wet and dry deposition of SO$_2$ and sulfate particles (Simpson et al., 2006).

Sulfur is also a crucial constituent in Venus’ atmosphere, an environment with very low relative humidity (RH) (Moroz et al., 1979; Hoffman et al., 1980), forming the main cloud layer in the form of sulfuric acid droplets (Donahue et al., 1982), which are maintained in an intricate photochemical cycle (photooxidation of OCS; Prinn, 1973). Sulfuric acid’s reaction paths remain a subject of investigation (Zhang et al., 2010), which makes the study of the sulfur cycle (including the sulfur species SO, SO$_2$, SO$_3$, H$_2$SO$_4$) an important endeavour for understanding both the chemistry and climate of Venus (Mills et al., 2007; Hashimoto and Abe, 2000).

H$_2$SO$_4$ serves as an effective nucleating species and, thus, strongly influences atmospheric new-particle formation (Laaksonen and Kulmala, 1991; Weber et al., 1999; Kulmala et al., 2000; Yu and Turco, 2001; Fiedler et al., 2005; Kuang et al., 2008). The nucleation rate, which is the formation rate (cm$^{-3}$ s$^{-1}$) of new particles at the critical size, strongly depends upon the saturation ratio of H$_2$SO$_4$. Uncertainty in this ratio results in an uncertainty of several orders of magnitude in the calculated nucleation rate (Roedel, 1979). To model the excess H$_2$SO$_4$ responsible for the gas-to-particle conversion it is necessary to know the vapour pressure of H$_2$SO$_4$ over sulfuric acid and/or neutralised solutions.

The sulfuric acid vapour pressure appears through the free-energy term in the exponent of the new-particle formation rate (Volmer and Weber, 1926; Stauffer, 1976). Quantitative theoretical predictions of nucleation rates are highly uncertain because the pure H$_2$SO$_4$ equilibrium vapour pressure is not well known (Gmitro and Vermeulen, 1964; Doyle, 1961; Kiang and Stauffer, 1973). However, accurate calculations of the H$_2$SO$_4$ vapour pressure require accurate equilibrium rate constant values to constrain the reactions of formation and dissociation of H$_2$SO$_4$ in aqueous solutions.

While H$_2$SO$_4$ is often presumed to be practically non-volatile, this is not always the case. There are several circumstances on Earth and Venus where the vapour pressure of H$_2$SO$_4$ matters: specifically, at very low RH, high temperature ($T$), when there is a deficit of stabilising bases, and when particles are very small. A very important region of Earth’s environment is the upper stratosphere, where these conditions prevail (Vaida et al., 2003). Under these conditions H$_2$SO$_4$ can evaporate from particles. This can either inhibit growth of nanoparticles or lead them to shrink.

Furthermore, molecular H$_2$SO$_4$ is never the dominant constituent in sulfuric acid solutions. It will completely dehydrate to sulfur trioxide (SO$_3$, which is extremely volatile) in a truly dry system and yet almost entirely dissociate into bisulfite ion (HSO$_4^-$) and hydronium cation (H$_3$O$^+$) in the presence of even trace water (H$_2$O) (Clegg and Brimblecombe, 1995). This is why H$_2$SO$_4$ is such a powerful desiccant. Also, bases such as ammonia (NH$_3$) will enhance chemical stabilisation and form sulfate salts. The thermodynamics of the H$_2$SO$_4$–H$_2$O system at low RH are uncertain, so we seek to improve our understanding of this part of the phase diagram. To accomplish this, we measured the shrinkage of nearly pure H$_2$SO$_4$ particles in the CLOUD chamber at CERN at very low RH and then simulated these experiments with an aerosol dynamics model coupled with a thermodynamics model to constrain the equilibrium constants, for the dissociation $K_{H_2SO_4}$ and the dehydration $k_{H_2SO_4}$, of H$_2$SO$_4$ coupling HSO$_4^-$, H$_2$SO$_4$, and SO$_3$. These new values can be used in models that simulate the evolution of sulfate aerosol particles in the atmospheres of Venus and Earth.

2 Aqueous-phase sulfuric acid reactions

H$_2$SO$_4$ dissociation and potential dehydration to SO$_3$ are the principal subjects of this study. In aqueous solutions H$_2$SO$_4$ can dissociate in two steps.

\[
\text{H}_2\text{SO}_4\text{(aq)} \rightleftharpoons K_{H_2SO_4} \text{HSO}_4^-(aq) + H^+ \quad (R1)
\]

\[
\text{HSO}_4^-(aq) \rightleftharpoons K_{HSO_4^-} \text{SO}_3(aq)^2^- + H^+ \quad (R2)
\]

H$_2$SO$_4$ partially dissociates to form HSO$_4^-$ via Reaction (R1). $K_{H_2SO_4}$ represents the equilibrium constant for Reaction (R1). HSO$_4^-$ can then undergo a second dissociation Reaction (R2) to form a sulfate ion ($\text{SO}_3^{2-}$). In the above reactions, sulfur’s oxidation number is 6 ($\text{S(VI)}$).

For dilute aqueous solutions, Reaction (R1) is considered to be complete. However, when the mole fraction of S(VI) exceeds ~0.5, H$_2$SO$_4$ can be detected in the solution (Walarfan et al., 2000; Margarella et al., 2013). When H$_2$SO$_4$ is present in the solution, dehydration of H$_2$SO$_4$ to form SO$_3$ (Reaction R3) can also be important (Wang et al., 2006; Que...
et al., 2011). $K_{SO_3}$ represents the equilibrium constant for Reaction (R3) on a mole fraction basis.

$$\text{SO}_3^{\text{aq}} + \text{H}_2\text{O} \rightleftharpoons \text{H}_2\text{SO}_4^{\text{aq}}$$ (R3)

NH$_3$, which mainly originates from anthropogenic agriculture emissions, is the most abundant base in atmospheric secondary aerosol particles. NH$_3$ neutralises sulfuric acid particles by reacting with H$^+$ and forming an ammonium ion (NH$_4^+$) (Reaction R4).

$$\text{NH}_3^{\text{aq}} + \text{H}^+ \rightleftharpoons \text{NH}_4^+$$ (R4)

Even in the cleanest environments, such as the stratosphere, NH$_3$ is present at low concentrations and NH$_3$(g) will be dissolved in the acidic sulfate particles.

3 Methods

In the CLOUD (Cosmics Leaving OUtdoor Droplets; Kirkby et al., 2011) chamber at CERN, we measured the H$_2$SO$_4$ aerosol particle evaporation under precisely controlled temperature and relative humidity. We designed experiments to accomplish a gradual decrease in RH (from 11.0 to 0.3 %) under atmospherically relevant conditions. To understand the processes governing the measured particle evaporation, we modelled the experiments with the Aerosol Dynamics, gas- and particle-phase chemistry model for laboratory CHAMber studies (ADCHAM; Roldin et al., 2014).

3.1 Experimental setup

Details of the CLOUD chamber, the main element of the experimental setup can be found in Kirkby et al. (2011) and Duplissy et al. (2016). For the experiments described here, we formed and grew sulfuric acid particles in the chamber by oxidising SO$_2$ with OH radicals that were generated by photolysing O$_3$ and allowing the resulting O($^1$D) to react with water vapour. During these experiments we fed the aerosol population to an array of instruments for characterisation of both physical and chemical properties.

We utilised the following instruments to measure gas-phase concentrations: a SO$_2$ monitor (enhanced trace level SO$_2$ 15 analyser, model 43i-TLE, Thermo Scientific, USA), an O$_3$ monitor (TEI 49C, Thermo Environmental Instruments, USA) and a chemical ionisation mass spectrometer (CIMS) to measure the gas-phase H$_2$SO$_4$ concentration ([H$_2$SO$_4$(g)] between $\sim 5 \times 10^5$ and $\sim 3 \times 10^6$ cm$^{-3}$; Kürten et al., 2011, 2012). The CIMS data provided the total gaseous sulfuric acid concentration, [H$_2$SO$_4$(g)], without constraining the hydration state of the evaporating molecules (e.g. H$_2$SO$_4$ associated with one, two, or three H$_2$O molecules).

We measured the evolution of the aerosol number size distribution with a scanning mobility particle sizer (SMPS; Wang and Flagan, 1990), which recorded the dry particle mobility diameter in the size range from about 10 to 220 nm. We operated the SMPS system with a recirculating dried sheath flow (RH $< 14 \%$ controlled by a silicon dryer) with a sheath to aerosol sample flow ratio of 3 : 0.3 L. We maintained the differential mobility analyser (DMA) and recirculating system at 278–288 K by means of a temperature control rack, while we operated the condensation particle counter (CPC) at room temperature. We corrected the SMPS measurements for charging probability, including the possibility of multiple charges, diffusion losses, and CPC detection efficiency.

We measured aerosol particle chemical composition with an Aerodyne aerosol mass spectrometer (AMS) quantifying sulfate, nitrate, ammonium and organics for particles between 50 and 1000 nm aerodynamic diameter (Jimenez et al., 2003; Drewnick et al., 2006; Canagaratna et al., 2007). The AMS provided the mass concentration measurements (µg m$^{-3}$) calculated from the ion signals by using measured air sample flow rate, nitrate ionisation efficiency (IE) and relative IE of the other species.

3.2 The experimental procedure

To study aerosol particle evaporation, the formation of sulfuric acid particles preceded. At the lowest H$_2$O levels (RH $< 11 \%$) and in the presence of O$_3$, controlled UV photo-excitation reactions initiated the oxidation of SO$_2$ to H$_2$SO$_4$. Sulfuric acid particles nucleated and grew to a size of $\sim 220$ nm by condensation of H$_2$SO$_4$(g) at a quasi-constant gas-phase concentration ($\sim 1 \times 10^9$ cm$^{-3}$ with an uncertainty of $> 20 \%$). The H$_2$SO$_4$ formation and particle growth ended when we closed the shutters in the front of the UV light source. Afterwards, we induced particle shrinkage by decreasing the RH. We decreased the RH in two separate ways; either by minimising the influx of water vapour to the chamber, or by increasing the temperature. This separation in experimental procedures gave the ability to achieve and control extremely low RH values (Table 1).

After the end of the particle formation period and during the initial steps of evaporation, before the RH started to decrease, the aerosol size distribution remained nearly constant. Subsequently, the RH decreased gradually initiating the particle evaporation. When the RH reached a certain low value (RH $< 1.5 \%$ for $T = 288.8$ K) the particles shrank rapidly, as revealed by the SMPS measurements, and the [H$_2$SO$_4$(g)] increased until it reached a peak value (see Supplement, Fig. S1). The [H$_2$SO$_4$(g)] peak was significantly higher than the background concentration before the onset of evaporation (Table 1). After reaching a maximum in gas-phase concentration, the sulfuric acid decreased again, though the size distribution remained stable (e.g. $\sim 50$ (±10) nm for experiments 1 and 2; see Sect. 4.3) depending on the RH and T conditions. This behaviour revealed that the remaining aerosol could not be pure sulfuric acid but rather consisted of a more stable chemical mixture that inhibited further evaporation.
Similarly, the AMS recorded the evaporation of particles (see Supplement, Fig. S1). The AMS measurements showed that the particles were composed almost exclusively of sulfuric acid (but not pure H$_2$SO$_4$). Based on AMS data, calculations of the kappa value ($\kappa$; Petters and Kreidenweis, 2007), which is defined as a parameter that describes the aerosols water uptake and cloud condensation nucleus activity (CCN activity), of the mixed particles as a function of time during particle evaporation (see Supplement, Fig. S2) yield a value close to the $\kappa$ for pure sulfuric acid particles (Sullivan et al., 2010). A $\kappa$ value is indicative of the solubility of aerosol particles, with $\kappa = 0$ referring to an insoluble particle and $\kappa = 0.7$ to pure sulfuric acid particles. $\kappa$ is computed by the approximate equation, Eq. (1)

$$ \kappa = \frac{4 \cdot A^3}{27 \cdot D_4^3 \cdot \ln S_c} $$

(1)

when the critical diameter $D_4$ and critical saturation $S_c$ (or supersaturation, $s_c$, when referring to CCN activity) are known. The term $A$ can be calculated from the water properties.

### 3.3 The model framework

In the present work we use ADCHAM (Roldin et al., 2014, 2015) to study the evolution of the particle number size distribution and particle chemical composition. Instead of simulating the new-particle formation in the CLOUD chamber, we use the measured particle number size distribution before the UV lights are turned off as well as time sequences of RH, $T$ and [H$_2$SO$_4(g)$] as inputs to the model (Fig. 1). In order to capture the evolution of the particle number size distribution we consider Brownian coagulation, particle wall deposition, condensation and evaporation of H$_2$SO$_4$, SO$_3$ and H$_2$O from the particles.

#### 3.3.1 The activity coefficients

Within an aqueous electrolyte solution, such as the H$_2$SO$_4$–SO$_3$–H$_2$O system, cations, anions and molecular species all disrupt ideality. Here, we consider interactions between ions (HSO$_4^-$, SO$_4^{2-}$, NH$_4^+$, H$^+$) and molecules (H$_2$SO$_4$, SO$_3$, H$_2$O) in the particle-phase chemistry model. To calculate the molality-based activity coefficients for the inorganic ions ($\gamma_i$) and the mole-fraction-based activity coefficient for water ($f_{H_2O}$) we apply the Aerosol Inorganic Organic Mixtures Functional groups Activity Coefficients (AIOMFAC) model (validated at room temperatures; Zuend et al., 2008, 2011). The reference state for ions and water in the model is an infinitely dilute aqueous solution ($\gamma_i (\chi_{H_2O} \rightarrow 1) = 1$ and $f_{H_2O}(\chi_{H_2O} \rightarrow 1) = 1$).

For relatively dilute H$_2$SO$_4(aq)$ solutions (low solute concentration), typical for most atmospheric conditions, it is reasonable to assume that the dissociation of H$_2$SO$_4$ to HSO$_4^-$ (Reaction R1) is complete (Clegg et al., 1998; Zuend et al., 2008). However, in this work we demonstrate that this assumption fails at low RH and also for small particles with a large Kelvin term. Furthermore, at a very low water activity ($\alpha_{w}$) (less than $\sim 0.01$) a non-negligible fraction of the H$_2$SO$_4$ could potentially decompose to SO$_3$ (Reaction R3); if this is the case, the thermodynamic model need to consider not only Reaction (R1) but (R3) as well (Fig. 1).

Since AIOMFAC does not consider inorganic non-electrolyte compounds like H$_2$SO$_4$ and SO$_3$ we implement additionally to this the symmetric electrolyte-NonRandom Two-Liquid (eNRTL) activity coefficient model (Bollas et al., 2008; Song and Chen, 2009) which is optimised for the H$_2$SO$_4$–H$_2$O–SO$_3$ systems by Que et al. (2011). In this work we use the repressed eNRTL binary interaction parameters from Que et al. (2011). Following the convention of the eNRTL model (Chen et al., 1982), we set the unknown binary parameters for NH$_4^+$–molecule, molecule–NH$_4^+$ and NH$_4^+$–ions to $−4$, $8$ and $0$, respectively.

The reference state of the molecular species in eNRTL is defined as the pure liquid. eNRTL provides mole-fraction-based activity coefficients for H$_2$SO$_4$ and SO$_3$, $f_{H_2SO_4}$ and $f_{SO_3}$, respectively. ADCHAM calculates $f_{H_2SO_4}$ and $f_{SO_3}$ as a function of $\alpha_{w}$ and $N:S: \chi_{N(-III)}: \chi_{S(VI)}$ (Fig. S3). The modelled $f_{H_2SO_4}$ and $f_{SO_3}$ approach unity not only at the standard state of the pure liquids ($f_{H_2SO_4}(\chi_{H_2SO_4} \rightarrow 1) = 1$ and $f_{SO_3}(\chi_{SO_3} \rightarrow 1) = 1$), but also for the infinitely dilute aqueous solution ($f_{H_2SO_4}(\chi_{H_2O} \rightarrow 1) = 1$ and $f_{SO_3}(\chi_{H_2O} \rightarrow 1) = 1$). This is because the eNRTL binary H$_2$O–H$_2$SO$_4$ and H$_2$O–SO$_3$ interaction parameters are zero in the model. For all conditions between these limiting states, the short-range ion (HSO$_4^-$, SO$_4^{2-}$, NH$_4^+$, H$^+$)–molecule (H$_2$SO$_4$, SO$_3$, H$_2$O) interactions, and Pitzer–Debye–Hückel long-range ion–molecule interactions influence the modelled $f_{H_2SO_4}$ and $f_{SO_3}$.
f\text{SO}_3. At T = 288.8 K, f\text{H}_2\text{SO}_4 reaches the highest values (~2.29) when a_w ≈ 0.25 and f\text{SO}_3 reaches the highest values (~1.95) when a_w ≈ 0.35 (Fig. S3). We also assume that the activity coefficient of NH_3 is unity for the model simulations. However, sensitivity tests performed for γ_{\text{NH}_3}=0.1 and γ_{\text{NH}_3}=10 reveal that, for the acidic particles (N : S < 1), our model results are completely insensitive of the absolute value of γ_{\text{NH}_3}.

### 3.3.2 The particle-phase composition

If ammonium cation (NH_4\textsuperscript{+}) is present in the sulfuric acid particles, then solid ammonium bisulfate (NH_4\text{HSO}_4(s)) may form when the S(VI) and H_2O start to evaporate from the particles. However, the particles may also stay as highly supersaturated droplets with respect to the crystalline phase (Zuend et al., 2011). The particle number size distribution measurements in our experiments do not indicate a sudden drop in particle size during evaporation. This is expected when the particles crystalise and all particle water is suddenly removed. Thus, in the present work we do not consider formation of any solid salts. We further neglect the influence of any mass-transfer limitations in the particle phase, and assume that the particle ion-molecule equilibrium composition (Reactions R1–R3) and water content can be modelled as equilibrium processes (because they are established rapidly compared to the composition change induced by the evaporation of H\textsubscript{2}SO\textsubscript{4} and SO\textsubscript{3}). We use the thermodynamic model to update the particle equilibrium water content, mole fractions and activity coefficients of all species. Then the model considers the gas–particle partitioning of H\textsubscript{2}SO\textsubscript{4} and SO\textsubscript{3} with a condensation algorithm in the aerosol dynamics model (Sect. 3.3.5). The time step set in the model is 1 s.

The thermodynamic model uses an iterative approach to calculate the particle equilibrium mole fractions of H\textsubscript{2}O, H\textsubscript{2}SO\textsubscript{4}, SO\textsubscript{3}, H\textsubscript{2}SO\textsubscript{4}\textsuperscript{−}, SO\textsubscript{4}\textsuperscript{2−}, NH\textsubscript{3}, NH\textsubscript{4}\textsuperscript{+} and H\textsuperscript{+}, based on the current time step, known RH, and absolute number of moles of S(VI) and N(-III) for each particle size bin. The modelled particle-phase mole fraction of N(-III) during the evaporation experiments is always substantially lower than that of S(VI) (N : S < 0.7). For these particles the saturation vapour pressure of NH\textsubscript{3} is always less than 10\textsuperscript{−10} Pa, within the experimental water activity range 0–0.11 and γ_{\text{NH}_3} ≥ 0.1. Thus, it is reasonable to assume that during the experiments NH\textsubscript{3} does not evaporate from the particles.

Based on the particle diameters from the previous time step (which depend on the particle water content), the thermodynamic model starts by calculating a_w for each particle size, considering the Kelvin effect. Given a_w, the model estimates the particle water mole fraction. Then the model calculates the H\textsuperscript{+} molality in the aqueous phase via a fourth-order polynomial, derived from the ion balance equation, Eq. (2), in combination with the thermodynamic equilibrium constant equations, Eqs. (3)–(6), and the S(VI) and N(-III) mole balance equations, Eqs. (7) and (8), respectively. The maximum positive real root of this polynomial gives the H\textsuperscript{+}
concentration, $[\text{H}^+]$.  
\[ [\text{H}^+] + [\text{NH}_4^+] = [\text{HSO}_4^-] + 2[\text{SO}_4^{2-}] \]  
(2)

\[ K_{\text{H}_2\text{SO}_4} = \left[ \frac{[\text{HSO}_4^-] \cdot [\text{H}^+] \cdot [\text{H}_2\text{SO}_4]}{[\text{H}_4\text{SO}_4]} \right] \]  
(3)

\[ K_{\text{HSO}_4} = \left[ \frac{[\text{SO}_4^{2-}] \cdot [\text{H}^+] \cdot [\text{H}_2\text{SO}_4]}{[\text{H}_2\text{SO}_4]} \right] \]  
(4)

\[ K_{\text{SO}_3} = \frac{[\text{H}_2\text{SO}_4] \cdot [\text{H}_2\text{O}]}{[\text{SO}_4^2^-] \cdot [\text{H}_4\text{SO}_4]} \]  
(5)

\[ K_{\text{NH}_3} = \left[ \frac{[\text{NH}_4^+]}{[\text{H}^+] \cdot [\text{NH}_3]} \right] \]  
(6)

\[ n_{\text{SO}_2(\text{V})} = n_{\text{H}_2\text{SO}_4} + n_{\text{HSO}_4^-} + n_{\text{SO}_4^{2-}} + n_{\text{SO}_3} \]  
(7)

\[ n_{\text{N}(-\text{III})} = n_{\text{NH}_3} + n_{\text{NH}_2}\text{O} \]  
(8)

The thermodynamic equilibrium coefficients for $\text{H}_2\text{SO}_4$ and $\text{HSO}_3$ dissociations and $\text{NH}_3$ protonation (Eqs. 3, 4 and 6) are given in a molality-based form while the equilibrium coefficient in Eq. (5), which involves the equilibration between the different solvents ($\text{H}_2\text{O}$, $\text{SO}_3$ and $\text{H}_2\text{SO}_4$), is given in a mole-fraction-based form. The Eq. (5) is given in a mole-fraction-based form for the following reasons: (a) the eNRTL provides mole-fraction-based activity coefficients, and (b) if Eq. (5) were to be applied for $a_w$ that are even lower than considered in this work, the assumption of using molalities, i.e. water is considered to be the only solvent, would not be acceptable. The model calculates $K_{\text{HSO}_4}$ and $K_{\text{NH}_3}$ (mol kg$^{-1}$) with Eqs. (9) and (10) (Jacobson, 2005). We treat $K_{\text{H}_2\text{SO}_4}$ and $K_{\text{SO}_3}$ as unknown model fitting parameters.

\[ K_{\text{H}_2\text{SO}_4} = 1.015 \times 10^{-2} \cdot e^{\left(8.85 \cdot \left(\frac{298}{T} - 1\right) + 25.14 \cdot \left(1 + \ln \left(\frac{298}{T}\right) - 298\right)\right)} \]  
(9)

\[ K_{\text{NH}_3} = 1.7882 \times 10^9 \cdot e^{21.02 \left(\frac{298}{T} - 1\right)} \]  
(10)

Once $[\text{H}^+]$ is estimated, all other ion and molecule concentrations can be derived from Eqs. (2)–(8). Based on the new estimated particle-phase ion and molecule mole fractions, the thermodynamic model uses AIOMFAC and eNRTL to update the ion and molecule activity coefficients. The model then repeats the whole procedure iteratively until the relative change in the concentration and activity coefficients for each compound is less than $10^{-9}$ between successive iteration steps. To stabilise convergence, the model estimates activity coefficients used in the proceeding iteration as a weighted average of the values from the previous and present iteration time steps.

### 3.3.3 $\text{H}_2\text{SO}_4$ and $\text{SO}_3$ in the gas phase

In the gas phase only a fraction of $\text{H}_2\text{SO}_4$ is in the form of pure sulfuric acid molecules while the rest of the $\text{H}_2\text{SO}_4$ is in a hydrated form. In this work we use the parameterisation from Hanson and Eisele (2000), who measured the diffusion loss rate of $\text{H}_2\text{SO}_4$ to flow-tube walls at different RH, to estimate the RH-dependent effective diffusion coefficient of $\text{H}_2\text{SO}_4(g)$.

In the gas phase, $\text{SO}_3$ reacts rapidly with $\text{H}_2\text{O}$ to form $\text{H}_2\text{SO}_4$. Based on the measured loss rate of $\text{SO}_3$, which shows a second-order dependence on the water vapour concentration (Jayne et al., 1997), we estimate that $\text{SO}_3(g)$ is converted to $\text{H}_2\text{SO}_4(g)$ in less than 1 s during the CLOUD chamber experiments, even at the lowest RH. Because of this rapid conversion to $\text{H}_2\text{SO}_4$ and the high vapour pressure of $\text{SO}_3$ (Eq. 12), it is reasonable to assume that the gas-phase concentration of $\text{SO}_3$ (vapour pressure, $p_{\infty,\text{SO}_3}$) is negligibly low.

#### 3.3.4 Saturation vapour pressures, surface tension and particle density

We use Eqs. (11) and (12) to calculate the temperature-dependent sub-cooled pure-liquid saturation vapour pressures for $\text{H}_2\text{SO}_4$ and $\text{SO}_3$ ($p_{0,i}$, where $i$ refers to $\text{H}_2\text{SO}_4$ or $\text{SO}_3$ in Pa). Equation (11) is based on the work of Ayers et al. (1980), with corrections for lower temperatures by Kulmala and Laaksonen (1990). We use the (best fit) L parameter value of $-11.695$ (Noppel et al., 2002, Noppel–Kulmala–Laaksonen, N–K–L, parameterisation; see Supplement Fig. S5a). Equation (12) is based on the work of Nickless (1968) (see Supplement Fig. S5b).

\[ p_{0,\text{H}_2\text{SO}_4} = 101.325 \cdot e^{\left(L + 10.156 \left[\frac{1}{\text{mol} \cdot \text{K}} - 0.38 \cdot \ln \left(\frac{360.15}{T}\right) - 360.15\right]\right)} \]  
(11)

\[ p_{0,\text{SO}_3} = e^{\left(28.9239 - \frac{7000}{T}\right)} \cdot 133.3224 \]  
(12)

As an alternative to Eqs. (11) and (12) we also use the $\text{H}_2\text{SO}_4$ and $\text{SO}_3$ pure-liquid saturation vapour pressure parameterisations from Que et al. (2011) (originally from the Aspen Plus Databank, Fig. S5).

We calculate the saturation vapour pressures of $\text{H}_2\text{SO}_4$ and $\text{SO}_3$ for each particle size with Eq. (13), using the mole fractions ($\chi_{i,j}$) and mole-fraction-based activity coefficients ($f_{i,j}$) of $\text{H}_2\text{SO}_4$ and $\text{SO}_3$ (from the thermodynamic model) and the Kelvin term, $C_{k,i,j}$ Eq. (14) for compound $i$ in particle size bin $j$.

\[ p_{s,i,j} = p_{0,i} \cdot a_{i,j} \cdot C_{k,i,j} \]  
(13)

where $a_{i,j} = \chi_{i,j} \cdot f_{i,j}$

\[ C_{k,i,j} = e^{\left(\frac{4 \cdot M_i \cdot a_{j}}{R \cdot T \cdot \rho_{p,j}^{3/2}}\right)} \]  
(14)

$a_{i,j}$ is the activity of compound $i$ in size bin $j$, $T$ is the temperature in kelvin, $R$ is the universal gas constant (J mol$^{-1}$ K$^{-1}$), $M_i$ is the molar mass (kg mol$^{-1}$) of compound $i$, $\rho_{p,j}$ is the density (kg m$^{-3}$) of the liquid particles.
\[\sigma_j \text{ is the surface tension (N m}^{-1}\text{) and } D_{p,j} \text{ is the diameter (m) of the particles in size bin } j.\]

As an alternative approach we also model the evaporation of H\(_2\)SO\(_4\) using composition-dependent H\(_2\)SO\(_4\) activities \(\left(\alpha_{H_2SO_4,i,j}\right)\) derived directly from the tabulated values of the difference in chemical potentials between the sulphuric acid in aqueous solution and that of the pure acid \(\left(\mu_{H_2SO_4,i,j} - \mu_0^{H_2SO_4}\right)\). The tabulated values that are valid at 298.15 K are taken from Giauque et al. (1960). The relationship between \(\mu_{H_2SO_4,i,j} - \mu_0^{H_2SO_4}\) and \(\alpha_{H_2SO_4,i,j}\) is given by Eq. (15).

\[
\ln(\alpha_{H_2SO_4,i,j}) = (\mu_{H_2SO_4,i,j} - \mu_0^{H_2SO_4})/(RT) \quad (15)
\]

In accordance with Ayers et al. (1980) we neglect any temperature dependence of \(\mu_{H_2SO_4,i,j} - \mu_0^{H_2SO_4}\). This empirically based approach is used in several chemistry transport models to simulate the evaporation of pure sulfuric acid particle in the stratosphere (see, e.g., Kokkola et al., 2009; English et al., 2011; Hommel et al., 2011).

We calculate the surface tension and density of the particles comprising a ternary mixture of water, sulfuric acid and ammonium with parameterisations given by Hyvärinen et al. (2005) that combine surface tension parameterisations for (NH\(_4\))\(_2\)SO\(_4\)-H\(_2\)O mixtures (Hämeri et al., 2000; Korhonen et al., 1998b), H\(_2\)SO\(_4\)-H\(_2\)O mixtures (Vehkamäki et al., 2002) and NH\(_3\)-H\(_2\)O mixtures (King et al., 1930). For the range of conditions in our experiments the minimum particle diameter after evaporation is \(\sim 50 \pm 20\) nm (for experiments 1 and 2). The Kelvin effect only increases the water saturation vapour pressure by maximum value of 1.07 (and the H\(_2\)SO\(_4\) saturation vapour pressure by 1.44; see Supplement Fig. S6) for the particle diameter of 40 nm.

### 3.3.5 Evaporation of H\(_2\)SO\(_4\), SO\(_3\) and H\(_2\)O

We model the gas-particle partitioning (evaporation) of H\(_2\)SO\(_4\) and SO\(_3\) using the full moving size distribution method in combination with the Analytic Prediction of Condensation (APC) scheme (Jacobson, 2005). APC is an unconditionally stable numerical discretisation scheme used to solve the condensation equation, Eq. (16). In Eq. (16), we substitute the saturation vapour pressures from Eq. (13) and the measured concentration, \(C_{\infty,H_2SO_4}(g)\) (vapour pressure, \(p_{\infty,H_2SO_4(g)}\)) of H\(_2\)SO\(_4\)(g). Based on the motivation given in Sect. 3.3.3 the vapour pressure of SO\(_3\), \(p_{\infty,SO_3(g)}\), is set to zero.

\[
\frac{dm_{i,j}}{dt} = \frac{2 \cdot \pi \cdot (d_i + d_j) \cdot (D_i + D_j) \cdot M_i}{R \cdot T} \cdot \beta_{i,j} \left(\bar{\alpha}_{i,j} \cdot \left(p_{\infty,i} - p_{t,i,j}\right)\right) \quad (16)
\]

\[
\beta_{i,j} \left(\bar{\alpha}_{i,j} \cdot \left(p_{\infty,i} - p_{t,i,j}\right)\right) = \frac{K_{n_{i,j}} + 1}{0.377 \cdot K_{n_{i,j}} + 1 + \frac{4}{3 \cdot \alpha_i} \cdot \left(K_{n_{i,j}}^2 + K_{n_{i,j}}\right)} \quad (17)
\]

\[
K_{n_{i,j}} = \frac{2 \cdot \lambda_{i,j}}{d_i + d_j} \quad \lambda_{i,j} = \frac{3 \cdot (D_i + D_j)}{\sqrt{v_i^2 + v_j^2}} \quad (18)
\]

Equation (16) describes the contribution of species \(i\) to the mass growth rate of a particle in size bin \(j\). \(\beta_{i,j}\) is the Fuchs–Sutugin correction factor in the transition region (Fuchs and Sutugin, 1971), \(d_i, d_j\) correspond to diameters (m) and \(D_i, D_j\) to diffusion coefficients (\(m^2\ s^{-1}\)) of the condensing molecule \(i\) and the particles in size bin \(j\), respectively. \(\alpha_i\) is the mass-accommodation coefficient of compound \(i\) and \(K_{n_{i,j}}\) is the non-dimensional Knudsen number, Eq. (17). \(\lambda_{i,j}\) is the mean free path (m) and \(v_i\) and \(v_j\) are the thermal speeds (m s\(^{-1}\)) of the molecule \(i\) and the particles in size bin \(j\), respectively. Equations (16) and (17) take into account that the condensing molecules have a non-negligible size compared to the size of the smallest particles, and that small particles have non-negligible diffusion coefficients (Lehtinen and Kulmala, 2003).

Based on measurements of H\(_2\)SO\(_4\) losses in a flow tube reactor, Pöschl et al. (1998) derived a mass accommodation coefficient of \(H_2SO_4(g)\) on aqueous sulfuric acid, which was close to unity, with a best fit value of 0.65, a lower limit value of 0.43 and an upper limit of 1.38 (physical limit 1.0). The measured mass accommodation coefficients do not show any dependence on the relative amount of water in the particles (Pöschl et al., 1998). For the model simulations in this work we use unity mass accommodation coefficients. The particle water content is modelled as an equilibrium process with the thermodynamic model (see Sect. 3.3.2).

### 3.3.6 Particle losses

The electric field strength of the stainless-steel CLOUD chamber, in contrast to smog chambers made of Teflon, is very low. Therefore, we can neglect electrostatic deposition enhancements (for details on how ADCHAM treats particle wall deposition losses see Roldin et al., 2014). We simulate the particle-size-dependent deposition losses with the model from Lai and Nazaroff (2000). The particle deposition loss depends on the friction velocity \(u^*\), which we treat as an unknown model fitting parameter. The best possible agreement between the modelled and measured particle number and volume concentration in the chamber is achieved with a friction velocity of \(\sim 0.2\) m s\(^{-1}\). Thus, for all model results we present in this article we use \(u^* = 0.2\) m s\(^{-1}\). Dilution
losses due to the purified air injected to the CLOUD chamber are also considered in the model.

3.3.7 Constraining the thermodynamic properties of sulfate aerosol particles

We use ADCHAM to constrain the values of the thermodynamic equilibrium coefficients, \( K_{H_2SO_4} \) and \( K_{SO_3} \), by treating these coefficients as unknown model fitting parameters. By varying the equilibrium coefficients we search for the best possible agreement (coefficient of determination \( R^2 \); see Supplement, Table S1) between the modelled and measured geometric mean diameter (GMD) with respect to particle number. Because experimental results reveal that the sulfate particles did not evaporate completely, they must have been contaminated with a small fraction of effectively non-volatile material (Sect. 3.2).

In the model we address this by assuming either that the particles (prior to evaporation) contained a small fraction of non-volatile organic material (e.g. secondary organic aerosol, SOA) or that the particles contained small amounts of ammonium, which prevented pure H\(_2\)SO\(_4\) or that the particles contained small amounts of ammonium, which prevented pure H\(_2\)SO\(_4\) particle formation and consequently prevented the evaporation. We calculate the initial SOA and ammonium dry particle volume fraction in particle size bin \( j \) (\( \chi_{SOA,j} \) and \( \chi_{NH4+,j} \)) with Eqs. (19) and (20), respectively. Here \( d_{SOA} \) and \( d_{NH4}^+ \) represent an effective particle diameter of SOA and ammonium if all other particle species are removed. For experiment 1 we use \( d_{SOA} = 60 \) nm and \( d_{NH4}^+ = 26 \) nm, for experiment 2 \( d_{SOA} = 43 \) nm and \( d_{NH4} = 19 \) nm and for experiment 3 \( d_{SOA} = 38 \) nm and \( d_{NH4} = 17 \) nm.

\[
\chi_{SOA,j} = \min \left( \frac{d_{SOA}^3}{d_j^3}, 0.2 \right) \tag{19}
\]

\[
\chi_{NH4+,j} = \min \left( \frac{d_{NH4}^+}{d_j^3}, 0.05 \right) \tag{20}
\]

4 Results and discussion

In order to fit the modelled particle number size distribution evolution to the observations we performed several hundred simulations where we varied \( K_{H_2SO_4} \) and \( K_{SO_3} \). We summarise these simulations into three main categories (cases):

- Case 1: only H\(_2\)SO\(_4\) and H\(_2\)O evaporation (\( K_{SO_3} = \infty \)).

- Case 2: a combination of H\(_2\)SO\(_4\), H\(_2\)O and SO\(_3\) evaporation.

- Case 3: practically only SO\(_3\) and H\(_2\)O evaporation.

Case 2 is further divided into two subcategories, Case 2a and 2b. In Case 2a the H\(_2\)SO\(_4\) is the dominant evaporating S(VI) species while in Case 2b the SO\(_3\) is the dominant evaporating S(VI) species.

4.1 Particle-phase mole fractions

Figure 2 shows an example of the modelled mole fractions of (a) H\(_2\)SO\(_4\)(aq), \( \chi_{H_2SO_4} \), and (b) SO\(_3\)(aq), \( \chi_{SO_3} \), as a function of the water activity \( a_w \) and N:S for Case 2a with equilibrium constants \( K_{H_2SO_4} = 2.40 \times 10^9 \) mol kg\(^{-1}\) and \( K_{SO_3} = 1.43 \times 10^{10} \) at \( T = 288.8 \) K. Figure 2 reveals that the increase in \( \chi_{SO_3} \) as \( a_w \) decreases is steeper than for \( \chi_{H_2SO_4} \). This is because H\(_2\)SO\(_4\) formation precedes SO\(_3\) formation (see Reaction R3). As expected, the highest values of \( \chi_{H_2SO_4} \) and \( \chi_{SO_3} \) occur when N:S = 0 and \( a_w \) approaches zero. While N:S increases, \( \chi_{H_2SO_4} \) and \( \chi_{SO_3} \) decrease gradually and reach lower values when N:S becomes larger than 0.6.

4.2 Particle number size distribution evolution

In Fig. 3 we present the particle number size distribution evolution after the shutter of the UV light is closed and the influx of water vapour to the chamber is interrupted for experiment 2, performed at \( T = 288.8 \) K, showing (a) the measured and (b) the modelled values for Case 2a with \( K_{H_2SO_4} = 2.40 \times 10^9 \) mol kg\(^{-1}\) and \( K_{SO_3} = 1.43 \times 10^{10} \). At the beginning of the evaporation process the particles in the size range from \( \sim 60 \) to \( \sim 180 \) nm in diameter contain approximately 70 mole \% H\(_2\)O; however, this percentage decreases, declining to 15 mole \% after 6 h (Fig. 3c). Before H\(_2\)SO\(_4\) and SO\(_3\)
Particle shrinkage at low RH. Measured (a) and modelled (b) particle number size distribution evolution during experiment 2 performed at \( T = 288.8 \) K for Case 2a, with \( \text{H}_2\text{SO}_4 \) being the dominating evaporating S(VI) species, \( K_{\text{H}_2\text{SO}_4} = 2.40 \times 10^9 \text{ mol kg}^{-1} \) and \( K_{\text{SO}_3} = 1.43 \times 10^{10} \). Panels (c) and (d) show the modelled particle water mole fraction, \( \chi_{\text{H}_2\text{O}} \) and \( \text{N}: \text{S} \), respectively.

Figure 3. Particle shrinkage at low RH. Measured (a) and modelled (b) particle number size distribution evolution during experiment 2 performed at \( T = 288.8 \) K for Case 2a, with \( \text{H}_2\text{SO}_4 \) being the dominating evaporating S(VI) species, \( K_{\text{H}_2\text{SO}_4} = 2.40 \times 10^9 \text{ mol kg}^{-1} \) and \( K_{\text{SO}_3} = 1.43 \times 10^{10} \). Panels (c) and (d) show the modelled particle water mole fraction, \( \chi_{\text{H}_2\text{O}} \) and \( \text{N}: \text{S} \), respectively.

start to evaporate from the particles the assumed mole fraction of ammonium is very low (Fig. 3d). However, during the evaporation process \( \text{N}: \text{S} \) increases steadily until it reaches a value of \( \sim 0.6 \) after \( \sim 6 \) h. At this point the particles are \( \sim 40 \) nm in diameter and do not shrink further. This model result is in good agreement with the experimental results reported by Marti et al. (1997) and confirms that \( \text{NH}_3^+ \) effectively stabilises sulfur particles against evaporation when \( \text{N}: \text{S} \approx 0.6 \). Thus, in the stratosphere, even small amounts of a base (such as \( \text{NH}_3 \)) can prevent the sulphate particles from shrinking.

4.3 Geometric mean diameter shrinkage influenced by relative humidity

Figure 4 compares the measured and modelled GMD evolution as a function of (a) time and (b) RH for experiments 1 and 2 performed at a temperature of \( T = 288.8 \) K (Table 1) with \( \text{NH}_3 \) as a particle-phase contaminant (see Supplement, Table S1, simulations 1–4 and 13–16). The pure-liquid saturation vapour pressures of \( \text{H}_2\text{SO}_4 \) and \( \text{SO}_3 \) are calculated with Eqs. (11) and (12). The model results are in good agreement with the measured GMD trend for Case 1 (\( K_{\text{H}_2\text{SO}_4} = 2.00 \times 10^9 \text{ mol kg}^{-1} \) and \( K_{\text{SO}_3} = 1.43 \times 10^{10} \)), Case 2a (\( K_{\text{H}_2\text{SO}_4} = 2.40 \times 10^9 \text{ mol kg}^{-1} \) and \( K_{\text{SO}_3} = 1.43 \times 10^{10} \)), Case 2b (\( K_{\text{H}_2\text{SO}_4} = 4.00 \times 10^9 \text{ mol kg}^{-1} \) and \( K_{\text{SO}_3} = 1.54 \times 10^{10} \)) and Case 3 (\( K_{\text{H}_2\text{SO}_4} = 1.00 \times 10^{11} \text{ mol kg}^{-1} \) and \( K_{\text{SO}_3} = 3.33 \times 10^7 \)). The Case 3 simulations give a particle shrinkage that begins somewhat too late and occurs somewhat too rapidly. However, considering the measurement uncertainties it is impossible to constrain the relative contribution of \( \text{H}_2\text{SO}_4 \) and \( \text{SO}_3 \) to the observed GMD loss only based on these two experiments (see Sect. 4.4).

With the Aspen Plus Databank pure-liquid saturation vapour pressure parameterisations it is also possible to find similarly good agreement between the modelled and observed GMD evolution during experiment 1 and 2 for cases 1, 2a, 2b and 3 (Fig. S8) with \( \text{NH}_3 \) as the particle-phase contaminant, but with somewhat different values of \( K_{\text{H}_2\text{SO}_4} \) and \( K_{\text{SO}_3} \) (see Supplement, Table S1, simulations 8–11 and 20–23).

The model simulations with non-volatile and non-water-soluble organics or dimethylamine (DMA) as the particle-phase contaminant give nearly identical results to those with \( \text{NH}_3 \), both for experiments 1 and 2 (see Supplement Table S1, simulations 6, 7, 17 and 18). In the case of DMA this occurs because it is also a strong enough base to be completely protonated (all \( \text{N}-(\text{III}) \) is in the form of \( \text{NH}_3^+ \)). In the case of an organic contaminant instead of \( \text{NH}_3 \) the model results mainly differ at a later stage of the particle evaporation phase when the \( \text{N}: \text{S} \) approaches \( \sim 0.5 \). This is because the evaporation rate does not slow down before all S(VI) is lost when the particles do not contain any base (see Fig. S9). Thus, the modelled GMD shrinkage becomes somewhat faster when assuming organic contamination. Without any particle-phase contamination (pure sulfuric acid parti-
chicles) the particles evaporate faster and completely (see Supplement, Fig. S10).

Instead of explicitly calculating the H$_2$SO$_4$ activity with the thermodynamic model we derive it directly from the tabulated values of the H$_2$SO$_4$ chemical potentials as a function of the molality, following Giauque et al. (1960), Eq. (15). With this method we simulate the evaporation of H$_2$SO$_4$ without explicitly calculating the concentration of H$_2$SO$_4$ in the particles. However, since the tabulated chemical potentials from Giauque et al. (1960) are only valid for pure sulfuric acid solutions and temperatures close to 298.15 K, it cannot be used if the particle aqueous phase contains ammonium or other stabilising molecules.

Based on data from Giauque et al. (1960), Eq. (15) and the pure-liquid saturation vapour pressure parameterisation, Eq. (11) (N–K–L parameterisation), the modelled GMD shrinkage is consistent with the observations for experiments 1 and 2 when we consider the Case 1 (H$_2$SO$_4$ as the only evaporating S(VI) species) and particle-phase contamination due to non-volatile non-water-soluble organics (see Supplement, Fig. S11 and Table S1, simulations 5, 12, 19 and 24). However, when we use the pure-liquid saturation vapour pressure parameterisation from the Aspen Plus Databank, the modelled particles evaporate earlier (at higher RH) than the observed particles. The reason is that the ASPEN compared to N–K–L parameterisation gives higher saturation vapour pressures (see Supplement, Fig. S5).

### 4.4 Geometric mean diameter shrinkage influenced by relative humidity and temperature

In an attempt to constrain how $K_{H_2SO_4}$ and $K_{SO_3}$ depend on the temperature, and the role of H$_2$SO$_4$ and SO$_3$ on the observed particle diameter shrinkage, as a next step we simulate experiment 3, which expands in temperature. For this experiment the temperature increases gradually from 268 to 293 K, while the absolute humidity remains at a constant value, thus allowing the RH to decrease. Equation (21) describes the modelled temperature dependence of $K_{H_2SO_4}$ and $K_{SO_3}$, where the $K_i$ values at $T = 288.8$ K ($K_{i,288.8}$K) set equal to the values in regard to the model simulations of experiments 1 and 2 (Sect. 4.3):

$$K_i = K_{i,288.8} \cdot e^{\left(\frac{\Delta H_i}{T} - \frac{\Delta S_i}{T} \right)}$$

where $i$ can be either H$_2$SO$_4$ or SO$_3$. With $B_i = 0$ K there is no temperature dependence of $K_i$.

For other acids like HNO$_3$, HCl and HSO$_4^-$, $K_i$ decreases with increasing $T$ ($B_i > 0$) (Jacobson, 2005). Que et al. (2011) estimate $B_{H_2SO_4}$ to be 3475 K and $B_{SO_3}$ to be 14245.7 K. Thus, based on this information we would expect the equilibrium Reactions (R1) and (R3) to shift towards the left (more H$_2$SO$_4$(aq) and SO$_3$ as temperature increases). This would result in a stronger temperature dependence of the H$_2$SO$_4$(aq) and SO$_3$ saturation vapour pressures over aqueous sulfuric acid droplets (Eq. 13) compared to the temperature dependence expected if we only consider the temperature effect of the pure-liquid saturation vapour pressures (Fig. S5).

Figure 5 compares the measured and modelled GMD evolution during experiment 3. For the simulations we use either the same temperature dependence as suggested by Que et al. (2011) ($B_{H_2SO_4} = 3475$ K and $B_{SO_3} = 14245.7$ K) or no temperature dependence of $K_{H_2SO_4}$ and $K_{SO_3}$ ($B_{H_2SO_4} = 0$ K and $B_{SO_3} = 0$ K) or weak temperature dependence $B_{H_2SO_4} = 0$ K and $B_{SO_3} = -3000$ K. One of these model simulations corresponds to Case 1 and the rest to Case 2a (see Supplement, Table S1, simulation 28 and 29, 33, 34 and 36, respectively).

For the Case 1 simulation (see Supplement, Table S1, simulation 28) we use Eq. (15) and the tabulated H$_2$SO$_4$ chemical potentials from Giauque et al. (1960) to derive the H$_2$SO$_4$ activity. The particle-phase contaminant is assumed to be non-volatile and non-water-soluble organics. In this simulation the modelled particles grow somewhat too much before they start to shrink. For the Case 2a simulation, where the temperature dependences of $K_{H_2SO_4}$ and $K_{SO_3}$ are described by the $B_{H_2SO_4}$ and $B_{SO_3}$ values derived by Que et al. (2011) (see Supplement, Table S1, simulation 29), the model cannot capture the observed GMD evolution. For the Case 2a simulations with $B_{H_2SO_4} = 0$ K and $B_{SO_3} = 0$ K (see Supplement, Table S1, simulations 33 and 34) the particle-phase contaminant is assumed to be NH$_3$ or non-volatile and non-water-soluble organics. These model simulations, which agree with the observed GMD, indicate that the temperature dependences of $K_{H_2SO_4}$ and $K_{SO_3}$ are important for the GMD evolution during experiment 3.
perature dependences of $K_{H_2SO_4}$ and $K_{SO_3}$ need to be very weak or insignificant ($B_{H_2SO_4} = 0 \text{ K}$ and $B_{SO_3} = 0 \text{ K}$). If the particles are contaminated with NH$_3$, B$_{SO_3}$ or B$_{H_2SO_4}$ even needs to be negative for optimum fitting (e.g. $B_{H_2SO_4} = 0 \text{ K}$ and $B_{SO_3} = -3000 \text{ K}$; see Supplement, Table S1, simulations 36). It is also possible to find good agreement between the modelled and measured GMD evolution if one of $B_{H_2SO_4}$ and $B_{SO_3}$ is negative and the other one is positive ($B_{H_2SO_4} = 3475 \text{ K}$ and $B_{SO_3} = -10000 \text{ K}$; see Supplement, Table S1, simulation 31). The H$_2$SO$_4$ and SO$_3$ pure-liquid saturation vapour pressures in these simulations are calculated with Eqs. (11) and (12).

If we instead use the pure-liquid saturation vapour pressure parameterisations from the Aspen Plus Databank (which have somewhat weaker temperature dependences than Eqs. 11 and 12), the model results captures the observed GMD evolution if both $B_{H_2SO_4}$ and $B_{SO_3}$ are zero and H$_2$SO$_4$ is the only evaporating (SVI) species (Case 1; see Supplement, Table S1, simulation 50) or the main evaporating (SVI) species (Case 2a; see Supplement, Table S1, simulation 51; see Supplement, Fig. S12).

For Case 2b and 3 simulations in which we assume that SO$_3$ is responsible for most of the SVI evaporation, the model can never capture the observed GMD evolution. This is the case regardless of the pure-liquid saturation vapour pressure method we use (N–K–L–Nickless or Aspen Plus Databank; see Supplement, Table S1, simulations 42, 48, 52 and 53).

Based on the simulations of experiment 3 we conclude that most of the SVI that evaporated from the particles probably was in the form of H$_2$SO$_4$ (cases 1 and 2a). The very weak temperature dependences for $K_{H_2SO_4}$ and $K_{SO_3}$ needed for the model to capture the GMD evolution during experiment 3 is surprising and calls for further investigation. Part of the explanation to this could be that the AIOMFAC activity coefficient model is developed based on experimental data derived at 298.15 K. The uncertainty arising from the two different pure-liquid saturation vapour pressure parameterisations (temperature-dependent) also limits our ability to fully constrain the $K_{H_2SO_4}$ and $K_{SO_3}$ values. Based on our experiments and model simulations the equilibrium constant $K_{H_2SO_4}$ should be somewhere in the range 2.0–4.0 $\times$ $10^9$ mol kg$^{-1}$ and the $K_{SO_3}$ needs to be larger than 1.4 $\times$ $10^{10}$ at a temperature of 288.8 $\pm$ 5 K. The type of contamination of the sulfate particles (NH$_3$, DMA or a non-volatile non-water-soluble organic compound) does not have a substantial impact on our results and conclusions.

4.5 Atmospheric implications

In the following section, we define an effective saturation concentration of H$_2$SO$_4$($g$) ($c_{H_2SO_4}^*$) as the sum of the saturation concentration of H$_2$SO$_4$ ($c_{H_2SO_4}^*$) and SO$_3$ ($c_{SO_3}^*$), based on the assumption of rapid conversion of SO$_3$(g) to H$_2$SO$_4$(g), Eq. (22) (see Supplement S5, Fig. S7).

\[
c_{H_2SO_4}^* = c_{H_2SO_4}^* + c_{SO_3}^*
\]

Figure 6 shows the modelled effective H$_2$SO$_4$ saturation concentration ($c_{H_2SO_4}^*$) as a function of particle size ($d_p = 1–10^3$ nm) and RH (0–100 %). The results are from a model simulation with $K_{H_2SO_4} = 2.40 \times 10^9$ mol kg$^{-1}$ and $K_{SO_3} = 1.43 \times 10^{10}$. The pure-liquid saturation vapour pressures of H$_2$SO$_4$ and SO$_3$ are calculated with Eqs. (11) and (12).

The observed atmospheric daytime range of the [H$_2$SO$_4(g)$] is approximately $10^5–10^8$ molecules cm$^{-3}$, and we shade this range in Fig. 6. When $c_{H_2SO_4}^*$ is less than this range (to the upper right in the panel), the particles for most atmospheric daytime conditions will grow by condensation of H$_2$SO$_4$; when $c_{H_2SO_4}^*$ is greater than

\[
\text{H}_2\text{SO}_4(g), \text{Eq. (22) (see Supplement S5, Fig. S7).}
\]

\[
c_{H_2SO_4}^* = c_{H_2SO_4}^* + c_{SO_3}^*
\]
this (to the lower left in the panel) the particles will for most conditions shrink by evaporation of S(VI); in the shaded range the particles will tend to equilibrate. The larger the mole fraction of bases (NH₃) in the aerosol particles the less prone they will be to shrink. When particles are composed only of S(VI) and H₂O (N:S = 0) and the concentration of H₂SO₄(g) is 10⁷ molecules cm⁻³ all particles smaller than 10 nm will shrink at RH < 13.2 %. For the same [H₂SO₄(g)] and N: S = 0.5 all particles smaller than 10 nm shrink at RH < 12.1 %. However, for N:S = 0.75 particles smaller than 4 nm shrink at RH < 5.5 %, and if N:S = 1 only particles smaller than ~1.9 nm shrink, independent of RH except when it is extremely dry (RH ≤ 1.5 %). With the vapour pressure parameterisations from the Aspen Plus Databank and K_{H₂SO₄} = 4.00 × 10⁹ and \(^{x}K_{SO₃} = 4.55 \times 10^{10}\) the results are almost identical.

These model results demonstrate that sulfuric acid can evaporate from particles or be unable to contribute to their growth for atmospherically relevant conditions, characterised by low relative humidity, relatively high temperatures and weak sources of NH₃ and SO₂. Such environments can be found in the stratosphere and possibly also in the troposphere over large desert regions.

5 Summary and conclusions

This study demonstrates, both experimentally and theoretically, the importance of H₂SO₄ evaporation from aerosol particles at atmospheric relevant conditions. We measured the sulfate aerosol particle shrinkage below a certain low relative humidity (e.g. RH = 1.5 % for \(T = 288.8 \text{ K}\) and RH = 0.7 % for \(T = 268.0 \text{ K}\)) in the CLOUD chamber at CERN. We modelled the sulfur evaporation with ADCHAM. Our model simulation showed the following:

i. The dissociation of H₂SO₄(aq) is not complete, and evaporation of H₂SO₄ and H₂O can explain the observed particle shrinkage. However, we cannot dismiss the possibility that some of the shrinkage is due to evaporating SO₃, which is formed when H₂SO₄(aq) is dehydrated.

ii. The equilibrium rate coefficient for the first dissociation stage of H₂SO₄(aq) (\(K_{H₂SO₄}\)) falls somewhere in the range 2.0–4.0 × 10⁷ mol kg⁻¹ at 288.8 ± 5 K.

iii. The equilibrium coefficient for the dehydration of H₂SO₄ (\(^{x}K_{SO₃}\)) must at least be larger than 1.4 × 10¹⁰.

The main factors limiting our estimation of \(K_{H₂SO₄}\) are uncertainties in the pure-liquid saturation vapour pressure of H₂SO₄ and the relative contribution of SO₃ to the observed particle evaporation. Other potential sources of error are the uncertainties in the derived activity coefficients, the mass accommodation coefficient of H₂SO₄ and solid salt formation during the particle evaporation phase. The model simulations of an experiment where the temperature was gradually increased from 268 to 293 K indicate that the temperature dependencies of \(K_{H₂SO₄}\) and \(^{x}K_{SO₃}\) need to be weak. Future studies should focus on constraining the pure-liquid saturation vapour pressures of H₂SO₄ and SO₃ and the temperature dependence of \(K_{H₂SO₄}\) and \(^{x}K_{SO₃}\).

In order to be able to make an accurate prediction of the sulfate particles’ influence on global climate, their thermodynamic properties need to be properly described in global climate models. Thus, our constraints on the dissociation, \(K_{H₂SO₄}\) and dehydration, \(^{x}K_{SO₃}\) of H₂SO₄ are important contributions to the global aerosol–climate model community. The outcome of this study implies that atmospheric modelling studies, especially those dedicated to new-particle formation, should not by default assume that sulfate particles are non-volatile. Models that exclude the evaporation process provide faster particle formation rates which has a misleading effect on the impact of aerosols on climate.

Our results are especially meaningful for high-altitude new-particle formation (e.g. in the upper troposphere and stratosphere). It has been previously reported that the particle formation (Brock et al., 1995) and the ion-induced nucleation (Lee et al., 2003; English et al., 2011) are sources of new particles in high altitudes. In the upper troposphere and stratosphere general circulation models coupled with aerosol dynamics models use aerosol evaporation as a source of \([H₂SO₄(g)]\) (English et al., 2011). The concentration of H₂SO₄(g) drastically affects new-particle formation rates. The equilibrium constants for the dissociation and dehydration of H₂SO₄ reported in this study are needed to accurately model the sulfate aerosol particle evaporation and concentration of H₂SO₄(g). They may also be important to evaluate particle formation schemes (homogeneous, ion-induced) for stratospheric conditions. These schemes are generally constrained based on tropospheric conditions (English et al., 2011) but applied for stratosphere simulations. Moreover, vapour-phase H₂SO₄ in the atmosphere appears to be ubiquitous, even in the absence of photochemistry (Mauldin et al., 2003; Wang et al., 2013); this may partly be due to evaporation of H₂SO₄ from aerosol particles.

In a changing climate it will become even more important to understand the thermodynamic properties of the sulfur aerosol particles involved in the development of polar stratospheric clouds and how sulfate aerosols influence the stratospheric O₃ layer. Experiments simulating stratospheric conditions (\(T \approx 200–265 \text{ K}, p \approx 10^{-1}–10^{-3} \text{ atm}, RH \geq 1.0 \%\) and \([H₂SO₄] \leq 10^{8} \text{molec. cm}^{-3}\)) are of great importance. Our results may also assist in explaining the atmospheric sulfur cycle of Venus. The Venusian clouds that are made up largely of sulfuric acid droplets cover an extended temperature range from 260 K (upper clouds) to 310 K (middle clouds) and even higher (lower clouds). The scientific understanding of the upper tropospheric and stratospheric sulfate aerosol is of great importance for the global climate and requires further investigation.
Data availability. Requests for underlying material should be addressed to the corresponding author, Georgios Tsagkogeorgas (george.tsagkogeorgas@tropos.de).

The Supplement related to this article is available online at https://doi.org/10.5194/acp-17-8923-2017-supplement.

Author contributions. GT and JD designed and performed the experiments. GT, JD and PR analysed the data. PR developed the model code. PR and GT performed the simulations. GT, JD, LR, JT, JGS, and AK collected the data and contributed to the analysis. GT, PR, JD, and NMD assisted in drafting the manuscript. GT, PR, JD, MB, JC, RCF, MK, NMD and FS contributed to scientific interpretation and editing of the manuscript. All authors contributed to the development of the CLOUD facility and analysis instruments and commented on the manuscript.

Competing interests. The authors declare that they have no conflict of interest.

Acknowledgements. We would like to thank CERN for supporting CLOUD with important technical and financial resources, and for providing a particle beam from the CERN Proton Synchrotron. We also thank Patrick Carrie, Louis-Philippe De Menezes, Jonathan Dumollard, Roberto Guida, Katja Ivanova, Francisco Josa, Ilia Krasin, Robert Kristic, Abdulmajid Laassiri, Osman Maksumov, Serge Mathot, Benjamin Marichy, Herve Martinati, Antti Onnela, Robert Sitals, Hansueli Walther, Albin Wasem and Mats Wilhelmsson for their important contributions to the experiment. This research has received funding from the EC Seventh Framework Programme (Marie Curie Initial Training Network “CLOUD-ITN” no. 215072 and “CLOUD-TRAIN” no. 316662, ERC-Starting “MOCAPAF” grant no. 57360 and ERC-Advanced “ATMNUCLE” grant no. 227463), the German Federal Ministry of Education and Research (project nos. 01LK0902A and 01LK1222A), the Swiss National Science Foundation (project nos. 200020 135307 and 206620 141278), the Academy of Finland (Centre of Excellence project no. 1118615 and other projects: 135054, 133872, 251427, 139656, 139995, 137749, 141217, 141451), the Finnish Funding Agency for Technology and Innovation, the Vaisala Foundation, the Nestling Foundation, the Austrian Science Fund (FWF; project no. J3198-N21), the Portuguese Foundation for Science and Technology (project no. CERN/FP/116387/2010), the Swedish Research Council, Vetenskapsradet (grant 2011-5120), the President of the Russian Academy of Sciences and Russian Foundation for Basic Research (grants 08-02-91006-CERN and 12-02-91522-CERN), the US National Science Foundation (grants AGS1136479, AGS1447056, AGC1439551 and CHE1012293), the PEGASOS project funded by the European Commission under the Seventh Framework Programme (FP7-ENV-2010-265148), and the Davdow Foundation. We thank the toTools team for providing tools for mass spectrometry analysis.

Pontus Roldin would like to thank the Cryosphere-Atmosphere Interactions in a Changing Arctic Climate (CRAICC) Nordic Top-Level Research Initiative and the Swedish Research Council for Environment, Agricultural Sciences and Spatial Planning FORMAS (project no. 214-2014-1445) for financial support.

Edited by: Yafang Cheng
Reviewed by: two anonymous referees

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