Observation of Long-Range, Near-Side Angular Correlations in Proton-Proton Collisions at the LHC

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Observation of long-range, near-side angular correlations in proton-proton collisions at the LHC

The CMS collaboration

ABSTRACT: Results on two-particle angular correlations for charged particles emitted in proton-proton collisions at center-of-mass energies of 0.9, 2.36, and 7 TeV are presented, using data collected with the CMS detector over a broad range of pseudorapidity (\(\eta\)) and azimuthal angle (\(\phi\)). Short-range correlations in \(\Delta \eta\), which are studied in minimum bias events, are characterized using a simple “independent cluster” parametrization in order to quantify their strength (cluster size) and their extent in \(\eta\) (cluster decay width). Long-range azimuthal correlations are studied differentially as a function of charged particle multiplicity and particle transverse momentum using a 980 nb\(^{-1}\) data set at 7 TeV. In high multiplicity events, a pronounced structure emerges in the two-dimensional correlation function for particle pairs with intermediate \(p_T\) of 1–3 GeV/c, \(2.0 < |\Delta \eta| < 4.8\) and \(\Delta \phi \approx 0\). This is the first observation of such a long-range, near-side feature in two-particle correlation functions in \(pp\) or \(p\bar{p}\) collisions.

KEYWORDS: Hadron-Hadron Scattering
1 Introduction

This paper presents measurements of two-particle angular correlations of charged particles emitted in proton-proton ($pp$) collisions at center of mass energies ($\sqrt{s}$) of 0.9, 2.36, and 7 TeV. This first study of short- and long-range correlations in $pp$ collisions at the LHC high energy frontier provides important information for characterizing Quantum Chromodynamics (QCD) in this energy regime, especially the mechanism of hadronization and possible collective effects due to the high particle densities reached in these collisions. Multiparticle correlations in high energy collisions have been measured previously for a broad range of collision energies and colliding systems with the goal of understanding the underlying mechanism of particle production [1–7].

Two related studies of angular correlations have been performed using two-dimensional $\Delta \eta$-$\Delta \phi$ correlation functions. Here $\Delta \eta$ is the difference in pseudorapidity $\eta (=-\ln(\tan(\theta/2)))$, where $\theta$ is the polar angle relative to the beam axis) between the two particles and $\Delta \phi$ is the difference in their azimuthal angle $\phi$ (in radians). In a first analysis, $pp$ data collected with a minimum bias trigger at 0.9, 2.36, and 7 TeV were used to study short-range correlations ($|\Delta \eta|$ less than $\approx 2$). In a second study, the long-range structure ($2.0 < |\Delta \eta| < 4.8$) of two-particle correlation functions was examined as a function of charged particle multiplicity and particle transverse momentum for a large data set at 7 TeV.
In short-range correlations in minimum bias events, a peak with a typical width of about one unit in $\Delta \eta$ is observed. A useful way to quantify this effect is to assume that the initial interactions emit so-called “independent clusters”, which subsequently decay isotropically in their own rest frame into the observed hadrons [1–3, 5–7]. This simple independent cluster model (ICM) parametrization of the observed correlation function allows a quantitative comparison of data and models for different collision energies and collision systems. The observed correlation strength and extent in relative pseudorapidity between the particles are parametrized by a Gaussian distribution. The fitted parameters in this ansatz are the cluster multiplicity or ”size” (the average number of particles into which a cluster decays) and the decay ”width” (the spread of the daughter particles in pseudorapidity). This ansatz is only a phenomenological parametrization which provides no insight as to the nature of the assumed clusters nor to the mechanisms by which clusters are formed. Relating these results to the underlying QCD dynamics requires further modeling.

To investigate long-range azimuthal correlations ($2.0 < |\Delta \eta| < 4.8$), a high-statistics data set of high multiplicity $pp$ events at 7 TeV was used. In current $pp$ Monte Carlo (MC) event generators, the typical sources of such long-range correlations are momentum conservation and away-side ($\Delta \phi \approx \pi$) jet correlations. Measurements at the Relativistic Heavy Ion Collider (RHIC) have revealed that the long-range structure of two-particle angular correlation functions is significantly modified by the presence of the hot and dense matter formed in relativistic heavy ion collisions [7]. Several novel correlation structures over large $\Delta \eta$ were observed in azimuthal correlations for intermediate particle transverse momenta, $p_T \approx 1 – 5$ GeV/c [8, 9]. Since the particle densities produced in the highest multiplicity $pp$ collisions at LHC energies begin to approach those in high energy collisions of relatively small nuclei such as copper [10], it is natural to search for the possible emergence of new features in the two-particle correlation function from high multiplicity $pp$ events [11–18]. Therefore, the azimuthal ($\Delta \phi$) correlation functions from the large data set at 7 TeV have been studied differentially by binning the events in the observed charged particle multiplicity and by selecting particle pairs in bins of the transverse momentum of the particles.

The paper is organized as follows: the experimental setup, event triggering, and event selection for both analyses are described in section 2. Criteria used to select tracks are listed in section 3. The general procedure for calculating the correlation functions and the CMS-specific efficiency corrections are described in sections 4 and 5, respectively. Results for the analysis of short-range correlations in minimum bias data using the cluster parametrization are given in section 6. The study of long-range correlations as a function of event multiplicity and particle transverse momentum is detailed in section 7.

## 2 Experimental setup, triggering, and event selections

This analysis used three data sets collected with $pp$ interactions at $\sqrt{s} = 0.9$, 2.36, and 7 TeV. A detailed description of the CMS experiment can be found in ref. [19]. The detector subsystems used for the present analysis are the pixel and silicon-strip tracker (SST), covering the region $|\eta| < 2.5$ and immersed in a 3.8 T axial magnetic field. The lead
tungstate crystal electromagnetic calorimeter (ECAL), the brass/scintillator hadron calorimeter (HCAL), and the forward calorimeter (HF, covering the region $2.9 < |\eta| < 5.2$), were also used for online and offline event selections. The detailed MC simulation of the CMS detector response is based on geant4 [20].

Any hit in the beam scintillator counters (BSC, $3.23 < |\eta| < 4.65$) coinciding with colliding proton bunches was used for triggering the data acquisition in the minimum bias trigger. To preferentially select non-single-diffractive (NSD) events, a coincidence of at least one HF calorimeter tower with more than 3 GeV of total energy on each of the positive and negative sides was required. Events were also required to contain at least one reconstructed primary vertex (PV) that fell within a 4.5 cm of the nominal collision point along the beam axis and within a radius of 0.15 cm measured perpendicular to the beam relative to the average vertex position, and to contain at least three fully reconstructed tracks associated with the primary vertex. Outside this relatively narrow vertex range, the density of events was too small to ensure enough statistics for constructing the random background distribution (section 4) in small bins of the longitudinal ($z$) vertex position. Beam-halo and other beam-background events were rejected as described in ref. [21]. The contamination of background events after selections in the colliding-bunch data sample was found to be negligible ($< 0.1\%$).

After all selections are applied, the total number of events used for the minimum bias analysis of cluster properties described in section 6 is 168 854 (3.3 $\mu$b$^{-1}$) for 0.9 TeV, 10 902 (0.2 $\mu$b$^{-1}$) for 2.36 TeV, and 150 086 (3.0 $\mu$b$^{-1}$) for 7 TeV, where the numbers in parentheses are the approximate integrated luminosity for the individual data samples. The systematic uncertainties in the results shown in section 6 significantly exceed the statistical uncertainties for the 150k event minimum bias data sample at 7 TeV, so no further events were included in this analysis.

In order to investigate the properties of the high multiplicity $pp$ collisions, a dedicated high multiplicity trigger was designed and implemented in the two levels of the CMS trigger system. At Level 1 (L1), the total transverse energy summed over the entire set of CMS calorimeters (ECAL, HCAL, and HF) was required to be greater than 60 GeV. At the high-level trigger (HLT), online tracks built from the three layers of pixel detectors with a track origin within a cylindrical region of 21 cm along the beam and 0.5 cm in the transverse radius were used in an online vertexing algorithm. The number of pixel tracks ($N_{\text{online\,track}}$) with $|\eta| < 2$, $p_T > 0.4$ GeV/$c$, and a distance of closest approach of 0.12 cm or less to the best vertex (the one associated with the highest number of tracks) was determined for each event. Data were taken with a threshold initially set to $N_{\text{online\,track}} > 70$. During later, higher-luminosity running, the lower limit was raised to 85.

The total integrated luminosity for the high multiplicity analysis was 980 $\mu$b$^{-1}$. The total number of events in each of the bins of offline reconstructed track multiplicity, $N_{\text{offline\,track}}$, used in the analysis are listed in table 1. To take advantage of the full acceptance of the CMS tracking system, $N_{\text{offline\,track}}$ includes tracks within $|\eta| < 2.4$ (see section 3 for other offline track selection criteria). The table also lists the average values of $N_{\text{track}}$, the event multiplicity corrected for all detector and algorithm inefficiencies, as described in section 5.
<table>
<thead>
<tr>
<th>Multiplicity bin ($N_{\text{offline}}^{\text{trk}}$)</th>
<th>Event Count</th>
<th>$\langle N_{\text{offline}}^{\text{trk}} \rangle$</th>
<th>$\langle N_{\text{corrected}}^{\text{trk}} \rangle$</th>
</tr>
</thead>
<tbody>
<tr>
<td>MinBias</td>
<td>21.43M</td>
<td>15.9</td>
<td>17.8</td>
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<td>$N_{\text{offline}}^{\text{trk}} &lt; 35$</td>
<td>19.36M</td>
<td>13.0</td>
<td>14.1</td>
</tr>
<tr>
<td>$35 \leq N_{\text{offline}}^{\text{trk}} &lt; 90$</td>
<td>2.02M</td>
<td>45.3</td>
<td>53.1</td>
</tr>
<tr>
<td>$90 \leq N_{\text{offline}}^{\text{trk}} &lt; 110$</td>
<td>302.5k</td>
<td>96.6</td>
<td>111.7</td>
</tr>
<tr>
<td>$N_{\text{offline}}^{\text{trk}} \geq 110$</td>
<td>354.0k</td>
<td>117.8</td>
<td>136.1</td>
</tr>
</tbody>
</table>

Table 1. Number of events for each multiplicity bin used in the 7 TeV analysis with total integrated luminosity of 980 nb$^{-1}$. The multiplicity of offline reconstructed tracks, $N_{\text{offline}}^{\text{trk}}$, was counted within the kinematic cuts of $|\eta| < 2.4$ and $p_T > 0.4$ GeV/c. The last two columns list the average values of $N_{\text{offline}}^{\text{trk}}$ as well as the average of $N_{\text{corrected}}^{\text{trk}}$, the event multiplicity corrected for all detector and algorithm inefficiencies.

3 Track selection

In this analysis, the so-called CMS highPurity [22] tracks were used. Additionally, a reconstructed track was considered as a primary-track candidate if the significance of the separation along the beam axis, $z$, between the track and the primary vertex, $d_z/\sigma(d_z)$, and the significance of the impact parameter relative to the primary vertex transverse to the beam, $d_{xy}/\sigma(d_{xy})$, were each less than 3. In order to remove tracks with potentially poorly reconstructed momentum values, the relative uncertainty of the momentum measurement, $\sigma(p_T)/p_T$, was required to be less than 10%.

To ensure reasonable tracking efficiency and low fake rate, only tracks within $|\eta| < 2.4$ and above a minimum $p_T$ value were used. For the inclusive analysis, the selected range was 0.1 GeV/c < $p_T$ < 5.0 GeV/c. The effect of the upper limit imposed on $p_T$ is negligible. The effects of the lower $p_T$ cut, as well as the effect of the $\eta$ restriction on the determination of cluster parameters from $\Delta \eta$ correlations, are significant and will be discussed in more detail below. To avoid possible bias in the high multiplicity analysis, the lower cutoff was raised to $p_T > 0.4$ GeV/c when classifying the event multiplicity in order to match the cut applied in the online tracking.

4 Calculation of the two-particle correlation function

For both minimum bias and high-multiplicity triggered collision events, the first step in extracting the correlation function was to divide the sample into bins in track multiplicity. For the minimum bias sample, 10 bins were used, each containing about the same number of events. Following an approach similar to that in refs. [3, 6], the $p_T$-inclusive charged two-particle correlation as a function of $\Delta \eta$ and $\Delta \phi$ is defined as follows:

$$R(\Delta \eta, \Delta \phi) = \left\langle \left( \langle N \rangle - 1 \right) \left( \frac{S_N(\Delta \eta, \Delta \phi)}{B_N(\Delta \eta, \Delta \phi)} - 1 \right) \right\rangle_{\text{bins}}$$

(4.1)

where $S_N$ and $B_N$ are the signal and random background distributions, defined in eqs. (4.2) and (4.3) respectively, $\Delta \eta(= \eta_1 - \eta_2)$ and $\Delta \phi(= \phi_1 - \phi_2)$ are the differences in pseudorapidity and azimuthal angle between the two particles, $\langle N \rangle$ is the number of tracks per
event averaged over the multiplicity bin, and the final $R(\Delta \eta, \Delta \phi)$ is found by averaging over multiplicity bins. For simplicity in eq. (4.1) and the discussion in this section, $N$ is used to represent the total number of offline reconstructed tracks per event. Note that the order in which the particles are considered has no significance. The quantities $\Delta \eta$ and $\Delta \phi$ are always taken to be positive and used to fill one quadrant of the $\Delta \eta, \Delta \phi$ histograms with the other three quadrants filled by reflection. Therefore, the resulting distributions are symmetric about $(\Delta \eta, \Delta \phi) = (0,0)$ by construction.

For each multiplicity bin, the signal distribution:

$$S_N(\Delta \eta, \Delta \phi) = \frac{1}{N(N-1)} \frac{d^2N_{\text{signal}}}{d\Delta \eta d\Delta \phi} \ (4.2)$$

was determined by counting all particle pairs within each event, using the weighting factor $N(N-1)$, then averaging over all events. This represents the charged two-particle pair density function normalized to unit integral. The background distribution:

$$B_N(\Delta \eta, \Delta \phi) = \frac{1}{N^2} \frac{d^2N_{\text{mixed}}}{d\Delta \eta d\Delta \phi} \ (4.3)$$

denotes the distribution of uncorrelated particle pairs representing a product of two single-particle distributions, also normalized to unit integral. This distribution was constructed by randomly selecting two different events within the same multiplicity bin and pairing every particle from one event with every particle in the other (in this case, the normalization factor $1/N^2$ corresponds to $1/N_1N_2$ event-by-event). The pairs of events used to compute the background were also required to be within the same 0.5 cm wide bin in the vertex location along the beam.

As indicated in eq. (4.1), the ratio of $S_N(\Delta \eta, \Delta \phi)$ to $B_N(\Delta \eta, \Delta \phi)$ was first calculated in each multiplicity bin. Dividing the background in this way corrects for detector effects such as tracking inefficiencies, non-uniform acceptance, etc. The ratio of signal to background was then weighted by the track multiplicity factor, $\langle N \rangle - 1$ (where $\langle N \rangle$ is the average multiplicity in each bin), and averaged over all the multiplicity bins to arrive at the final two-particle correlation function $R(\Delta \eta, \Delta \phi)$.

### 5 Corrections for tracking and event selection inefficiencies

#### 5.1 Correction for tracking inefficiency

Studies with simulated events showed that the combined geometrical acceptance and reconstruction efficiency for the global track reconstruction exceeds 50% around $p_T \approx 0.1$ GeV/c over the full CMS tracker acceptance ($|\eta| < 2.4$) for charged hadrons. The efficiency is greater than 90% in the $|\eta| < 1$ region for $p_T > 0.6$ GeV/c. Detailed studies of tracking efficiencies using MC-based and data-based methods can be found in [23]. The tracking efficiency correction factor, $\epsilon_{\text{trk}}$, was determined by taking the ratio of the number of reconstructed tracks ($N_{\text{trk}}$) to that of generator level primary charged particles ($N_{\text{gen}}$) in the simulated MC events as a function of $p_T$, $\eta$, $z_{\text{vtx}}$:

$$\epsilon_{\text{trk}}(\eta, p_T, z_{\text{vtx}}) = \frac{N_{\text{trk}}(\eta, p_T, z_{\text{vtx}})}{N_{\text{gen}}(\eta, p_T, z_{\text{vtx}})} \ (5.1)$$
In constructing the signal and background distributions, this correction was applied as an inverse weight, \(1/\epsilon_{\text{trk}}(\eta, p_T, z_{\text{vtx}})\), to each particle. After this correction, the two-particle correlation function found using reconstructed tracks from simulated events matched that obtained at the generator level to within 1.4%.

Using simulations, the tracking efficiency was found to have little or no dependence on multiplicity within the range studied in the present work. The fake rate did increase slightly with multiplicity but remained at the 1-2% level. Therefore, the corrections applied for tracking efficiency and fake rate were independent of event multiplicity.

5.2 Event selection correction for minimum bias data

For the minimum bias data, inefficiencies in triggering and vertex reconstruction of low multiplicity events resulted in multiplicity distributions of reconstructed tracks which were biased toward higher average values. The correction factor for this effect, \(\epsilon_{\text{evt}}\), was determined by taking the ratio of two generator-level MC multiplicity distributions, one with offline event selection applied \((N_{\text{evtSel}}^\text{gen})\) and one for all NSD MC events \((N_{\text{NSD}}^\text{gen})\). In eq. (5.2), \(N_{\text{true}}\) represents the true number of particles in the event. The NSD event selection efficiency:

\[
\epsilon_{\text{evt}}(N_{\text{true}}) = \frac{N_{\text{evtSel}}^\text{gen}(N_{\text{true}})}{N_{\text{NSD}}^\text{gen}(N_{\text{true}})}
\]  

(5.2)

is about 50% at \(N_{\text{true}}=6\) and reaches 100% around \(N_{\text{true}}=15\). When calculating the correlation function, each event was weighted by the inverse of the event selection efficiency evaluated at \(N_{\text{corrected}}\) which is the number of particles corrected for acceptance and tracking efficiency as described above, \(1/\epsilon_{\text{evt}}(N_{\text{corrected}})\).

5.3 Event selection correction for high multiplicity data

The two high-multiplicity trigger thresholds used in the HLT (see section 2) give different trigger efficiencies. Distributions for offline reconstructed track multiplicity, \(N_{\text{offline}}\), in minimum bias and high multiplicity triggered events at 7 TeV are shown in the top panels of figure 1. Kinematic cuts of \(|\eta| < 2.4\) and \(p_T > 0.4\) GeV/c were used in defining \(N_{\text{offline}}\) (see section 3 for other offline track selections). The statistics of events with \(N_{\text{offline}} \geq 110\) were enhanced by a factor of about 1000 with the high multiplicity trigger relative to the minimum bias trigger due the large prescale factor applied to the latter sample. The lower panels in figure 1 show the HLT efficiency, obtained from data, of the two high multiplicity triggers relative to the minimum bias trigger. The L1 triggering efficiency (not shown in figure 1) is not a concern since it reaches 100% efficiency for events with \(N_{\text{offline}} \geq 90\). A weight given by the inverse of the HLT efficiency, \(\epsilon_{\text{evt}}^{\text{HLT}}(N_{\text{offline}})\), was applied to all pairs from a given event.

6 Short-range correlations in 0.9, 2.36, and 7 TeV data

The final two-particle inclusive correlation functions are shown in figure 2 as a function of \(\Delta \eta\) and \(\Delta \phi\) at \(\sqrt{s} = 0.9, 2.36, \text{and} 7\) TeV. A small region with \(|\Delta \eta| < 0.06\) and \(|\Delta \phi| <\)
Figure 1. Distributions of the number of tracks reconstructed in offline analysis, \(N_{\text{offline}}\), for minimum bias events, as well as high-multiplicity triggered events, both at 7 TeV, with online multiplicity \(N_{\text{online}}\) greater than (a) 70 and (b) 85. The total integrated luminosity of the data set is \(980 \text{ nb}^{-1}\). The minimum bias trigger was heavily prescaled during higher luminosity LHC running. The HLT efficiency turn-on curves for the two high multiplicity triggers are shown in the two panels at the bottom.

Figure 2. Two-particle correlation functions versus \(\Delta \eta\) and \(\Delta \phi\) in pp collisions at \(\sqrt{s}\) = (a) 0.9, (b) 2.36, and (c) 7 TeV.

0.06 was excluded in both signal and background distributions in order to reject residual secondary effects (i.e., any tracks from photon conversions, weak decays, or \(\delta\)-electrons which were not rejected by the cut on the projected distance of the track from the vertex).

The complex two-dimensional (2-D) correlation structure shown in figure 2 is dominated by three prominent components: a narrow peak at \((\Delta \eta, \Delta \phi) \approx (0,0)\) which can be
understood as the contribution from higher $p_T$ clusters (e.g., hard processes like jets); a ridge at $\Delta \phi \approx \pi$ spread over a broad range in $\Delta \eta$, interpreted as due to away-side jets or more generally momentum conservation; and an approximately Gaussian ridge at $\Delta \eta \approx 0$ extending over the whole range of $\Delta \phi$, becoming broader toward larger $\Delta \phi$ values, which arises from the decay of clusters with lower $p_T$ (e.g., soft QCD string fragmentation). This broadening will be discussed in quantitative detail later in this section. The PHOBOS experiment at RHIC observed similar correlation structures in $pp$ collisions at $\sqrt{s} = 200$ GeV and 410 GeV \[6\]. Qualitatively similar structures also exist in PYTHIA (figure 3 for D6T tune \[24\]) although they do not reproduce the strength of the correlations seen in the data. The qualitative features of the observed correlations in the data are also consistent with an independent cluster approach according to a simulation study from the ISR experiment using a low-mass resonance ($\rho$, $\omega$, $\eta$) gas model \[3\] and a MC model of isotropic cluster decays from the PHOBOS experiment \[7\]. Bose-Einstein Correlations (BEC, also known as the Hanbury-Brown and Twiss effect \[25\]) have been measured in $pp$ collisions \[26–28\] but their influence on the extracted cluster parameters has been found to be negligible \[6\].

To quantify one aspect of the correlation structure, the 2-D correlation functions were reduced to one-dimensional (1-D) functions of $\Delta \eta$ by integrating $S_N(\Delta \eta, \Delta \phi)$ and $B_N(\Delta \eta, \Delta \phi)$ over $\Delta \phi$:

$$R(\Delta \eta) = \left( \langle N \rangle - 1 \right) \left( \frac{\int S_N(\Delta \eta, \Delta \phi) d\Delta \phi}{\int B_N(\Delta \eta, \Delta \phi) d\Delta \phi} - 1 \right) \right) \right)_{\text{bins}}.$$  \hspace{1cm} (6.1)

The 1-D two-particle pseudorapidity correlation functions, $R(\Delta \eta)$, where $\Delta \phi$ was averaged over the entire range from 0 to $\pi$, are shown for all three energies in figure 4.

In the context of an ICM description, $R(\Delta \eta)$ can be parametrized using the functional form \[2\]:

$$R(\Delta \eta) = \alpha \left[ \frac{\Gamma(\Delta \eta)}{B(\Delta \eta)} - 1 \right]$$  \hspace{1cm} (6.2)

where the correlation strength $\alpha = \frac{(K(K-1))}{(K)}$ depends on the average numbers of particles into which a cluster decays, the cluster size $K$. The function $\Gamma(\Delta \eta)$ is a Gaussian function proportional to

$$\exp \left[ -\frac{(\Delta \eta)^2}{(4\delta^2)} \right]$$

---

**Figure 3.** Two-particle correlation functions versus $\Delta \eta$ and $\Delta \phi$ in PYTHIA D6T tune at $\sqrt{s}$ = (a) 0.9, (b) 2.36, and (c) 7 TeV.
where $\delta$ quantifies the average spread of particles originating from a single cluster, i.e. the decay width. The background distribution, $B(\Delta \eta)$, in eq. (6.2) is the same event-mixed distribution defined in eq. (4.3) but averaged over all the multiplicity bins with all corrections applied, and integrated over $\Delta \phi$.

Without knowing $\sigma_K$, the width of the distribution of $K$, it is impossible to calculate the average cluster size $\langle K \rangle$ directly from the measured value of $\alpha$. However, an effective cluster size can be defined using the extracted correlation strength via the relation:

$$K_{\text{eff}} = \alpha + 1 = \frac{\langle K(K-1) \rangle}{\langle K \rangle} + 1 = \langle K \rangle + \frac{\sigma_K^2}{\langle K \rangle}.$$  \hspace{1cm} (6.3)

The effective cluster size $K_{\text{eff}}$ and decay width $\delta$ can be estimated by means of a least $\chi^2$ fit of eq. (6.2) to the measured two-particle pseudorapidity correlation function. The ICM provides a good fit to the data over a large range in $\Delta \eta$, as shown in figure 4.

The statistical uncertainties of the fit parameters are much smaller than the systematic ones. The correction for event selection efficiency (see section 5.2) has an overall systematic uncertainty of less than 2.8% found by comparing the result at the generator level to that from the reconstructed tracks after corrections. The model dependence of this procedure (i.e. the selection efficiency for NSD events) was investigated by using correction factors derived from different MC generators such as PYTHIA, PHOJET \cite{29}, and HERWIG++ \cite{30}. The biggest discrepancy in the final results was about 2.6%.

Systematic uncertainties due to track quality cuts were examined by loosening the cuts on the significance of both the transverse track impact parameter, $d_{xy}/\sigma(d_{xy})$, and the distance along the beam to the primary vertex, $d_z/\sigma(d_z)$ from 3 to 5. The final results were found to be insensitive to these track selections to within 1.2%.

A summary of systematic uncertainties for the inclusive analysis is given in table 2. The uncertainties are presented for the cluster model fit parameters listed in table 2, namely the correlation strength ($\alpha = K_{\text{eff}} - 1$) and the width in pseudorapidity ($\delta$).


<table>
<thead>
<tr>
<th>Source</th>
<th>$K_{\text{eff}} - 1 (\alpha)$</th>
<th>$\delta$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Track quality cuts</td>
<td>1.2</td>
<td>1.0</td>
</tr>
<tr>
<td>Correction for tracking/acceptance efficiency and fake rate</td>
<td>1.3</td>
<td>1.4</td>
</tr>
<tr>
<td>Correction for event selection efficiency</td>
<td>2.6</td>
<td>2.8</td>
</tr>
<tr>
<td>Model dependence of the corrections</td>
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<td>1.3</td>
</tr>
<tr>
<td>Total systematic uncertainties</td>
<td>4.1</td>
<td>3.5</td>
</tr>
</tbody>
</table>

Table 2. Summary of systematic uncertainties in the inclusive analysis.

| $\sqrt{s}$ | $K_{\text{eff}}^{|\eta|<2.4}$ | $\delta^{|\eta|<2.4}$ |
|------------|-------------------------------|-----------------------|
| 0.9 TeV    | 2.12± < 0.01 (stat.) ± 0.05 (syst.) | 0.53± < 0.01 (stat.) ± 0.02 (syst.) |
| 2.36 TeV   | 2.23 ± 0.02 (stat.) ± 0.05 (syst.) | 0.52± < 0.01 (stat.) ± 0.02 (syst.) |
| 7 TeV      | 2.34± < 0.01 (stat.) ± 0.06 (syst.) | 0.51± < 0.01 (stat.) ± 0.02 (syst.) |

Table 3. Final results on $K_{\text{eff}}$ and $\delta$ measured within the kinematic cuts of $p_T > 0.1 \text{ GeV/c}$ and $|\eta| < 2.4$ at CMS.

| $\sqrt{s}$ | $K_{\text{eff}}^{|\eta|<3.0}$ | $\delta^{|\eta|<3.0}$ |
|------------|-------------------------------|-----------------------|
| 0.9 TeV    | 2.50± < 0.01 (stat.) ± 0.06 (syst.) | 0.64± < 0.01 (stat.) ± 0.02 (syst.) ± 0.03 |
| 2.36 TeV   | 2.65 ± 0.03 (stat.) ± 0.07 (syst.) | 0.60 ± 0.01 (stat.) ± 0.02 (syst.) ± 0.03 |
| 7 TeV      | 2.75± < 0.01 (stat.) ± 0.07 (syst.) | 0.59± < 0.01 (stat.) ± 0.02 (syst.) ± 0.03 |

Table 4. Final results on $K_{\text{eff}}$ and $\delta$ measured by CMS after extrapolation to $p_T > 0$ and $|\eta| < 3$. The third quoted uncertainty is due to the extrapolation procedure.

Values of effective cluster sizes and widths observed within the kinematic cuts on $p_T$ and $|\eta|$ are summarized in table 3.

As can be seen in figure 4, the most central point of the 1-D pseudorapidity correlation function always lies slightly above the fits. This could be due to the residual effects of secondary processes that were not fully removed by the track selection, as well as BEC or other physics processes at this small scale in $\Delta \eta$. All fits exclude this central point, but including it in the fit affects the values of $K_{\text{eff}}$ and $\delta$ by no more than 0.5%.

In figure 5, CMS measurements of $K_{\text{eff}}$ and $\delta$ for $p_T > 0.1 \text{ GeV/c}$ and $|\eta| < 2.4$ are shown as functions of $\sqrt{s}$, and compared with the PYTHIA D6T tune. An energy dependence of $K_{\text{eff}}$ is observed, while $\delta$ remains roughly constant over the three energies. PYTHIA shows energy dependencies of $K_{\text{eff}}$ and $\delta$ similar to those seen in the data, but the magnitude of $K_{\text{eff}}$ is significantly smaller in PYTHIA. The effect of tensor mesons in PYTHIA was investigated, but even using an unrealistically large probability of 50% for the angular momentum $L=1$ meson states accounted for only about one third of the difference. Results from the HERWIG++ model were also studied and found to have correlation function shapes dramatically different from the data, in agreement with previous results [31] showing that HERWIG++ is insufficiently tuned to reproduce soft QCD processes.
Figure 5. (a) $K_{\text{eff}}$ and (b) $\delta$ as a function of $\sqrt{s}$, measured for $p_T > 0.1 \text{GeV}/c$ and $|\eta| < 2.4$ by CMS in solid circles. Open circles show the PYTHIA results with the D6T tune.

In order to compare with measurements made at lower energies, CMS results were extrapolated to $|\eta| < 3$ and the full $p_T$ range $p_T > 0$ to achieve a consistent kinematic range. The fraction of tracks below $p_T \approx 0.1 \text{GeV}/c$ was estimated by fitting the measured $p_T$ distributions using the Tsallis function as was done in ref. [21], which empirically describes both the low $p_T$ exponential and the high $p_T$ power-law behaviors [32]. The integral of the fit function for $p_T < 0.1 \text{GeV}/c$ amounts to about 5.5% of the total yield, consistent with the results in ref. [21]. As first quantified in ref. [7], the loss of particles falling outside a limited $\eta$ acceptance results in a significant reduction of both $K_{\text{eff}}$ and $\delta$. This effect was investigated using several dynamical models as well as the simple ICM following the identical approach used in ref. [7]. As was the case in the previous analysis, the ratios of $K$ and $\delta$ for different $\eta$ acceptances ($|\eta| < 3.0$ and $|\eta| < 2.4$ in the present work) were found to scale very closely with $\delta^{|\eta|<2.4}$, the measured cluster width using data in the $|\eta| < 2.4$ region, reinforcing the conclusion that the dependence of the extracted cluster parameters on pseudorapidity acceptance is primarily a simple geometric effect.

Figure 6 shows the results of $K_{\text{eff}}$ and $\delta$ measured by the CMS experiment after the extrapolation to $|\eta| < 3$ and $p_T \approx 0$, as well as previous measurements at lower energies in the same pseudorapidity range [3, 5, 6]. Values of the extrapolated CMS results are sum-
Figure 6. (a) $K_{\text{eff}}$ and (b) $\delta$ as a function of $\sqrt{s}$ based on a model-dependent extrapolation of CMS data to $p_T \approx 0$ and $|\eta| < 3$ (solid circles), as well as data from PHOBOS [6] (solid squares), UA5 [5] (solid triangles) and ISR [3] (solid stars) experiments for pp and p$\bar{p}$ collisions. Open circles and squares show the PYTHIA results for the D6T tune and default parameters, respectively.

The observed cluster size cannot be fully explained by a resonance decay model even at very low energies, since the expectation of $\langle K \rangle$ from resonance decays is about 1.5 (extrapolating to 1.7 for $K_{\text{eff}}$ depending on the assumed cluster size distribution [5]). This is significantly lower than the observed values, but is close to what is seen in PYTHIA. Additional sources of pseudorapidity correlations, such as local quantum number conservation [33], are needed to describe the data. As the energy increases further (especially at the TeV scale), the onset of jets should play a more important role in the particle production, resulting in bigger clusters. This effect could be the underlying cause for the observed energy dependence of $K_{\text{eff}}$. 

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The study of long-range azimuthal correlations involved generating 2-D $\Delta\eta$-$\Delta\phi$ distributions in bins of event multiplicity and particle transverse momentum. The analysis procedure was to a large extent identical with that used for the minimum bias data described in section 4. With the addition of $p_T$ binning, both particles in the pairs used to calculate $R(\Delta\eta, \Delta\phi)$ were required to be within the selected $p_T$ range. The events were divided into bins of offline track multiplicity as outlined in table 1. In order to reach good statistics for the highest attainable charged particle densities, only data at 7 TeV were considered.

Figure 7 compares 2-D two-particle correlation functions for minimum bias events and high multiplicity events, for both inclusive particles and for particles in an intermediate $p_T$ bin. The top two panels show results from minimum bias events. The correlation function for inclusive particles with $p_T > 0.1$ GeV/$c$ shows the typical structure as described by the independent cluster model. The region at $\Delta\eta \approx 0$ and intermediate $\Delta\phi$ is dominated...
by particle emission from clusters with low transverse momentum, with some contribution from jet-like particle production near \((\Delta \eta, \Delta \phi) \approx (0, 0)\) due to near-side jet fragmentation and a broad elongated ridge around \(\Delta \phi \approx \pi\) due to fragmentation of back-to-back jets. Also visible is a shallow minimum at \(\Delta \phi \approx 0\) at large \(|\Delta \eta|\) due to momentum conservation. For the intermediate \(p_T\) region of \(1 \, \text{GeV}/c < p_T < 3 \, \text{GeV}/c\) a more pronounced near-side jet peak and away-side ridge are visible, due to the enhanced contribution of jet fragmentation to particle production for increasing \(p_T\).

For \(p_T\)-integrated two-particle correlations in high multiplicity events \((N_{\text{trk}}^{\text{offline}} \geq 110\), figure 7c\), most correlation structures are similar to those for minimum bias events. The cut on high multiplicity enhances the relative contribution of high \(p_T\) jets which fragment into a large number of particles and, therefore, has a qualitatively similar effect on the shape as the particle \(p_T\) cut on minimum bias events (compare figure 7b and figure 7c). However, it is interesting to note that a closer inspection of the shallow minimum at \(\Delta \phi \approx 0\) and \(|\Delta \eta| > 2\) in high multiplicity \(p_T\)-integrated events reveals it to be slightly less pronounced than that in minimum bias collisions.

Moving to the intermediate \(p_T\) range in high multiplicity events shown in figure 7d, an unexpected effect is observed in the data. A clear and significant “ridge”-like structure emerges at \(\Delta \phi \approx 0\) extending to \(|\Delta \eta|\) of at least 4 units. This is a novel feature of the data which has never been seen in two-particle correlation functions in \(pp\) or \(p\bar{p}\) collisions. Simulations using MC models do not predict such an effect. An identical analysis of high multiplicity events in PYTHIA8 [34] results in correlation functions which do not exhibit the extended ridge at \(\Delta \phi \approx 0\) seen in figure 7d, while all other structures of the correlation function are qualitatively reproduced. PYTHIA8 was used to compare to these data since it produces more high multiplicity events than PYTHIA6 in the D6T tune. Several other PYTHIA tunes, as well as HERWIG++ [30] and Madgraph [35] events were also investigated. No evidence for near-side correlations corresponding to those seen in data was found.

The novel structure in the high multiplicity \(pp\) data is reminiscent of correlations seen in relativistic heavy ion data. In the latter case, the observed long-range correlations are generally assumed to arise from various components of hydrodynamic flow of the produced medium [9, 36–39], from interactions between hard scattering processes and the medium, and from collective effects in the initial interaction of the nuclei.

However, new correlations can also start to emerge in the new energy regime probed here due to more elementary processes. For example, long range correlations are predicted also to occur in systems with a large number of fluctuating components, e.g. originating from additional color string connections. Such effects are presently not modeled in the MC generators.

Compared to the minimum bias analysis, the online and offline event selection of the rare high multiplicity events eliminated some sources of systematic uncertainties, but also introduced several additional ones. The bias due to the selection efficiency for NSD events, and its associated correction, were not an issue for the high multiplicity analysis since the efficiency reaches 100% as discussed in section 5.2. However, it was necessary to correct for the inefficiency in the HLT selection shown in figure 1. Comparison of correlation functions
for the high multiplicity bin, \( N_{\text{trk}}^{\text{offline}} \geq 110 \), taken from the two different trigger paths, \( (N_{\text{trk}}^{\text{offline}} > 70 \) and \( N_{\text{trk}}^{\text{offline}} > 85 \), see section 5.3) showed a systematic variation of 4 to 5%.

The pile-up rate (fraction of events with more than one good offline vertex found) reached about 40\% for the LHC conditions pertaining for most of the high multiplicity data-taking. Studies on correlations between two offline vertices in each event showed that about 10\% of the events contained pile-up that could not be distinguished by the vertex finding algorithm. Therefore, a high multiplicity event could be faked by a pile-up of several minimum bias collisions with very close vertex positions. Although such pile-up of independent pp collisions is not expected to generate additional correlations in this analysis, a data-driven limit on the effect of pile-up events was established. This was based on a comparison of results from runs with negligible pile-up collected with lower instantaneous luminosity to results obtained with high luminosity data at nominal bunch intensity. This comparison was limited by the size of the event sample collected for low luminosity conditions in early LHC running. For all luminosity selections, the near-side ridge signal was observed and a conservative systematic error of 15\%, which covers the difference over all run periods, was assigned.

In order to investigate the turn-on behavior of the "ridge"-like structure quantitatively and in finer detail, correlation functions were obtained in four bins of charged particle multiplicity and four bins of particle transverse momentum. To study the long-range azimuthal correlations, the 1-D \( \Delta \phi \) were calculated by integrating over the \( 2.0 < |\Delta \eta| < 4.8 \) region. Figure 8 shows the results for a range of \( p_T \) (from left to right) and multiplicity (from top to bottom) bins. CMS data are shown as solid circles and the lines show PYTHIA8 results. In this projection, only the range of \( 0 < \Delta \phi < \pi \) is shown, as the \( \Delta \phi \) correlation function is symmetric around \( \Delta \phi = 0 \) by construction. All panels show the away-side jet contribution at \( \Delta \phi \approx \pi \). In addition, for high multiplicity bins in the intermediate \( p_T \) region, \( 1 < p_T < 3 \) GeV/c, a second local maximum near \( \Delta \phi \approx 0 \) is clearly observed. This new feature of the long-range azimuthal correlation function is not present in low multiplicity or minimum bias data, which are dominated by the low multiplicity events.

The comparison of data to PYTHIA8 simulations is characterized by two discrepancies: the strength of the away-side correlation is over- or underpredicted for almost all bins. This quantitative discrepancy could be remedied by further tuning of the relative contributions of di-jet and multi-jet processes compared to particle production from soft processes in the model without introducing a qualitatively new mechanism. More importantly, PYTHIA8 qualitatively fails to reproduce the novel local maximum near \( \Delta \phi \approx 0 \) in any of the \( p_T \) or multiplicity bins. It appears that soft particle production from string fragmentation, the contribution from jet fragmentation, final-state radiation, and concurrent semihard multiparton interactions, to the extent they are parametrized in PYTHIA8, do not provide a mechanism to create the observed long-range, near-side particle correlations.

Figure 8 shows that the long-range, near-side correlation increases in strength with increasing multiplicity and is most prominent in the region of \( 1 < p_T < 3 \) GeV/c. The strength of the near-side ridge and its dependence on \( p_T \) and multiplicity can be quantified in more detail by calculating the associated yield, i.e., the number of other particles correlated with a specific particle. In the presence of multiple sources of correlations, the
Figure 8. Projections of 2-D correlation functions onto $\Delta \phi$ for $2.0 < |\Delta \eta| < 4.8$ in different $p_T$ and multiplicity bins for fully corrected 7 TeV $pp$ data and reconstructed PYTHIA8 simulations. Error bars are smaller than the symbols.

yield for the correlation of interest is commonly estimated using an implementation of the zero-yield-at-minimum (ZYAM) method \[40\]. The procedure uses $R(\Delta \phi)$ integrated over $2.0 < |\Delta \eta| < 4.8$ as shown in figure 8. In the first step, a second-order polynomial is fit to $R(\Delta \phi)$ in the region $0.1 < |\Delta \phi| < 2.0$. The location of the minimum of the polynomial in this region is denoted $\Delta \phi_{ZYAM}$. The contribution from the background source of correlations, in this case the away-side jet correlations, is assumed to be zero for $|\Delta \phi| \leq \Delta \phi_{ZYAM}$. Using the position of the minimum, the associated yield is then found by integrating $R(\Delta \phi)$ over the region $0 < |\Delta \phi| < \Delta \phi_{ZYAM}$ relative to the minimum in $R(\Delta \phi)$ and multiplying by $\int_{2.0}^{4.8} B(\Delta \eta) d|\Delta \eta|$ to account for the fact that only a limited $\Delta \eta$ range is used. The uncertainty on the minimum level of $R(\Delta \phi)$ obtained by the ZYAM procedure as well as varying the fit range in $\Delta \phi$ gives an uncertainty of 0.0025 on the associated yield, uniformly over all multiplicity and $p_T$ bins.
Figure 9. Associated yield for the near-side of the correlation function integrated over the region of $2.0 < |\Delta \eta| < 4.8$ as a function of event multiplicity in bins of $p_T$ for 7 TeV $pp$ collisions. The error bars correspond to statistical errors, while the brackets around the data points denote the systematic uncertainties. The open squares show results for PYTHIA8.

Figure 9 shows the associated yield as a function of event multiplicity integrated over $2.0 < |\Delta \eta| < 4.8$ in increasing bins of $p_T$. The ridge yield is consistent with zero for low multiplicity events. The emergence of the ridge is observed toward the very high multiplicity region, primarily for the intermediate $p_T$ range of $1 - 3$ GeV/$c$. The error bars correspond to statistical errors, while the brackets around the data points denote the systematic uncertainties. Results from the PYTHIA8 MC, shown in open squares in figure 9, are consistent with zero for all multiplicity and $p_T$ regions, indicating that the ridge observed in the data is totally absent in events produced by this generator.

To investigate the novel ridge-like structure further, two-particle correlations were calculated separately for like-sign and unlike-sign charged pairs. Possible problems related to the track reconstruction algorithm, like multiple reconstruction of the same particle or local occupancy changes, would be expected to affect like-sign pairs differently than unlike-sign pairs. The same choice of pairs of like- or unlike-sign was made for both the signal and background in eq. (4.1). Figure 10 shows the associated yield for like-sign (solid circles) and unlike-sign (open squares) two-particle correlations respectively as a function of event multiplicity integrated over $2.0 < |\Delta \eta| < 4.8$ in bins of $p_T$. Consistent multiplicity and $p_T$ dependencies of the near-side associated yield are observed for charge dependent and charge independent correlations. The results for like-sign and unlike-sign pairs agree with each other within uncertainties. Since the number of like- and unlike-sign pairs each represent roughly half of the total, the yield of associated pairs counting only one sign option is expected to be roughly a factor of two smaller than the unrestricted yield.

As a further cross-check, correlation functions were generated for tracks paired with ECAL photons (primarily due to $\pi^0$s) as well as pairs of two ECAL photons. These distributions showed similar behavior to those shown in figures 7 and 8, i.e., the high $|\Delta \eta|$ region contained a dip at $|\Delta \phi| \approx 0$ in minimum bias events and a ridge in that region for high multiplicity events. Data at 0.9 and 2.36 TeV were also analyzed for long-range correlations, but the statistics were not sufficient to draw a conclusion.
Figure 10. Like-sign and unlike-sign associated yield for the near-side of the correlation function integrated over the region of $2.0 < |\Delta \eta| < 4.8$ as a function of event multiplicity in bins of $p_T$. The error bars correspond to statistical errors, while the brackets around the data points denote the systematic uncertainties.

8 Conclusion

The CMS detector at the LHC has been used to measure angular correlations between two charged particles up to $|\Delta \eta| \approx 5$ and over the full range of $\Delta \phi$ in $pp$ collisions at $\sqrt{s} = 0.9$, 2.36, and 7 TeV. The extracted 2-D correlation functions show a variety of features. In minimum bias collisions they are dominated by a maximum at $\Delta \eta = 0$ extending over the full range in $\Delta \phi$, with a width which tends to increase with increasing $\Delta \phi$. A simple cluster model parametrization was fit to these short-range correlations in order to quantify their strength (the effective cluster size) and their extent in relative pseudorapidity (the cluster decay width). The cluster size is observed to increase slowly with beam energy, while the cluster width is essentially constant. The PYTHIA event generator with D6T tune correctly describes the cluster widths and the energy dependence of the cluster size but systematically underestimates the cluster size.

Long-range azimuthal correlations for $2.0 < |\Delta \eta| < 4.8$ have been studied for 7 TeV data, leading to the first observation of a long-range ridge-like structure at the near-side ($\Delta \phi \approx 0$) in $pp$ collisions. This striking feature is clearly seen for large rapidity differences $|\Delta \eta| > 2$ in events with an observed charged particle multiplicity of $N \approx 90$ or higher. The enhancement in the near-side correlation function is most evident in the intermediate transverse momentum range, $1 < p_T < 3$ GeV/c. In the $2.0 < |\Delta \eta| < 4.8$ range, a steep increase of the near-side associated yield with multiplicity has been found in the data, whereas simulations show an associated yield consistent with zero, independent of multiplicity and transverse momentum. The novel structure resembles similar features observed in heavy ion experiments [7–9]. However, the physical origin of our observation is not yet understood. Additional characteristics of the high multiplicity $pp$ events displaying this novel feature deserve further detailed study.
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References


[16] CMS collaboration, V. Khachatryan et al., Transverse momentum and pseudorapidity distributions of charged hadrons in pp collisions at $\sqrt{s} = 0.9$ and 2.36 TeV, JHEP 02 (2010) 041 [arXiv:1002.0621] [SPIRES].


[26] UA1 collaboration, C. Albajar et al., Bose-Einstein correlations in \( \bar{p}p \) interactions at \( \sqrt{s} = 0.2 \text{ TeV} \) to 0.9 TeV, Phys. Lett. B 226 (1989) 410 [SPIRES].

[27] CMS collaboration, V. Khachatryan et al., First Measurement of Bose-Einstein Correlations in Proton-Proton Collisions at \( \sqrt{s} = 0.9 \) and 2.36 TeV at the LHC, Phys. Rev. Lett. 105 (2010) 032001 [arXiv:1005.3294] [SPIRES].


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