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Relations between the aromaticity and magnetic dipole transitions in the electronic spectra of hetero[8]circulenes

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Abstract

Magnetically induced current densities have been calculated at the second-order Møller-Plesset perturbation theory (MP2) level for seven hetero[8]circulenes and their dicationic and dianionic forms. Calculations of the magnetic dipole transition moments have also been carried out at the algebraic diagrammatic construction (ADC(2)) and the second-order approximate coupled-cluster (CC2) levels. The calculations show that the degree of aromaticity and the size of the magnetic dipole transition moment of the lowest magnetic-dipole allowed excited state are related. We show that neutral hetero[8]circulenes are weakly antiaromatic when the first excited state with a large magnetic dipole transition moment of 10-16 a.u. lies at high energies (~2.8-3.5 eV). For the dications, this transition often lies at much lower energies. Hetero[8]circulene dications with large magnetic dipole transition moments are strongly antiaromatic. The lowest excited states of the hetero[8]circulene dianions have very small magnetic dipole transition moments implying that they are aromatic.

Graphical abstract

1. INTRODUCTION

The hetero[8]circulenes constitute a group of macroheterocyclic compounds that are characterized by unique spectral properties because of their peculiar electronic structure [1-3]. They can be used in nanophotonic applications [4], in photodynamic therapy [5], as the active media in the fabrication of organic light-emitting diodes (OLEDs) [6-8], and in organic field-effect transistors (OFETs) [9-11]. The generic molecular structure of the studied hetero[8]circulenes are shown in Figure 1. The molecular structure consists of an inner 8π -electron eight-membered ring called the “hub” and of the $24/20/16\pi$ -electron outer perimeter called the “rim”. The aromatic character of the hetero[8]circulenes based on structural and magnetic ring-current criteria has been thoroughly investigated in our previous works [12-15], which showed that neutral hetero[8]circulenes do not sustain any net ring-current and can therefore be considered nonaromatic. Even though hetero[8]circulenes sustain strong currents, the net ring-current strength vanishes, because the magnetically induced ring current in the *rim* is diatropic and the ring current in the *hub* is of the same strength but flows in the opposite *e.g.*, in the paratropic direction [12-15].

Figure 1. The molecular structure of the studied hetero[8]circulenes can be grouped into the three classes based on the aromatic properties of the neutral molecule and doubly charged ions. For the SiH-containing compound, the single-double bond alternation differs from the other studied molecules as shown in the left part.

Radenkovic *et. al.* [16] draw similar conclusions for a series of benzoannulated tetraoxa[8]circulenes based on calculations using the continuous transformation of origin of current density diamagnetic zero (CTOCD-DZ) method [17]. The obtained ring current maps showed that there are two weakly interacting current flows, namely a diatropic ring current around the rim and a paratropic ring current around the inner hub of the cyclooctatetraene core [16]. The results do not support the so-called “annulene within an annulene” model that predicts paratropic ring currents in both the rim (24π) and the hub (8π). Another computational study that suggested competing diatropic and paratropic ring currents in the rim and the hub for a number of selected tetraoxa[8]circulenes was reported by Kleinpeter *et. al.* [18]. Their conclusions were based on through space NMR shielding (TSNMRS) calculations, which were visualized using iso-chemical-shielding-surfaces (ICSS) [19]. Nucleus-independent chemical shifts (NICS) calculations [20] for the individual rings of the tetraoxa[8]circulene molecule and related isoelectronic hetero[8]circulenes are also able to identify the

inner COT ring as an antiaromatic moiety, whereas the five- and six-membered rings was shown to have aromatic character [1, 3, 21, 22]. However, NICS calculations cannot be used for estimating the balance between the global paratropic and diatropic magnetically-induced ring currents of the rim and the hub, whereas current density calculations using the gauge-including magnetically induced currents (GIMIC) and CTOCD-DZ methods yield explicit information about the current density flow of the molecules.

The doubly charged hetero[8]circulenes have interesting aromatic properties [13-15]. It has been shown that the dications of tetrathia[8]circulene (**I**), tetraoxa[8]circulene (**II**) and tetraphospha[8]circulene (**III**) are strongly antiaromatic, whereas their dianions are aromatic [12-15]. The calculated degree of aromaticity of strongly antiaromatic molecules depends to some extent on the employed computational level. B3LYP calculations tend to overestimate the antiaromatic character of strongly antiaromatic molecules. It is therefore necessary to study the current densities using *ab initio* correlated levels of theory such as second-order Møller-Plesset perturbation theory (MP2) level or alternatively to employ a functional with a large fraction of Hartree-Fock exchange [23-25].

The reason for the strong antiaromaticity of porphyrinoids like carbaporphyrins, carbathiaporphyrins, isophlorins and expanded porphyrins has been shown to be due to a low-lying excited state that has a large magnetic dipole transition moment from the ground state [23-25]. The paratropic ring current of strongly antiaromatic porphyrinoids can result in closed-shell paramagnetic molecules [23]. Thus, antiaromatic hetero[8]circulenes sustaining strong paratropic ring currents might also be paramagnetic. In this work, we study at correlated *ab initio* levels of theory the molecular aromaticity and ground-state transition properties of the lowest excited states of selected neutral and doubly charged hetero[8]circulenes.

2. INVESTIGATED MOLECULES

Three groups of hetero[8]circulenes with the different aromatic character have been studied. The first group consists of tetraoxa[8]circulene (**I**), tetrathia[8]circulene (**II**) and tetraphospha[8]circulene (**III**), which have similar aromatic properties. Their neutral form is weakly antiaromatic, the dications are strongly antiaromatic and the dianions are aromatic [13-15]. Tetraaza[8]circulene (**IV**) and tetraarsena[8]circulene (**V**) are the second group. The neutral form is weakly antiaromatic, the dication is nonaromatic or very weakly antiaromatic, and the dianion is aromatic [13-15]. The hetero[8]circulenes species belonging to the groups 1 and 2 have 8π electrons in the hub and 24π electrons in the rim. The third group consists of tetramethylenephénylene (**VI**), which has 8π electrons in the hub and 16π electrons in the rim, and tetrasilala[8]circulene (**VII**) with 8π electrons in the hub and 20π electrons in the rim. The neutral **VI** and **VII** are weakly antiaromatic, whereas the dication and

the dianion are aromatic [13-15]. The molecular structures of the studied hetero[8]circulenes are shown in Figures 2.

Figure 2. The molecular structure of the studied hetero[8]circulenes optimized at the B3LYP/def2-TZVP level. **I** – tetrathia[8]circulene, **II** – tetraoxa[8]circulene, **III** – tetraphospha[8]circulene, **IV** – tetraaza[8]circulene, **V** – tetraarsena[8]circulene, **VI** – tetramethylenephénylene and **VII** – tetrasil[8]circulene.

3. COMPUTATIONAL METHODS

The ground-state molecular structure of the neutral **I-VII** as well as of the doubly charged cations and anions of **I-VII** were optimized at the density functional theory (DFT) [26] level using the B3LYP functional [27,28] and the def2-TZVP basis set [29]. The vertical excitation energies (VEE) and the electronic magnetic-dipole transition moments (*m*) were calculated at the algebraic diagrammatic construction model through second order (ADC(2)) [30,31]. Approximate second-order coupled-cluster calculations (CC2) [32] were used for assessing the accuracy of the ADC(2) results for the strongly antiaromatic dications of **I-III**. We calculated the VEEs and transition moments at the *ab initio* correlated levels, because time-dependent density functional theory (TDDFT) calculations often yield inaccurate excitation energies for multi-charged species. The calculations were performed with the Turbomole program version 7.2 [33,34]. The multiconfiguration character of the **VII** molecule was investigated by performing extended multi-configuration quasi-degenerate perturbation theory (XMC-QDPT2) [35]. The XMC-QDPT2 calculations were performed using the firefly software [36]. The excitation energies of the first singlet and triplet states were calculated at the XMC-QDPT2 level for

the **VII** molecule, which has a low-lying excited singlet state with an excitation energy of 0.21 eV at the ADC(2) level. The active space of the complete active space self-consistent field (CASSCF) calculations needed for the XMC-QDPT2 study consisted of 10 electrons in 10 orbitals. State averaging was performed for the four lowest states. The effective Hamiltonian contained 35 states.

Magnetically induced current densities (current strengths) were calculated using GIMIC software [37-41] at the second-order Møller–Plesset perturbation theory (MP2) level [42]. GIMIC uses basis-set information and density matrices that are obtained when calculating nuclear magnetic resonance (NMR) shielding constants [37-41]. The NMR shielding calculations were performed at the MP2 level using Turbomole 7.2 [30, 33, 34]. Ring-current strengths (I in nA/T) and current strengths passing selected chemical bonds were obtained by integrating the current density that flows through planes intersecting the chemical bonds [38, 41]. The integrated ring-current strengths can be used as an aromaticity index, since the ring-current (susceptibility) strength for benzene is 11.8 nA/T and for the antiaromatic cyclobutadiene it is -19.8 nA/T. Nonaromatic molecules have very small net ring-current strengths [37]. The aromatic pathways of the multiring molecules such as hetero[8]circulenes and porphyrinoids can be determined by calculating the current strengths that pass selected chemical bonds [12-15, 25, 37].

4. RESULTS AND DISCUSSIONS

4.1. Current strengths

Ring-current strength calculations at the B3LYP level lead to an overestimation of the paratropic current density contribution of strongly antiaromatic porphyrinoids, whereas MP2 calculations yielded more accurate magnetically induced current density (MIC) strengths [23-25]. Thus, *ab initio* correlated calculations at least at the MP2 level are needed in order to obtain reliable MIC strengths for strongly antiaromatic hetero[8]circulenes.

MIC strengths calculated at the MP2 level of theory are almost the same as those previously obtained in DFT calculations using the B3LYP functional for most of the studied hetero[8]circulenes. The discrepancies between the MIC strengths calculated at the MP2 and DFT levels are generally less than 0.5 nA/T. The exceptions are the dications of **(I-III)**²⁺ and the neutral form of **VII**. The current-density strengths and current pathways of the hetero[8]circulenes are therefore investigated at the MP2 level in this work. The molecular structures and current pathways are shown in Figure 3. The current density of the rest of the hetero[8]circulenes has been discussed in detail in previous studies [13-15].

The net ring-current strength of the antiaromatic **I**²⁺, **II**²⁺, **III**²⁺, **VII**⁰ species calculated at the MP2 level are -46, -66, -51 and -13.2 nA/T, respectively, which can be compared with the corresponding net ring-current strength of -55, -84, -66 and -22.4 nA/T calculated at the B3LYP level [14]. The differences in the current strengths obtained at the two levels of theory are in the range of 9-

18 nA/T. Larger discrepancies were obtained for the very strongly antiaromatic molecules. The calculations show that the two levels of theory yield roughly the same current pathways, whereas the current strengths of the individual bonds calculated at the MP2 level are weaker than the B3LYP currents in about the same proportion as between the net ring-current strengths. The strengths of the current pathways are shown in Figure 3. The main current pathways and the degree of molecular aromaticity are qualitatively the same at the two computational levels.

Figure 3. Current density pathways and MIC strengths (in nA/T) calculated for the $\mathbf{I}^{2+}$, $\mathbf{II}^{2+}$, $\mathbf{III}^{2+}$, $\mathbf{VII}^0$ species at the MP2 level (top) and the B3LYP (bottom).

4.2. Excitation energies and electronic magnetic-dipole transition moments

4.2.1. Molecules I, II and III

The vertical excitation energies (VEE) and magnetic dipole transition moments ($\mathbf{m}$) of the electronic transitions calculated at the ADC(2) and CC2 levels for the molecules **I-III** are summarized in Table 1. The data in Table 1 show that similar VEEs are obtained at the two levels of theory with discrepancies of less than 0.2 eV. Almost the same $\mathbf{m}$ values are also obtained in the ADC(2) and CC2 calculations. The lowest or the second-lowest excited state of the dication of **I-III** at 0.44-0.65 eV has a strong magnetic dipole allowed transition from the ground state with an $\mathbf{m}$ value of 7-15 a.u. The excitation energy of the corresponding strongly magnetic dipole allowed transition, with $\mathbf{m}$ values of 10-14 a.u. for the neutral molecules, is in the range of 3.12-3.67 eV. The dianions of **I-III** have no strong magnetic dipole allowed transitions among the eight lowest excited states. For the anions, the $\mathbf{m}$ values are in the range of 0.0-0.4 a.u. The paratropic contribution to the ring-current strength that is responsible for the molecular antiaromaticity can be estimated using perturbation theory as [38,43,44]:

$$I_{paratropic} \sim \sum_i \langle \psi(S_i) | \hat{L} | \psi(S_0) \rangle \frac{1}{E(S_i) - E(S_0)} I_{paratropic} \sim \sum_i \frac{\langle \psi(S_i) | \hat{L} | \psi(S_0) \rangle}{E(S_i) - E(S_0)}, \quad (1)$$

where $\langle \psi(S_i) | \hat{L} | \psi(S_0) \rangle$ is the matrix element of the angular momentum operator for the transition between the i -th singlet excited state (S_i) and the electronic ground state (S_0).

$E(S_i) - E(S_0)$ is the vertical ground-state excitation energy to the S_i state [24]. For the studied closed-shell molecules, the following expression holds:

$$\langle \psi(S_i) | \hat{\mu} | \psi(S_0) \rangle = \langle \psi(S_i) | \hat{L} | \psi(S_0) \rangle \quad (2),$$

where $\hat{\mu}$ is the magnetic-dipole operator. Eq. (1) and Eq. (2) show that there is a relation between electronic magnetic dipole transition moments and antiaromatic properties of molecules [43,44]. The small excitation energies of 0.44-0.65 eV for **I**²⁺, **II**²⁺, and **III**²⁺ combined with the large m values of 7-15 a.u. lead to a dominating paratropic ring-current strength and the obtained antiaromatic character of the molecules. For neutral **I-III**, the electronic transition still possesses a large m value (Table 1). However, the states are much higher in energy implying that their contribution to the paratropic ring current is smaller than for the dications. The neutral molecules are practically nonaromatic sustaining very weak paratropic ring currents of a few nA/T. The dications (**I**²⁺, **II**²⁺, **III**²⁺) have several low-lying magnetic-dipole allowed excited states that contribute to the paratropic ring current.

Table 1. Vertical excitation energies (VEE in eV) and the corresponding magnetic dipole transition moments in parenthesis (a.u.) calculated at the ADC(2) and CC2 levels for the neutral and doubly charged **I-III** species. The VEEs and transition moments of the states with large magnetic dipole transition moments are highlighted. The MIC strengths (in nA/T) calculated at the MP2 level are also reported.

Molecule		Neutral		Dication		Dianion	
I	transition	CC2	ADC(2)	CC2	ADC(2)	CC2	ADC(2)
	$S_0 \rightarrow S_1$	3.46(13.8)	3.48(12.9)	0.44(0.0)	0.38(0.00)	2.33(0.0)	2.44(0.00)
	$S_0 \rightarrow S_2$	3.64(0.0)	3.67(0.00)	0.65(10.7)	0.53(7.90)	2.33(0.0)	2.44(0.00)
	$S_0 \rightarrow S_3$	3.64(0.0)	3.67(0.00)	0.98(0.0)	0.65(1.10)	2.81(0.0)	3.04(0.00)
	$S_0 \rightarrow S_4$	3.75(0.0)	3.72(0.00)	2.14(0.0)	1.87(2.22)	3.33(0.0)	3.26(0.00)
	$S_0 \rightarrow S_5$	4.54(0.0)	4.63(0.00)	2.17(0.0)	2.13(0.00)	3.34(0.0)	3.28(0.00)
	$S_0 \rightarrow S_6$	4.95(0.0)	5.04(0.00)	2.73(0.40)	2.65(0.00)	3.40(0.0)	3.28(0.00)
	$S_0 \rightarrow S_7$	4.95(0.0)	5.35(0.00)	2.82(0.8)	2.75(0.60)	3.34(0.0)	3.28(0.00)
	$S_0 \rightarrow S_8$	5.31(0.0)	5.35(0.00)	3.02(9.0)	2.96(7.80)	3.55(0.2)	3.65(0.14)
	I (nA/T) MP2	-2.5		-46.1		22.1	
II	transition	Neutral		Dication		Dianion	
	$S_0 \rightarrow S_1$	3.43(0.0)	3.41(0.0)	0.53(15.0)	0.48(14.6)	1.85(0.0)	1.83(0.0)

	$S_0 \rightarrow S_2$	3.43(0.0)	3.43(0.0)	0.60(0.0)	0.51(0.00)	1.95(0.1)	1.92(0.1)
	$S_0 \rightarrow S_3$	3.43(0.0)	3.43(0.0)	0.60(0.0)	0.53(0.00)	1.95(0.1)	1.92(0.1)
	$S_0 \rightarrow S_4$	3.57(14.4)	3.67(13.4)	2.14(0.0)	2.04(0.00)	2.10(0.0)	2.15(0.0)
	$S_0 \rightarrow S_5$	4.43(0.0)	4.53(0.0)	2.18(0.0)	2.15(0.00)	2.46(0.2)	2.51(0.2)
	$S_0 \rightarrow S_6$	4.48(0.0)	4.55(0.00)	2.33(0.00)	2.37(0.00)	2.46(0.2)	2.51(0.2)
	$S_0 \rightarrow S_7$	4.78(0.0)	4.55(0.00)	2.55(0.3)	2.49(0.2)	1.85(0.0)	1.87(0.0)
	$S_0 \rightarrow S_8$	4.88(0.0)	4.90(0.0)	3.09(10.2)	3.10(10.4)	1.95(0.1)	2.05(0.2)
	I (nA/T) MP2	-0.03		-66.0		20.6	
III		Neutral		Dication		Dianion	
		CC2	ADC(2)	CC2	ADC(2)	CC2	ADC(2)
	$S_0 \rightarrow S_1$	3.12(10.5)	3.14(11.4)	0.22(0.2)	0.33(0.1)	1.08(0.0)	1.15(0.00)
	$S_0 \rightarrow S_2$	3.48(0.3)	3.49(0.12)	0.44(8.0)	0.45(7.00)	1.65(0.4)	1.7(0.3)
	$S_0 \rightarrow S_3$	3.48(0.3)	3.49(0.12)	1.1(0.0)	1.1(0.00)	1.65(0.4)	1.7(0.3)
	$S_0 \rightarrow S_4$	3.64(0.0)	3.65(0.0)	1.57(0.0)	1.62(0.00)	1.98(0.0)	1.92(0.0)
	$S_0 \rightarrow S_5$	4.0(0.0)	4.05(0.0)	1.78(0.0)	1.85(0.00)	2.26(0.15)	2.21(0.15)
	$S_0 \rightarrow S_6$	4.26(0.3)	4.27(0.2)	1.97(0.2)	2.07(0.20)	2.26(0.15)	2.21(0.15)
	$S_0 \rightarrow S_7$	4.26(0.3)	4.27(0.2)	2.12(0.0)	2.22(0.00)	2.64(0.1)	2.59(0.1)
	$S_0 \rightarrow S_8$	4.28(0.0)	4.29(0.0)	2.55(0.13)	2.65(0.13)	2.72(0.2)	2.60(0.1)
	I (nA/T) MP2	-3.7		-50.8		17.9	

4.2.2. Molecules IV and V

The lowest VEEs and $\mathbf{m}$ values calculated for the neutral and doubly charged **IV** and **V** species at the ADC(2) level are summarized in the Table 2. For neutral **IV** and **V**, we obtained excited states with large $\mathbf{m}$ values at 3.50 eV and 2.88 eV, respectively. These transitions provide significant contributions to the paratropic part of the ring current. Due to the large excitation energy, the neutral **V** hetero[8]circulene is only weakly antiaromatic and **IV** with the even larger excitation energy is nonaromatic. For the **IV**²⁺ and **V**²⁺ dications, these transitions appear at lower energies of 1.11 and 1.42 eV. However, they have though smaller $\mathbf{m}$ values than for neutral **IV** and **V** (Table 2) leading to a somewhat stronger paratropic ring current of -4.5 nA/T and -8.0 nA/T for **IV**²⁺ and **V**²⁺, respectively. The **IV**²⁻ and **V**²⁻ dianions do not have any excited states with a large $\mathbf{m}$ values among the eight lowest excited states. They are therefore aromatic sustaining net diatropic ring currents of 21.7 nA/T and 15.4 nA/T for **IV**²⁻ and **V**²⁻, respectively.

Table 2. Vertical excitation energies (VEE in eV) and the corresponding magnetic dipole transition moments in parenthesis (a.u.) for the neutral and doubly charged **IV** and **V** species. The VEEs and transition moments of the states with large magnetic dipole transition moments are highlighted. The MIC strengths (in nA/T) calculated at the MP2 level are also reported.

molecule	Transition	Neutral	Dication	Dianion
		ADC(2)	ADC(2)	ADC(2)
IV	$S_0 \rightarrow S_1$	2.95(0.00)	0.51(0.00)	2.01(0.01)
	$S_0 \rightarrow S_2$	3.35(0.00)	0.51(0.00)	2.04(0.00)
	$S_0 \rightarrow S_3$	3.35(0.00)	1.11(1.0)	2.04(0.00)

	$S_0 \rightarrow S_4$	3.50(15.8)	1.41(0.00)	2.07(0.00)
	$S_0 \rightarrow S_5$	4.62(0.00)	2.43(0.00)	2.38(0.00)
	$S_0 \rightarrow S_6$	4.70(0.00)	3.18(0.00)	2.38(0.00)
	$S_0 \rightarrow S_7$	4.92(0.00)	3.18(0.00)	2.69(0.00)
	$S_0 \rightarrow S_8$	5.04(0.00)	3.43(0.00)	2.79(0.02)
	I (nA/T) MP2	-0.7	-4.5	21.7
molecule		Neutral	Dication	Dianion
V	Transition	ADC(2)	ADC(2)	ADC(2)
	$S_0 \rightarrow S_1$	2.88(10.1)	0.29(0.0)	1.19(0.0)
	$S_0 \rightarrow S_2$	3.43(0.10)	0.29(0.0)	1.70(0.0)
	$S_0 \rightarrow S_3$	3.43(0.1)	0.63(0.2)	1.79(0.3)
	$S_0 \rightarrow S_4$	3.50(0.0)	1.40(0.2)	1.79(0.3)
	$S_0 \rightarrow S_5$	4.09(0.0)	1.42(8.0)	2.04(0.1)
	$S_0 \rightarrow S_6$	4.18(0.0)	1.50 (0.2)	2.04(0.1)
	$S_0 \rightarrow S_7$	4.29(0.2)	1.62(0.2)	2.44(0.1)
	$S_0 \rightarrow S_8$	4.29(0.2)	1.70(0.0)	2.65(0.01)
	I (nA/T) MP2	-4.0	-8.0	15.4

4.2.3. Molecules VI and VII

The lowest ADC(2) excitation energies and magnetic dipole transition moments of the neutral and doubly charged **VI** and **VII** species are summarized in the Table 3. The lowest excited state of neutral **VI** and **VII** have large m values. The m value of the lowest excited state of **VI** at 3.57 eV is 12.7 a.u. leading to a weakly antiaromatic molecule, whereas neutral **VII** is more antiaromatic, because the excitation energy of the first excited state is 0.21 eV and it has a relatively large m value of 6.2 a.u. The dications and dianions of **VI** and **VII** are aromatic sustaining diatropic ring currents of 4.0-21.9 nA/T.

Table 3. Vertical excitation energies (VEE in eV) and the corresponding magnetic dipole electronic transition moments in the parenthesis (a.u.) for compounds **VI** and **VII**. VEEs and transition moments for the states with large or significant magnetic dipole transition moments are highlighted. The total MIC strengths (in nA/T) are also reported.

molecule		Neutral	Dication	Dianion
VI	Transition	ADC(2)	ADC(2)	ADC(2)
	$S_0 \rightarrow S_1$	3.57(12.7)	0.40(0.00)	1.28(0.00)
	$S_0 \rightarrow S_2$	3.99(0.00)	0.42(0.00)	1.88(0.00)
	$S_0 \rightarrow S_3$	3.99(0.00)	0.62(0.00)	1.88(0.00)
	$S_0 \rightarrow S_4$	4.11(0.00)	1.63(0.2)	2.20(0.00)
	$S_0 \rightarrow S_5$	4.90(0.00)	2.40(0.33)	2.29(0.04)
	$S_0 \rightarrow S_6$	5.02(0.00)	2.57(0.10)	2.29(0.04)
	$S_0 \rightarrow S_7$	5.02(0.00)	2.65(0.00)	2.40(0.00)
	$S_0 \rightarrow S_8$	5.56(9.30)	3.41(0.00)	2.77(0.00)

	I (nA/T) MP2	-2	105	21.9
VII		Neutral	Dication	Dianion
	transition	ADC(2)	ADC(2)	ADC(2)
	$S_0 \rightarrow S_1$	0.21(6.2)	1.61(0.01)	0.58(0.0)
	$S_0 \rightarrow S_2$	0.80(0.04)	1.61(0.01)	0.74(0.0)
	$S_0 \rightarrow S_3$	1.23(0.13)	1.68(0.001)	0.92(0.0)
	$S_0 \rightarrow S_4$	1.43(0.1)	2.27(0.1)	1.82(0.3)
	$S_0 \rightarrow S_5$	2.20(0.2)	2.27(0.1)	1.85(0.0)
	$S_0 \rightarrow S_6$	2.40(0.10)	2.74(1.00)	2.04(0.1)
	$S_0 \rightarrow S_7$	2.40(0.10)	2.74(1.00)	2.25(0.01)
	$S_0 \rightarrow S_8$	2.47(1.40)	2.88(0.0)	2.52(0.2)
	I (nA/T) MP2	-13.2	10.5	4.0

4.3. The molecular orbital analysis

The molecular structures of the neutral **I** and **IV** are planar belong to the D_{4h} point group (see Figure 2). The molecular structures of **II**, **III**, **V** and **VI** have a lower symmetry than **I** and **VI**. They are saddle shaped belonging to the D_{2d} point group. The molecular structure of **VII** is also saddle shaped belonging to the less symmetric C_2 point group. The dications and dianions of compounds **I-VII** are nonsymmetric belonging to the C_1 point group. However, since they have approximately the same symmetry as the corresponding neutral molecule, the electronic transitions of the doubly charged species can be labeled in the same way as use for the neutral molecules. The energy diagram of the occupied frontier orbitals (HOMO- n , $n = 0, 1, \dots$) and the unoccupied orbitals (LUMO+ n , $n = 0, 1, \dots$) that play a significant role in the electronic transitions of the eight lowest excited states of the neutral hetero[8]circulenes **I-VII** are shown in Figures 4-6. The calculations show the eight lowest excited states are reached by ground-state transitions dominated by $\pi\pi^*$ character.

4.3.1. Molecules I-III

The transition from HOMO (b_{2u}) to LUMO (b_{1u}) of **I** dominates the ground-state transition to the A_{2g} state, which is lowest excited state of neutral **I**. The HOMO to LUMO transition has a weight of 0.98 leading to a large $\mathbf{m}$ value. For $\mathbf{I}^{2+}$, the strong electronic magnetic dipole transition is the S_0 - S_2 transition that occurs from the orbital corresponding to HOMO-3 (b_{1u}) of **I** to the one corresponding to HOMO (b_{2u}) of **I**. Here, the frontier orbitals refer to the ones for the neutral molecules. The excitation energies and the transition moments are given in Table 1. The orbital transitions of the neutral molecules are illustrated with red arrows in the orbital energy diagram in Figure 4. The energy gap between HOMO-3 and HOMO of $\mathbf{I}^{2+}$ is much smaller than the energy gap between HOMO and LUMO of **I** explaining why the excited state of $\mathbf{I}^{2+}$ with the large $\mathbf{m}$ value lies much lower in energy than the one for **I**. For $\mathbf{I}^{2-}$, the highest occupied orbital corresponds to LUMO (b_{1u}) of **I**. The excitation with a

large **m** value occurs from the highest occupied orbital of **I**²⁻ to a higher-lying LUMO of b_{2u} symmetry. The energy gap between the orbitals is large implying that the first excited state with a large **m** value is not found among the first eight electronic transitions. However, the electronic transitions with large **m** values are from the orbitals corresponding to LUMO (b_{2u}) to LUMO+4, LUMO+5 (e_u) of neutral **I** as indicated by the green arrow in Figure 4.

For **II** and **III**, the strong magnetic dipole transition from the A₁ ground state to the first excited A₂ state is dominated by the transition from HOMO-2 (a₂) to LUMO (a₁) and from HOMO (a₂) to LUMO (a₁) with weights of 0.97 and 0.90, respectively. For **II**²⁺, the strong magnetic transition occurs from the orbital corresponding to HOMO-3 (a₁) to HOMO-2 (a₂) of **II**. In the case of **II**²⁺, the first electronic transition does not occur from the orbital corresponding to the HOMO of the neutral molecule **II**, because the electronic structure optimization of **II**²⁺ affects the relative order of the orbitals. The HOMO (e) of neutral **II** becomes HOMO-1 of the **II**²⁺ dication.

For **III**²⁺, the strong magnetic transition occurs from the orbital corresponding to HOMO-3 (a₁) to HOMO (a₂) of **III**. For **II**²⁻ and **III**²⁻, the LUMO (a₁) of the neutral molecules is the highest occupied orbital and the lowest a₂ orbital lies high up in energy implying that no states of the dianions with a large **m** value appear among the eight lowest excited states. For **II**²⁻ and **III**²⁻, there are electronic transitions with small **m** values from the orbitals corresponding to LUMO (a₁) to LUMO+1, LUMO+2 (e) of **II** and from the orbitals corresponding to LUMO (a₁) to LUMO+3, LUMO+4 (e) of **III**, respectively.

Figure 4. The energy diagram for the frontier molecular orbitals of **I-III**. The strong magnetic dipole transitions of the practically nonaromatic neutral molecules are shown in red and the corresponding orbital transitions of the strongly antiaromatic dianions are shown in blue. Transitions of the dianions with significant magnetic dipole transition moments are shown in green.

4.3.2. Molecules IV and V

For **IV**, the strong magnetic transition to the S_4 state of A_{2g} symmetry is completely dominated by the transition from HOMO-2 (b_{2u}) to LUMO (b_{1u}) with a weight of 0.99. The magnetic transition to the A_{2g} state of **IV**²⁺ dominates by a transition from the orbital corresponding to HOMO-3 (b_{2u}) of **IV** to the orbital corresponding to LUMO (b_{1u}) of **IV**. For **IV**²⁻, the weak magnetic transition of the A_{2g} state involves electronic transition from LUMO (b_{1u}) to LUMO+3 (b_{2u}) of **IV**. The orbital transitions of **IV** and **IV**²⁺ are illustrated with red, blue and green arrows in the orbital energy diagram in Figure 5.

For **V**, the strong magnetic transition to the A_2 state is dominated by a transition from HOMO (a_2) to LUMO (a_1) with a weight of 0.9. For **V**²⁺, the magnetic transition occurs from HOMO-4 (a_1) to HOMO (a_2) of **V**. **V**²⁻ is aromatic, because the lowest unoccupied a_2 orbital lies high in energy relatively to the highest occupied a_1 orbital and there are only electronic transitions with weak m from LUMO (a_1) to LUMO+2 and LUMO+3 (e). The orbital transitions are illustrated in Figure 5.

Figure 5. The energy diagram for the frontier molecular orbitals of neutral **IV** and **V**. The strong magnetic dipole transitions of the nonaromatic or weakly antiaromatic neutral molecules are shown in red and the corresponding orbital transitions of the antiaromatic dianions are shown in blue. Transitions of the dianions with significant magnetic dipole transition moments are shown in green.

4.3.3. Molecules VI and VII

For **VI**, the strong magnetic transition to the excited state of A_2 symmetry corresponds to a transition from HOMO (a_1) to LUMO (a_2) with a weight of 0.9. For **VI**²⁺, the lowest transition with non-vanishing but small magnetic moment ($S_0 \rightarrow S_4$) involves a transition from HOMO-4 (a_2) to HOMO (a_1) of **VI**. **VI**²⁻ has no strong magnetic transition among the eight lowest excited states, because it involves a transition from LUMO (a_2) of **VI** to a high-lying a_1 orbital.

For **VII**, the most important transition of the strong magnetic moments to the A state is HOMO (b) to LUMO (b) with a weight of 0.8. For **VII**²⁺, the S₀-S₆ and S₀-S₇ transitions are the lowest transitions with significant but small *m* values. They correspond to a transition from HOMO-3 (a) to LUMO (b) of **VII**. For **VII**²⁻, the first eight transitions do not have any large *m* values. The orbital transitions are illustrated in Figure 6.

The smallest singlet excitation energy of 0.21 eV was calculated at the ADC(2) level for the neutral molecule **VII**. The multiconfiguration character of the ground state wave function was therefore investigated by performing XMC-QDPT2 calculations, which yielded an excitation energy of 0.17 eV for the lowest triplet state and an excitation energy of 0.39 eV the first singlet state. The weight of the dominating configuration of the ground singlet state is 0.80 indicating that the ground state has some multiconfigurational character, whereas the reasonable agreement between the excitation energies calculated at the XMC-QDPT2 and ADC(2) levels as well as the small D₁ diagnostic value of 0.09 suggest that the single-reference methods are appropriate for investigating the aromatic and spectroscopic properties of **VII**, which seems to be the most problematic molecule among the studied species judged from the small optical gap.

Figure 6. The energy diagram for the frontier molecular orbitals of neutral **VI** and **VII**. The strong magnetic dipole transitions of the nonaromatic or weakly antiaromatic neutral molecules are shown in red and the corresponding orbital transitions of the aromatic diacations are shown in blue. Transitions of the dianions with significant magnetic dipole transition moments are shown in green.

5. SUMMARY AND CONCLUSIONS

Relations between the aromatic character and spectroscopic properties of the seven hetero[8]circulenes and their double charged ions have been investigated at correlated *ab initio* levels of theory. The calculations showed that the strongly antiaromatic hetero[8]circulene species have a low-lying excited state with a large magnetic dipole transition moment (*m* value). The low-lying excited

state with a large m value contributes significantly to the paratropic part of the magnetically induced ring-current strength. When the excited state with a large m value lies higher in energy (~ 2.8 - 3.5 eV) the molecule is weakly antiaromatic due to the large denominator in the perturbation theory expression in Eq. (1). When the hetero[8]circulene has no excited state below 3.5 eV with a large m value, it is aromatic. Thus, hetero[8]circulenes that have a low-lying excited state with a large magnetic dipole transition moment can be expected to be strongly antiaromatic. This rule may hold more generally, because similar results have previously been obtained for carbaporphyrins and isophlorins [24]. Current density calculations at the MP2 and B3LYP levels lead to the almost same current strengths for weakly antiaromatic and aromatic hetero[8]circulenes, whereas the paratropic ring-current strength of strongly antiaromatic hetero[8]circulenes are overestimated at the B3LYP level.

CONFLICTS OF INTEREST

There are no conflicts to declare.

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