

Lepton flavor violating Higgs boson decay at e^+e^- collidersIndrani Chakraborty^{*} and Biswarup Mukhopadhyaya[†]*Regional Centre for Accelerator-based Particle Physics, Harish-Chandra Research Institute, HBNI,
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We estimate the smallest branching ratio for the Higgs decay channel $h \rightarrow \mu\tau$, which can be probed at an e^+e^- collider, and compare it with the projected reach at the high-luminosity run of the LHC. Using a model-independent approach, Higgs production is considered in two separate cases. In the first case, hWW and hZZ couplings are allowed to be scaled by a factor allowed by the latest experimental limits on hWW and hZZ couplings. In the second case, we have introduced higher-dimensional effective operators for these interaction vertices. Keeping $\text{BR}(h \rightarrow \mu\tau)$ as a purely phenomenological quantity, we find that this branching ratio can be probed down to $\approx 2.69 \times 10^{-3}$ and $\approx 5.83 \times 10^{-4}$, respectively, at the 250 GeV and 1000 GeV runs of an e^+e^- collider.

DOI: [10.1103/PhysRevD.96.115020](https://doi.org/10.1103/PhysRevD.96.115020)**I. INTRODUCTION**

After the discovery of the scalar resonance around 125 GeV at the LHC [1,2], efforts are under way to determine whether it is indeed the Standard Model (SM) Higgs boson. The spin, parity, and couplings [3–12] of this new member are found to be in good agreement so far with the SM expectation. The couplings between the Higgs boson and gauge bosons, though consistent with the predictions of the SM [13–19], still leave some scope for deviation, thus keeping alive the possibility that it is “a Higgs” rather than “the Higgs.” The former possibility keeps up the hope of addressing the yet unanswered questions such as finding a suitable dark matter candidate, non-zero neutrino masses, and mixing and baryon asymmetry of the Universe. Side by side, possible hints of new physics may still be hidden in the considerable amount of imprecision remaining in the measurement of couplings between Higgs and heavy fermion pairs such as $\tau^+\tau^-$, $b\bar{b}$ [20–23], and, of course, the Higgs boson self-coupling. In fact, a global analysis of the Higgs boson data collected so far reveals that non-standard decays of the Higgs boson (including invisible decays) with branching ratio (BR) up to $\sim 23\%$ are still consistent with experimental measurements [24].

The study of non-standard decay modes of the Higgs boson in various scenarios can thus be a good probe of new physics, lepton flavor violating (LFV) Higgs decays being one class of them. Among them the decay rate of the

channel, $h \rightarrow \mu\tau$, is relatively less constrained. The ATLAS Collaboration has set an upper limit on $\text{BR}(h \rightarrow \mu\tau) < 1.43\%$ at 95% confidence level with the run-I data collected at an integrated luminosity of 20.3 fb^{-1} [25]. At the same center-of-mass energy, CMS has reported an upper limit of $\text{BR}(h \rightarrow \mu\tau) < 1.51\%$ at 95% confidence level with an integrated luminosity 19.7 fb^{-1} [26]. The CMS Collaboration has further updated their analysis with the $\sqrt{s} = 13 \text{ TeV}$ (run-II) data at an integrated luminosity 2.3 fb^{-1} and puts an upper limit $\text{BR}(h \rightarrow \mu\tau) < 1.2\%$ [27]. Side by side with these direct searches, several low-energy flavor violating processes, e.g., $\tau \rightarrow \mu\gamma$, $\tau \rightarrow 3\mu$, muon electric dipole moment, muon $(g-2)$, put indirect constraints on the Higgs flavor violating couplings [28–31]. In the context of specific models, attempts have been made to study this non-standard flavor violating decay for supersymmetric [32–44] as well as nonsupersymmetric extensions of SM [45–49], including two Higgs doublet models [35,50–57], the simplest little Higgs model [58], Randall-Sundrum scenarios [59,60], and models containing leptoquarks [61].

While further accumulation of data at the LHC 13 TeV run will be helpful in probing smaller $\text{BR}(h \rightarrow \mu\tau)$, the upper limit is not expected to improve in a drastic manner [31]. In this context, the relatively cleaner environment of electron-positron colliders can be more useful. We, therefore, explore the possibility of probing the same decay mode of the Higgs boson in an e^+e^- collider with the aim of improving upon the existing upper limit on its branching ratio imposed by the LHC.

We have adopted a model-independent approach. In practice, such lepton flavor violating Higgs decays can

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happen in extensions of the single-doublet scenario, such as those considered in Refs. [62,63]. In addition, terms originating from higher-dimensional operators that encapsulate physics at a high scale may drive such decays [29,64,65].

It is obvious that the event rates for the $(\mu\tau)$ final state depend, in addition to $\text{BR}(h \rightarrow \mu\tau)$, on the Higgs production rate in e^+e^- collisions, where the hVV ($V = W, Z$) interaction vertex is involved. We allow the possibility of new physics in hVV coupling as well, as perhaps can be expected in a scenario that drives flavor violating Higgs decays in the leptonic sector. We do this by (i) scaling the hVV coupling strength, keeping the Lorentz structure the same as SM, and (ii) introducing CP -even dimension-6 operators with new Lorentz structures. In the second scenario, momentum-dependent interactions can alter the kinematics of Higgs production. The existing constraints on such anomalous coupling have been taken into account [4,10,66–68].

The paper is organized as follows. In Sec. II we present the theoretical framework including two types of modifications at the production level as mentioned earlier. In this section we also discuss the relevant constraints derived from precision observables and their impact on the parameters characterizing physics beyond the Standard Model (BSM). Section III includes modification of Higgs production rates considering two aforementioned scenarios. In Sec. IV detailed collider simulation at different center-of-mass energies has been reported. We summarize and conclude in Sec. V.

II. SCHEME OF THE ANALYSIS

The objective of this study is to examine the reach of e^+e^- colliders in probing the lowest possible $\text{BR}(h \rightarrow \mu\tau)$, using a model-independent approach. For this, we study the different dominant Higgs production modes at different center-of-mass energies and further decay of the Higgs boson to $\mu\tau$. Since the signal event rate depends on both the Higgs production cross section as well as its decay branching ratio, we explore the possibility of BSM physics in both production and decay. For the decay of Higgs in $\mu\tau$ mode, instead of introducing a specific kind of coupling, we adopt a model-independent approach where the corresponding branching ratio itself is varied up to the allowed limit. We further take into account both the leptonic and the hadronic decays of τ , resulting in various final states in order to do a comparative study. The final state in the leptonic τ decay consists of two opposite-sign same- or different-flavored leptons ($\mu\mu$ or $e\mu$) and \cancel{E} . The hadronic decay ultimately leads to a $\mu + \tau_{\text{had}}(j) + \cancel{E}$ final state. The Higgs mass is reconstructed from various observed decay products using the collinear approximation [69], which has been discussed later in Sec. IV.

The dominant production channels of the Higgs boson at the e^+e^- collision is $e^+e^- \rightarrow Zh$ at low center-of-mass

energies such as $\sqrt{s} = 250$ GeV. $e^+e^- \rightarrow h\nu_e\bar{\nu}_e$ driven by W fusion dominates at $\sqrt{s} = 500$ GeV and 1000 GeV (the production cross section in ZZ fusion is negligible). Therefore hVV interaction ($V = W, Z$) is involved at the production level both at high and at low energies.

We include new physics effects at the production level, by modifying the Standard Model hVV couplings in two possible ways:

- (i) One can bring in just a multiplicative factor in the hVV interactions.
- (ii) The effect of various dimension-6 operators with new Lorentz structures in hVV interactions may have some role to play.

Any change in the predicted values of Higgs couplings is bound to affect the electroweak precision data [66–68] and the Higgs signal strengths in various decay modes. The allowed departure of the oblique electroweak parameters from their SM predicted values can be obtained from [70]

$$\begin{aligned} \Delta S &= 0.05 \pm 0.11, & \Delta T &= 0.09 \pm 0.13, \\ \Delta U &= 0.01 \pm 0.11. \end{aligned} \quad (1)$$

The signal strength in a particular decay channel of Higgs boson is defined as

$$\begin{aligned} \mu_{h \rightarrow X} &= \frac{\sigma^{\text{BSM}}(gg \rightarrow h) \times \text{BR}^{\text{BSM}}(h \rightarrow X)}{\sigma^{\text{SM}}(gg \rightarrow h) \times \text{BR}^{\text{SM}}(h \rightarrow X)}, \\ &= \frac{\sigma^{\text{BSM}}(gg \rightarrow h) \times \Gamma^{\text{BSM}}(h \rightarrow X) \times \Gamma_{\text{tot}}^{\text{SM}}}{\sigma^{\text{SM}}(gg \rightarrow h) \times \Gamma^{\text{SM}}(h \rightarrow X) \times \Gamma_{\text{tot}}^{\text{BSM}}}, \end{aligned} \quad (2)$$

$\sigma^{\text{SM}}(gg \rightarrow h)$, $\text{BR}^{\text{SM}}(h \rightarrow X)$ being the production cross section of the Higgs boson via gluon-gluon fusion and the branching ratio of that particular decay mode $h \rightarrow X$ in the SM. $\sigma^{\text{BSM}}(gg \rightarrow h)$, $\text{BR}^{\text{BSM}}(h \rightarrow X)$ are their BSM counterparts respectively.

For the Higgs signal strength (μ), we have used the combined results obtained from ATLAS and CMS [71,72] derived from both $\sqrt{s} = 7$ TeV and $\sqrt{s} = 8$ TeV runs of the LHC as shown in Table I. The 2σ allowed ranges for all the μ values have been used throughout our analysis.

TABLE I. Signal strengths of different decay channels of Higgs boson obtained at $\sqrt{s} = 7$ TeV and $\sqrt{s} = 8$ TeV.

Decay mode	ATLAS	CMS	ATLAS + CMS
$\mu_{h \rightarrow \gamma\gamma}$	$1.15^{+0.27}_{-0.25}$	$1.12^{+0.25}_{-0.23}$	$1.16^{+0.20}_{-0.18}$
$\mu_{h \rightarrow ZZ^*}$	$1.51^{+0.39}_{-0.34}$	$1.05^{+0.32}_{-0.27}$	$1.31^{+0.27}_{-0.24}$
$\mu_{h \rightarrow WW^*}$	$1.23^{+0.23}_{-0.21}$	$0.91^{+0.24}_{-0.21}$	$1.11^{+0.18}_{-0.17}$
$\mu_{h \rightarrow \tau\tau}$	$1.41^{+0.40}_{-0.35}$	$0.89^{+0.31}_{-0.28}$	$1.12^{+0.25}_{-0.23}$
$\mu_{h \rightarrow b\bar{b}}$	$0.62^{+0.37}_{-0.36}$	$0.81^{+0.45}_{-0.42}$	$0.69^{+0.29}_{-0.27}$

III. MODIFICATION OF HIGGS PRODUCTION RATES

A. Modification of SM hVV coupling with multiplicative factors only

Taking the Lorentz structure of the hVV interaction to be the same as the SM, the modified Lagrangian can be written as

$$\mathcal{L}_{\text{eff}}^{hVV} \supset a_W \left(\frac{2m_W^2}{v} \right) h W_\mu^+ W^{\mu-} + a_Z \left(\frac{m_Z^2}{v} \right) h Z_\mu Z^\mu, \quad (3)$$

where a_W and a_Z are the multiplicative factors, m_W and m_Z are the masses of W and Z bosons, respectively, and $v = 246$ GeV. It is assumed that Higgs couplings with the gluons and fermions are not modified with respect to the SM.

At $\sqrt{s} = 250$ GeV, the dominant production process of the Higgs boson is $e^+e^- \rightarrow Zh$, which includes the hZZ vertex, prompting us to vary a_Z . In a similar way, while considering W fusion to be the dominant one among the production channels at $\sqrt{s} = 500$ GeV and 1000 GeV, multiplicative factor a_W has been allowed to be varied, since the W -mediated channel $e^+e^- \rightarrow \nu\bar{\nu}h$ dominates over the other production modes. Such scaling of the SM hVV couplings arises, for example, when the SM Higgs doublet mixes with additional scalar multiplets. Any inequality of a_W and a_Z violates the invariance of custodial $SU(2)$ symmetry, resulting in tight constraints coming from the T parameter [10,66]. The values of a_W and a_Z are also chosen consistently with the Higgs signal strengths.

While checking consistency with the LHC data it has been assumed that the Higgs boson is produced via gluon fusion, which is the most efficient Higgs production mode at the LHC. Hence modification of the hVV vertices does not affect the Higgs production cross section. Thus the modifications in the μ values can be computed simply by the variation of Higgs branching ratios in different channels due to the introduction of the multiplicative factors a_Z and a_W .¹ The variation of the known signal strengths due to non-vanishing $\text{BR}(h \rightarrow \mu\tau)$ is neglected. The obtained ranges of a_Z and a_W compatible with the above precision constraints are

$$0.991 \leq a_Z \leq 1.001, \quad 0.997 \leq a_W \leq 1.028. \quad (4)$$

B. Modification of SM hVV coupling by introducing dimension-6 operators

We consider next the effect of introducing new Lorentz structures at the hVV interaction vertices, keeping

¹Note that, throughout this paper, while computing the modified μ values, we have considered Higgs boson production only via gluon fusion.

aforementioned multiplicative factors a_Z and a_W unity. For this purpose we have introduced the CP -even $SU(2)_L \times U(1)_Y$ invariant dimension-6 operators \mathcal{O}_W , \mathcal{O}_{WW} , \mathcal{O}_B , and \mathcal{O}_{BB} , as defined below [66],

$$\begin{aligned} \mathcal{O}_W &= (D_\mu \Phi)^\dagger \hat{W}^{\mu\nu} (D_\nu \Phi), & \mathcal{O}_{WW} &= \Phi^\dagger \hat{W}_{\mu\nu} \hat{W}^{\mu\nu} \Phi, \\ \mathcal{O}_B &= (D_\mu \Phi)^\dagger \hat{B}^{\mu\nu} (D_\nu \Phi), & \mathcal{O}_{BB} &= \Phi^\dagger \hat{B}_{\mu\nu} \hat{B}^{\mu\nu} \Phi \end{aligned} \quad (5)$$

with

$$\begin{aligned} D_\mu \Phi &= \left(\partial_\mu + \frac{i}{2} g_1 B_\mu + i g_2 \frac{\sigma_a}{2} W_\mu^a \right) \Phi, \\ \hat{B}_{\mu\nu} &= i \frac{g_1}{2} (\partial_\mu B_\nu - \partial_\nu B_\mu), \\ \hat{W}_{\mu\nu} &= i \frac{g_2}{2} \sigma^a (\partial_\mu W_\nu^a - \partial_\nu W_\mu^a - g_2 f^{abc} W_\mu^b W_\nu^c). \end{aligned} \quad (6)$$

Here Φ is SM or SM-like scalar doublet, g_1 and g_2 are, respectively, the $U(1)_Y$ and $SU(2)_L$ gauge couplings, σ_a 's are the Pauli spin matrices, and f^{abc} are the $SU(2)$ structure constants. The operator $\mathcal{O}_{BW} = \Phi^\dagger \hat{B}_{\mu\nu} \hat{W}^{\mu\nu} \Phi$ has been excluded, since it allows Z - γ mixing at tree level, thereby violating the custodial $SU(2)$ symmetry which is responsible for keeping the ρ parameter within its experimental bound [66,68]. Hence the Lagrangian involving only hVV interactions takes the form [66]

$$\mathcal{L}_{\text{eff}}^{hVV} \supset \frac{f_W}{\Lambda^2} \mathcal{O}_W + \frac{f_{WW}}{\Lambda^2} \mathcal{O}_{WW} + \frac{f_B}{\Lambda^2} \mathcal{O}_B + \frac{f_{BB}}{\Lambda^2} \mathcal{O}_{BB}, \quad (7)$$

where the f_n 's and Λ are couplings and new physics scale, respectively. We have taken $\Lambda = 1$ TeV throughout our analysis.

Since the hVV couplings are modified in the presence of these effective operators, this poses an apparent threat to perturbative unitarity in $V_L V_L \rightarrow V_L V_L$ ($V = W, Z$) at high energies. It should, however, be remembered that such a threat arises at scales above Λ , when additional degrees of freedom become operative. Unitarity is then expectedly ensured by the scenario that is responsible for such degrees of freedom.

The Lagrangian involving new Lorentz structures in hVV interactions can be written as [66]

$$\begin{aligned} \mathcal{L}_{\text{eff}}^{hVV} &= g_{h\gamma\gamma} h A_{\mu\nu} A^{\mu\nu} + g_{hZ\gamma}^{(1)} A_{\mu\nu} Z^\mu \partial^\nu h + g_{hZ\gamma}^{(2)} h A_{\mu\nu} Z^{\mu\nu} \\ &+ g_{hZZ}^{(1)} Z_{\mu\nu} Z^\mu \partial^\nu h + g_{hZZ}^{(2)} h Z_{\mu\nu} Z^{\mu\nu} \\ &+ g_{hWW}^{(1)} (W_{\mu\nu}^+ W^{-\mu} \partial^\nu h + \text{H.c.}) \\ &+ g_{hWW}^{(2)} h W_{\mu\nu}^+ W^{-\mu\nu} \end{aligned} \quad (8)$$

with effective couplings $g_{h\gamma\gamma}$, $g_{hZ\gamma}^{(1)}$, $g_{hZ\gamma}^{(2)}$, $g_{hZZ}^{(1)}$, $g_{hZZ}^{(2)}$, $g_{hWW}^{(1)}$, $g_{hWW}^{(2)}$. Here $V_{\mu\nu} = \partial_\mu V_\nu - \partial_\nu V_\mu$ with $V = A, Z, W$. These

effective couplings can be expressed as a linear combination of the f_n 's, mentioned earlier in Eq. (7).

$$\begin{aligned}
g_{h\gamma\gamma} &= -\left(\frac{g_2^2 v s_W^2}{2\Lambda^2}\right) \frac{f_{BB} + f_{WW}}{2}, \\
g_{hZ\gamma}^{(1)} &= \left(\frac{g_2^2 v}{2\Lambda^2}\right) \frac{s_W(f_W - f_B)}{2c_W}, \\
g_{hZ\gamma}^{(2)} &= \left(\frac{g_2^2 v}{2\Lambda^2}\right) \frac{s_W(s_W^2 f_{BB} - c_W^2 f_{WW})}{c_W}, \\
g_{hZZ}^{(1)} &= \left(\frac{g_2^2 v}{2\Lambda^2}\right) \frac{c_W^2 f_W + s_W^2 f_B}{2c_W^2}, \\
g_{hZZ}^{(2)} &= -\left(\frac{g_2^2 v}{2\Lambda^2}\right) \frac{s_W^4 f_{BB} + c_W^4 f_{WW}}{2c_W^2}, \\
g_{hWW}^{(1)} &= \left(\frac{g_2^2 v}{2\Lambda^2}\right) \frac{f_W}{2}, \\
g_{hWW}^{(2)} &= -\left(\frac{g_2^2 v}{2\Lambda^2}\right) f_{WW}. \tag{9}
\end{aligned}$$

c_W and s_W are the shorthand notations for $\cos\theta_W$ and $\sin\theta_W$, respectively, θ_W being the Weinberg angle. Here Higgs-gluon-gluon and Higgs-fermion-fermion interactions are taken to be the same as the SM.

For simplicity, we have switched on only one of the aforementioned four operators at a time. It is clear from Table II that hZZ couplings are modified for non-zero f_B , f_W and f_{BB} , f_{WW} , respectively. Likewise $g_{hWW}^{(1)}$ and $g_{hWW}^{(2)}$ depend on f_W and f_{WW} , respectively.

Thus the partial decay widths for the channels $h \rightarrow ZZ^*$, $h \rightarrow WW^*$, $h \rightarrow \gamma\gamma$, and $h \rightarrow Z\gamma$ are expected to be modified for non-zero f_n 's. The modified partial decay width of the Higgs boson can be expressed as polynomials of the effective coupling constants, i.e., f_B, f_{BB}, f_W, f_{WW} , partial width of all the other channels being the same as the SM. Since the decay width of $h \rightarrow Z\gamma$ is rather small in SM, its modification will hardly change the final results. Thus we have not included modification of this particular decay width, nor do we include the decay width for $h \rightarrow \mu\tau$ that contributes not more than 1% to the total Higgs decay rate. Expressions for modified decay widths involving the four effective couplings are as follows:

TABLE II. Modified couplings for non-zero f_n 's (taken one at a time).

Nonzero f_n 's	Modified couplings in Eq. (9)
f_B	$g_{hZ\gamma}^{(1)}, g_{hZZ}^{(1)}$
f_{BB}	$g_{h\gamma\gamma}, g_{hZ\gamma}^{(2)}, g_{hZZ}^{(2)}$
f_W	$g_{hZ\gamma}^{(1)}, g_{hZZ}^{(1)}, g_{hWW}^{(1)}$
f_{WW}	$g_{h\gamma\gamma}, g_{hZ\gamma}^{(2)}, g_{hZZ}^{(2)}, g_{hWW}^{(2)}$

(i) *Involving f_B only:*

$$\begin{aligned}
\Gamma_{h \rightarrow ZZ^*}^{\text{BSM}} &= 1.0745 \times 10^{-4} - 3.205 \times 10^{-7} f_B \\
&\quad + 1.751 \times 10^{-9} f_B^2. \tag{10}
\end{aligned}$$

(ii) *Involving f_{BB} only:*

$$\begin{aligned}
\Gamma_{h \rightarrow ZZ^*}^{\text{BSM}} &= 1.0745 \times 10^{-4} + 3.458 \times 10^{-8} f_{BB} \\
&\quad + 2.435 \times 10^{-10} f_{BB}^2, \\
\Gamma_{h \rightarrow \gamma\gamma}^{\text{BSM}} &= 9.279 \times 10^{-6} + 1.675 \times 10^{-5} f_{BB} \\
&\quad + 6.691 \times 10^{-6} f_{BB}^2. \tag{11}
\end{aligned}$$

(iii) *Involving f_W only:*

$$\begin{aligned}
\Gamma_{h \rightarrow ZZ^*}^{\text{BSM}} &= 1.0745 \times 10^{-4} - 1.0103 \times 10^{-6} f_W \\
&\quad + 1.075 \times 10^{-8} f_W^2, \tag{12}
\end{aligned}$$

$$\begin{aligned}
\Gamma_{h \rightarrow WW^*}^{\text{BSM}} &= 8.7505 \times 10^{-4} - 9.99 \times 10^{-6} f_W \\
&\quad + 1.8604 \times 10^{-8} f_W^2. \tag{13}
\end{aligned}$$

(iv) *Involving f_{WW} only:*

$$\begin{aligned}
\Gamma_{h \rightarrow ZZ^*}^{\text{BSM}} &= 1.0745 \times 10^{-4} + 4.452 \times 10^{-7} f_{WW} \\
&\quad + 6.838 \times 10^{-10} f_{WW}^2, \tag{14}
\end{aligned}$$

$$\begin{aligned}
\Gamma_{h \rightarrow \gamma\gamma}^{\text{BSM}} &= 9.279 \times 10^{-6} + 7.66 \times 10^{-6} f_{WW} \\
&\quad + 5.599 \times 10^{-6} f_{WW}^2, \tag{15}
\end{aligned}$$

$$\begin{aligned}
\Gamma_{h \rightarrow WW^*}^{\text{BSM}} &= 8.7505 \times 10^{-4} + 8.484 \times 10^{-6} f_{WW} \\
&\quad + 2.2 \times 10^{-8} f_{WW}^2. \tag{16}
\end{aligned}$$

The f_n -independent term as well as those linear and quadratic in f_n in the above equations correspond to contributions from SM, interference between SM and BSM, and purely BSM, respectively. For each case the modifications in the μ values have been calculated to compare with the existing constraints.

The allowed ranges of f_B, f_W, f_{BB}, f_{WW} have been derived using 2σ -allowed ranges of the electroweak precision observables as given in Eq. (1) and 2σ -allowed ranges of the signal strength values shown in Table I. The allowed ranges for the individual couplings are given in Table III. In the presence of f_{BB} and f_{WW} , $\Gamma_{h \rightarrow \gamma\gamma}$ gets modified. The partial decay width $\Gamma_{h \rightarrow \gamma\gamma}$ becomes minimum at $f_{BB} = -1.25$ and $f_{WW} = -0.68$, respectively (taking one of them non-zero at a time). In the intermediated excluded region around the minimum, the signal strength of the channel $h \rightarrow \gamma\gamma$ becomes lower than its 2σ allowed lower limit. Thus the intermediate region $-2.38 < f_{BB} < -0.12$ for f_{BB} and $-1.04 < f_{WW} < -0.319$

TABLE III. Allowed ranges of f_n 's with $\Lambda = 1$ TeV obtained by using 2σ -allowed ranges of the electroweak precision observables and 2σ -allowed ranges of the Higgs signal strengths.

Couplings	Allowed ranges
f_B	$[-11.74, 18.66]$
f_{BB}	$[-2.78, -2.38] \cup [-0.12, 0.283]$
f_W	$[-25.1, 25.8]$
f_{WW}	$[-1.86, -1.04] \cup [-0.319, 0.5]$

for f_{WW} are excluded by the 2σ constraint on the signal strength.

IV. COLLIDER ANALYSIS

The prospect of observing LFV decays of the 125 GeV Higgs boson has been explored in the context of the LHC [25,26,31,73,74]. These studies indicate that the smallest LFV decay branching ratio $[\text{BR}(h \rightarrow \mu\tau)]$ that can be probed at the high-luminosity run of the LHC at 14 TeV is $\sim 10^{-2}$. A recent phenomenological study [75] provides the lower bound of the branching ratio of $h \rightarrow \mu\tau$ to be $\sim 10^{-3}$. A lepton collider on the other hand provides a much cleaner environment and thus provides the ideal platform to probe such non-standard decays of the Higgs boson [31,76]. Our primary aim in this section would be to assess whether one can probe even smaller branching ratios with different center-of-mass energies. At $\sqrt{s} = 250$ GeV, $e^+e^- \rightarrow Zh$ is the most dominant production mode of the Higgs boson. However, this production cross-section diminishes with increasing center-of-mass energy unlike the W -fusion channel, $e^+e^- \rightarrow h\nu_e\bar{\nu}_e$. As a result, at $\sqrt{s} = 500$ and 1000 GeV, the W -fusion channel turns out to be the dominant contributor in Higgs production (the production cross section of ZZ fusion is negligible even at high \sqrt{s}). We have explored the search prospects of the present scenario at all these three center-of-mass energies.

To perform our collider analysis, the new interaction vertices have been included in FEYNRULES [77,78]. We have used MADGRAPH5 [79,80] to generate events at the parton level and subsequently PYTHIA-6 [81] for decay, showering, and hadronization. While generating the events, we have used the default dynamic factorization and renormalization scales [82] at MADGRAPH. Detector simulation has been performed using DELPHES-3.3.3 [83–85]. Jets have been reconstructed with FASTJET [86] using the anti-kt [87] algorithm. We have taken the τ -tagging efficiency and the probability of a jet faking τ to be 60% and 2%, respectively. To identify the leptons, photons, and jets in the final state, we have imposed the following primary selection criteria:

- (i) All the charged leptons are selected with a minimum transverse momentum cut-off of 10 GeV, i.e., $p_T^\ell > 10$ GeV. Further, the electrons and muons

must also lie within the pseudorapidity windows $|\eta^e| < 2.5$ and $|\eta^\mu| < 2.5$, respectively.

- (ii) All the photons are selected with $p_T^\gamma > 10$ GeV and $|\eta^\gamma| < 2.5$.
- (iii) All the jets in the final state must satisfy $p_T^j > 30$ GeV and $|\eta^j| < 2.5$.
- (iv) It is ensured that the final state particles are well separated by demanding $\Delta R > 0.4$ between lepton-jet pairs and $\Delta R > 0.25$ between lepton pairs.

Let us first consider the scenario described in Sec. II where we have used the maximally allowed values of a_Z ($a_Z = 1.001$) and a_W ($a_W = 1.028$) in agreement with the electroweak precision observables and Higgs signal strength measurements, in order to determine the cross sections in $e^+e^- \rightarrow Zh$ and $e^+e^- \rightarrow \nu_e\bar{\nu}_e h$ production modes, respectively. Later in this section, we proceed to discuss the possible improvement in the results in the presence of higher-dimensional operators.

A. $e^+e^- \rightarrow Zh$ at $\sqrt{s} = 250$ GeV

For this production mode, we chose to study the cleaner channel where the Z boson decays leptonically. Further, we have considered both the leptonic and hadronic decays of the τ arising from the 125 GeV h decay. Thus depending on the decays of τ , the various final states can be as follows:

- (1) Tau decaying leptonically: $4\ell + \cancel{E}$, $\ell = e, \mu$
 - (a) $e^+e^- \rightarrow Zh, Z \rightarrow \mu^+\mu^-, h \rightarrow \mu\tau \rightarrow e\mu + \cancel{E} \Rightarrow e + 3\mu + \cancel{E}$
 - (b) $e^+e^- \rightarrow Zh, Z \rightarrow \mu^+\mu^-, h \rightarrow \mu\tau \rightarrow 2\mu + \cancel{E} \Rightarrow 4\mu + \cancel{E}$
 - (c) $e^+e^- \rightarrow Zh, Z \rightarrow e^+e^-, h \rightarrow \mu\tau \rightarrow e\mu + \cancel{E} \Rightarrow \mu + 3e + \cancel{E}$
 - (d) $e^+e^- \rightarrow Zh, Z \rightarrow e^+e^-, h \rightarrow \mu\tau \rightarrow 2\mu + \cancel{E} \Rightarrow 2e + 2\mu + \cancel{E}$
- (2) Tau decaying hadronically: $3\ell + \tau_{\text{had}} + \cancel{E}$, $\ell = e, \mu$
 - (a) $e^+e^- \rightarrow Zh, Z \rightarrow \mu^+\mu^-, h \rightarrow \mu\tau \rightarrow \mu\tau_{\text{had}} + \cancel{E} \Rightarrow \tau_{\text{had}} + 3\mu + \cancel{E}$
 - (b) $e^+e^- \rightarrow Zh, Z \rightarrow e^+e^-, h \rightarrow \mu\tau \rightarrow \mu\tau_{\text{had}} + \cancel{E} \Rightarrow 2e + \mu + \tau_{\text{had}} + \cancel{E}$

The corresponding major SM backgrounds can arise from the following channels:

- (1) $e^+e^- \rightarrow Zh, Z \rightarrow \ell\bar{\ell}, h \rightarrow \ell\bar{\ell}; \ell = e, \mu, \tau$
- (2) $e^+e^- \rightarrow ZZ, Z \rightarrow \ell\bar{\ell}, Z \rightarrow \ell\bar{\ell}; \ell = e, \mu, \tau$
- (3) $e^+e^- \rightarrow ZZ\ell\bar{\ell}, Z \rightarrow \ell\bar{\ell}, Z \rightarrow \nu\bar{\nu}; \ell = e, \mu, \tau; \nu = \nu_e, \nu_\mu, \nu_\tau$
- (4) $e^+e^- \rightarrow ZZ\nu\bar{\nu}, Z \rightarrow \ell\bar{\ell}, Z \rightarrow \ell\bar{\ell}; \nu = \nu_e, \nu_\mu, \nu_\tau$
- (1) Final state: $4\ell + \cancel{E}$:

We have used the following set of cuts to identify our signal events and reduce the SM background contribution to get the best possible signal to background ratio:

- (a) **A0**: The final state must consist of four leptons with at least one μ . A veto has been applied on the jets in the final state since the τ in this case is expected to decay leptonically.

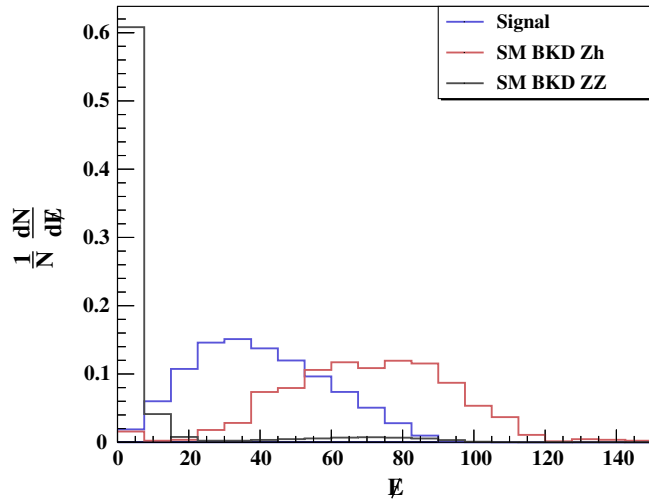


FIG. 1. Normalized E distribution for signal and backgrounds at $\sqrt{s} = 250$ GeV for final state: $4\ell + \cancel{E}$.

- (b) **A1**: For such a signal, some amount of missing energy is always expected to arise from Higgs boson decay. A normalized distribution of E for the signal process as well as the most dominant background channels ZZ and Zh are shown in Fig. 1 where the blue line corresponds to the signal process and the black and the red lines correspond to ZZ and Zh background production channels, respectively. We demand, $100 \text{ GeV} > E > 20 \text{ GeV}$.
- (c) **A2**: At least one of the same-flavor opposite-sign lepton pairs is expected to arise from the Z -boson decay in the signal. Hence all such pairs have been identified in order to reconstruct their invariant masses ($M_{\ell\ell}$), and the pair for which $M_{\ell\ell}$ lies closest to the Z -boson mass (m_Z) has been identified. We have then demanded that $|M_{\ell\ell} - m_Z| < 10 \text{ GeV}$ for that particular pair of same-flavor opposite-sign leptons.
- (d) **A3**: Once the leptons arising from the Z -boson decays are identified, the rest of the leptons and missing energy should mostly originate from the decay of h . To reconstruct the Higgs mass, the collinear approximation [69] has been used as mentioned earlier. The mass of Higgs being much greater than that of τ , the decay products of τ are highly boosted in its original direction. Thus the direction of the neutrino momenta can be approximated to be in the same direction of the visible decay products of τ . Thus the transverse component of the neutrino momentum can be estimated by taking the projection of the missing transverse energy in the direction of the visible tau decay products, i.e., $\vec{p}_T^\nu = \vec{E}_T \cdot \hat{p}_T^{\tau_{\text{vis}}}$.

We have used the collinear mass (M_{coll}) [88], defined as

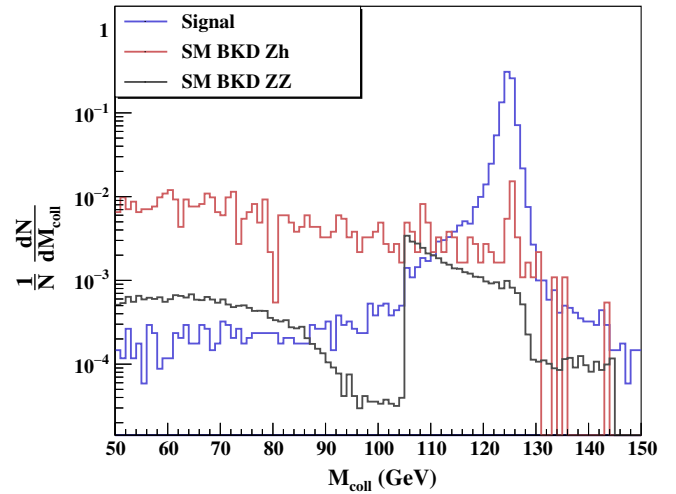


FIG. 2. Normalized M_{coll} distribution for signal and backgrounds at $\sqrt{s} = 250$ GeV for final state: $4\ell + \cancel{E}$.

$$M_{\text{coll}} = \frac{M_{\text{vis}}}{\sqrt{x_{\tau_{\text{vis}}}}}, \quad (17)$$

where M_{vis} represents the invariant mass of the remaining leptons and the fraction of the tau momentum carried by the visible tau decay products is $x_{\tau_{\text{vis}}} = \frac{|\vec{p}_T^{\tau_{\text{vis}}}|}{|\vec{p}_T^{\tau_{\text{vis}}}| + |\vec{p}_T^\nu|}$.

Figure 2 represents the normalized distribution of M_{coll} for the signal and background channels with the same color coding as in Fig. 1. The signal clearly shows a sharper peak around the Higgs boson mass region.

We have demanded that $(m_h + 20) \text{ GeV} > M_{\text{coll}} > (m_h - 20) \text{ GeV}$.

In Table IV we have presented the detailed cut-flow numbers obtained from our collider simulation at $\sqrt{s} = 250$ GeV for integrated luminosity $\mathcal{L} = 250 \text{ fb}^{-1}$

TABLE IV. Cross sections of the signal and various background channels for leptonic decay of τ are shown in pb alongside the number of expected events for the individual channels at 250 fb^{-1} luminosity after applying each of the cuts **A0–A3** as listed in the text. NEV \equiv number of events. Signal cross section has been quoted for $\text{BR}(h \rightarrow \mu\tau) = 9.78 \times 10^{-3}$.

Process	$\sqrt{s} = 250 \text{ GeV}$				
	σ [pb]	NEV ($\mathcal{L} = 250 \text{ fb}^{-1}$)			
		A0	A1	A2	A3
$e^+e^- \rightarrow Zh$	1.37×10^{-4}	5	4	4	4
$e^+e^- \rightarrow Zh$	0.24	27	23	20	2
$e^+e^- \rightarrow ZZ$	9.48×10^{-3}	515	25	20	...
$e^+e^- \rightarrow ZZll$	2.558×10^{-4}	1
$e^+e^- \rightarrow ZZ\nu\bar{\nu}$	1.3×10^{-3}	1	1

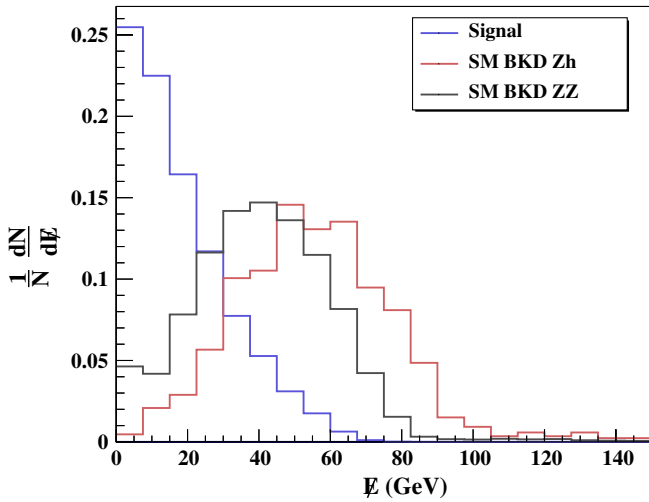


FIG. 3. Normalized E distribution for signal and backgrounds at $\sqrt{s} = 250$ GeV for final state: $3\ell + 1\tau - \text{jet} + E$.

corresponding to the signal $4\ell + E$ [with $\text{BR}(h \rightarrow \mu\tau) = 9.78 \times 10^{-3}$] as well as the different SM background channels.

As evident from Table IV, the ZZ production channel is potentially the most dominant contributor to the SM background. However, the E (A1) and M_{coll} (A3) cuts turn out to be particularly effective in reducing this background. The SM Zh production channel can also be a possible source of background due to its large production cross section, but the signal requirement of multiple leptons and no associated jets reduces this contribution that is further dented by the cut A3. Clearly, the signal rate being extremely small, one requires a large integrated luminosity in order to observe any such events. As the numbers in Table IV indicate, one would need an integrated luminosity of $\approx 450 \text{ fb}^{-1}$ in order to gain a 3σ statistical significance for this signal at $\sqrt{s} = 250$ GeV with our choice of $\text{BR}(h \rightarrow \mu\tau) = 9.78 \times 10^{-3}$.

(2) Final state: $3\ell + 1\tau - \text{jet} + E$:

As discussed earlier, such final states may arise if the τ originating from the Higgs decays hadronically. We have used the following set of cuts to identify our signal events and reduce the SM contribution to get the best possible signal to background ratio.

- (a) **B0**: The final state must consist of three leptons with at least one μ . We further demand that the number of jets in the final state should be restricted to one and it must be identified as a τ jet.
- (b) **B1**: For a hadronic decay of τ , the E distribution is softer compared to the leptonic decay scenario. This is indicated by Fig. 3, which shows the normalized distribution of E for the $3\ell + 1\tau - \text{jet} + E$ final state for the signal as well as ZZ and Zh background production channels with the same color coding as Fig. 1.

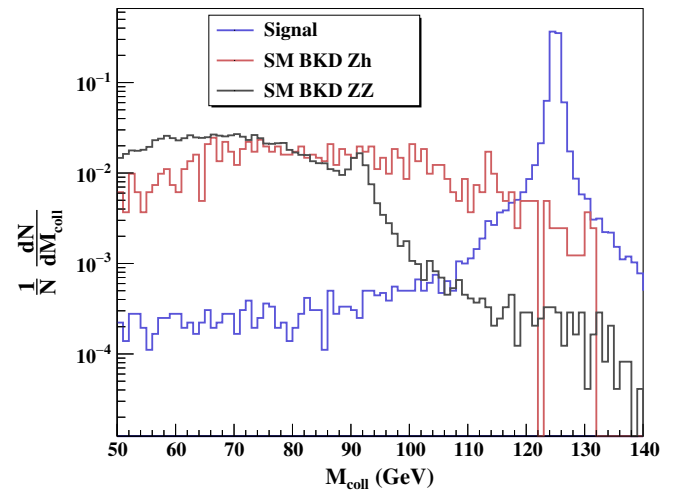


FIG. 4. Normalized M_{coll} distribution for signal and backgrounds at $\sqrt{s} = 250$ GeV for final state: $3\ell + 1\tau - \text{jet} + E$.

We, therefore, demand a missing energy upper limit: $E < 30$ GeV.

- (c) **B2**: If the other two leptons in the event apart from the one μ originating from h happen to be electrons, they have most likely been originated from the Z boson. However, if all three leptons in the event happen to be muons, we follow the same exercise as described in A2 to identify the $\mu^+\mu^-$ pair originating from the Z boson and similarly restrict the resulting $M_{\ell\ell}$ within $|M_{\ell\ell} - m_Z| < 10$ GeV.
- (d) **B3**: In this case, the visible decay products of the Higgs boson consist of a lepton and a τ jet. We reconstruct M_{coll} in a similar way as described in A3 and subsequently demand that $(m_h + 20) \text{ GeV} > M_{\text{coll}} > (m_h - 20) \text{ GeV}$. Figure 4 represents the distribution of M_{coll} before applying the cuts.

In Table V below we have presented the cut-flow numbers obtained from our collider simulation at $\sqrt{s} = 250$ GeV and

TABLE V. Cross sections of the signal and various background channels for hadronic decay of τ are shown in pb alongside the number of expected events for the individual channels at 250 fb^{-1} luminosity after applying each of the cuts **B0–B3** as listed in the text. NEV \equiv number of events. Signal cross section has been quoted for $\text{BR}(h \rightarrow \mu\tau) = 9.78 \times 10^{-3}$.

		$\sqrt{s} = 250$ GeV			
		NEV ($\mathcal{L} = 250 \text{ fb}^{-1}$)			
Process	σ [pb]	B0	B1	B2	B3
$e^+e^- \rightarrow Zh$	1.37×10^{-4}	5	3	3	3
$e^+e^- \rightarrow Zh$	0.24	10	1	1	1
$e^+e^- \rightarrow ZZ$	9.48×10^{-3}	25	6	6	...
$e^+e^- \rightarrow ZZll$	2.558×10^{-4}
$e^+e^- \rightarrow ZZ\nu\bar{\nu}$	1.3×10^{-3}

TABLE VI. Lowest branching ratio that can be probed with 3σ statistical significance for the two different final states (arising from leptonic and hadronic decay of τ) at $\sqrt{s} = 250$ GeV. The last column indicates the BR reach when the event rates of these two final states are combined.

$\mathcal{L}(\text{fb}^{-1})$	Lowest BR in $(4\ell + \cancel{E})$	Lowest BR in $(3\ell + \tau_{\text{had}} + \cancel{E})$	Combined BR
350	0.0109	0.0111	7.42×10^{-3}
500	8.87×10^{-3}	8.96×10^{-3}	6.0×10^{-3}
1000	5.94×10^{-3}	5.92×10^{-3}	4.09×10^{-3}

an integrated luminosity of $\mathcal{L} = 250 \text{ fb}^{-1}$ corresponding to our signal $3\ell + 1\tau - \text{jet} + \cancel{E}$ [with $\text{BR}(h \rightarrow \mu\tau) = 9.78 \times 10^{-3}$] as well as the different SM background channels.

As evident from Table V, the ZZ production channel is potentially the dominant contributor to the SM background. However, in this case also, \cancel{E} (**B1**) and M_{coll} (**B3**) cuts turn out to be particularly effective in reducing this background. The SM Zh production channel can also be the possible source of background which is reduced effectively by **B1**. As the numbers indicate, much as the leptonic τ -decay scenario, here also one requires an integrated luminosity of $\approx 450 \text{ fb}^{-1}$ in order to obtain a 3σ statistical significance with a choice of $\text{BR}(h \rightarrow \mu\tau) = 9.78 \times 10^{-3}$.

In Table VI we have shown the lowest possible reach of the e^+e^- collider in probing $\text{BR}(h \rightarrow \mu\tau)$ at the 3σ level for different integrated luminosities for the two possible final states, $3\ell + 1\tau - \text{jet} + \cancel{E}$ and $4\ell + \cancel{E}$ studied at $\sqrt{s} = 250$ GeV for comparison. We have presented the numbers for three predicted luminosities, i.e., 350 fb^{-1} , 500 fb^{-1} , and 1000 fb^{-1} at 3σ significance.² Results for both hadronic and leptonic decay modes of τ have been quoted individually along with the combined result (obtained by merging the results from two different decay modes of τ). Both the leptonic and hadronic decay modes of τ perform with similar effectiveness in probing the lowest possible $\text{BR}(h \rightarrow \mu\tau)$ at $\sqrt{s} = 250$ GeV. The result obtained by combining the two different final states, however, can do slightly better than the individual channels as indicated by the numbers in the last column of Table VI. It can be inferred that the lowest probed branching ratio at $\sqrt{s} = 250$ GeV is $\sim 10^{-3}$.

B. $e^+e^- \rightarrow \nu_e \nu_e h$ at $\sqrt{s} = 1000$ GeV

The W -fusion production mode, namely $e^+e^- \rightarrow \nu_e \bar{\nu}_e h$, although having a negligible cross section compared to $e^+e^- \rightarrow Zh$ at $\sqrt{s} = 250$ GeV, becomes the most dominating one at $\sqrt{s} = 500$ GeV and 1000 GeV. The production cross section in the channel $e^+e^- \rightarrow Zh$, on the other

²The statistical significance (σ') has been calculated for the number of signals (s) and number of backgrounds (b) using $\sigma' = \sqrt{2[(s+b)\ln(1+\frac{s}{b}) - s]}$.

hand, starts gradually decreasing beyond $\sqrt{s} = 250$ GeV and thus becomes less relevant for $\sqrt{s} = 500$ GeV or above. It would be interesting to see if a further increase in the center-of-mass energy can help us reach better sensitivity in probing a smaller $h \rightarrow \mu\tau$ branching ratio. The W -fusion production mode gives rise to a single Higgs associated with two electron neutrinos that contribute to the missing energy. Hence depending on the leptonic or hadronic decay of the τ , the final state may consist of the following signal channels:

- (1) Tau decaying leptonically: $2\ell + \cancel{E}$, $\ell = e, \mu$
 - (a) $e^+e^- \rightarrow \nu_e \bar{\nu}_e h, h \rightarrow \mu\tau \rightarrow e\mu + \cancel{E} \Rightarrow e + \mu + \cancel{E}$
 - (b) $e^+e^- \rightarrow \nu_e \bar{\nu}_e h, h \rightarrow \mu\tau \rightarrow 2\mu + \cancel{E} \Rightarrow 2\mu + \cancel{E}$
- (2) Tau decaying hadronically: $\mu + \tau_{\text{had}} + \cancel{E}$
 - (a) $e^+e^- \rightarrow \nu_e \bar{\nu}_e h, h \rightarrow \mu\tau \rightarrow \mu\tau_{\text{had}} + \cancel{E} \Rightarrow \tau_{\text{had}} + \mu + \cancel{E}$

The relevant SM background channels consist of W^+W^- , $\tau^+\tau^-$, $t\bar{t}$, ZZ, Zh, W^+W^-Z , ZZZ, $t\bar{t}Z$, ZZh, and $\ell j j \nu$. Our analysis with $\sqrt{s} = 500$ GeV reveals that there is little scope to increase the sensitivity in probing $\text{BR}(h \rightarrow \mu\tau)$ to much smaller values than what we have already obtained for the $\sqrt{s} = 250$ GeV case with $e^+e^- \rightarrow Zh$ production mode even at higher ($\approx 1000 \text{ fb}^{-1}$) luminosities. At $\sqrt{s} = 500$ GeV, the overall rate of the Higgs production through $e^+e^- \rightarrow \nu_e \bar{\nu}_e h$ and its subsequent decay to $\mu\tau$ is of the order of 10^{-4} pb. Moreover, the background coming from the W^+W^- channel dominates over the other SM backgrounds at this center-of-mass energy. The number of background events coming from the W^+W^- channel being very large compared to the number of signals even after applying suitable cuts on the kinematic variables makes it non-trivial to achieve a 3σ significance. Hence we chose not to present the numerical results from this simulation. Instead we have presented below the results obtained for the $\sqrt{s} = 1000$ GeV analysis, where the production rate is considerably higher.

- (1) *Final state: $2\ell + \cancel{E}$:*

Here we have used the following set of kinematical cuts in order to reduce the SM background contributions to gain the best possible signal to background ratio.

- (a) **C0**: There must be one hard muon along with another lepton (electron or muon) in the final state. Since the τ decays leptonically, there are no direct sources of jets. Hence we put a veto on jets on the final state including τ and b jets.
- (b) **C1**: Missing energy distribution for the final state $2\ell + \cancel{E}$ is shown in Fig. 5 for the signal events (blue line) as well as the dominant background production channels, namely, $t\bar{t}$ (brown line), WW (black line), WWZ (violet line), and ZZ (grey line) at $\sqrt{s} = 1000$ GeV.

We demand a \cancel{E} window: $1000 \text{ GeV} > \cancel{E} > 600 \text{ GeV}$.

- (c) **C2**: In the signal events, both the leptons in the event are expected to arise from the Higgs decay,

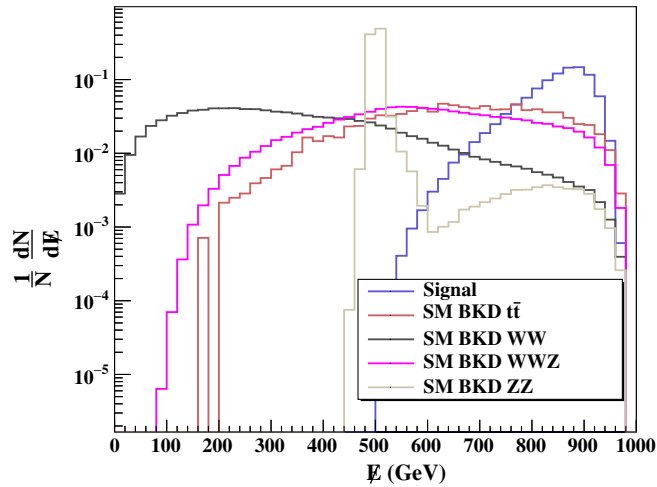


FIG. 5. Normalized \cancel{E} distribution for signal and backgrounds at $\sqrt{s} = 1000$ GeV for final state: $2\ell + \cancel{E}$.

whereas for the background events, two leptons can originate from two different parent particles and may have a larger angle in between them. For example, in the W^+W^- background channel, the two leptons in the event are back to back and thus have a large separation angle that can be exploited to reduce the background contribution. This kinematic feature can be observed in Fig. 6 where the normalized distribution of $\cos\theta_{\ell\mu}$ is shown for the signal and SM background events with the same color coding as in Fig. 5.

We demand $0.9 > \cos\theta_{\ell\mu} > -0.8$.

- (d) **C3**: We demand that the invariant mass of the visible particles, that is, of the two-lepton system, should lie within the region $120 \text{ GeV} > M_{\ell\mu} > 40 \text{ GeV}$. Figure 7 represents normalized distribution of $M_{\ell\mu}$ for the signal and SM

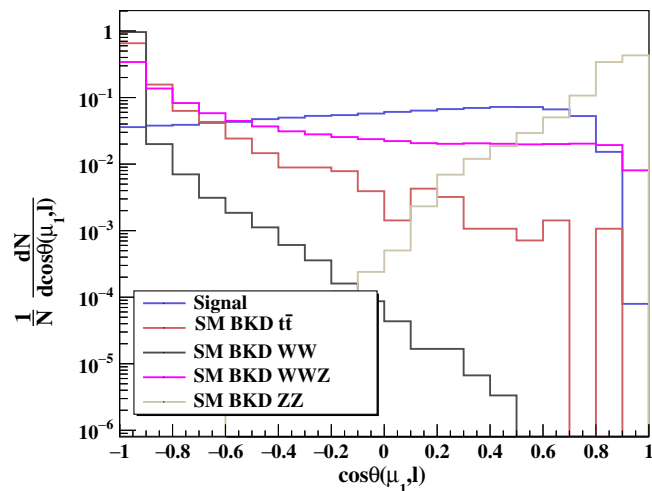


FIG. 6. Normalized $\cos\theta_{\ell\mu}$ distribution for signal and backgrounds at $\sqrt{s} = 1000$ GeV for final state: $2\ell + \cancel{E}$.

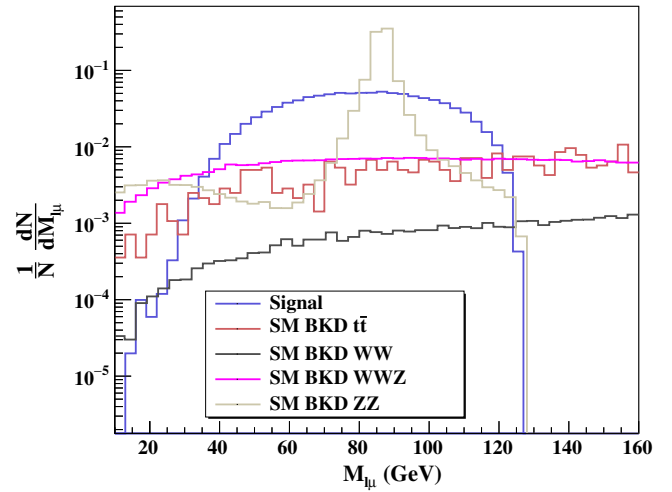


FIG. 7. Normalized $M_{\ell\mu}$ distribution for signal and backgrounds at $\sqrt{s} = 1000$ GeV for final state: $2\ell + \cancel{E}$.

background events with the same color coding as in Fig. 5.

- (e) **C4**: In our signal events, the hardest muon (μ_1) is likely to be generated directly from the Higgs decay. Hence, we expect the missing energy vector $\vec{\cancel{E}}$ to be well separated from this muon. We demand $3.14 > \Delta\phi(\mu_1, \vec{\cancel{E}}) > 1.0$. Figure 8 shows the distribution of $\Delta\phi(\mu_1, \vec{\cancel{E}})$ for the signal and SM background events with the same color coding as in Fig. 5.

In Table VII, we have presented the cut-flow numbers obtained from our simulation at $\sqrt{s} = 1000$ GeV and an integrated luminosity of $\mathcal{L} = 500 \text{ fb}^{-1}$ corresponding to our signal $2\ell + \cancel{E}$ [with $\text{BR}(h \rightarrow \mu\tau) = 9.78 \times 10^{-3}$] as well as the different SM background channels.

As evident from the numbers in Table VII, the WW production channel is the most dominant contributor to the

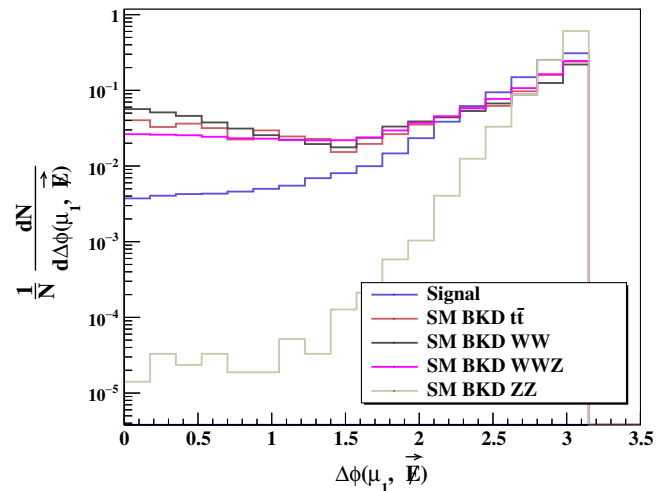


FIG. 8. Normalized $\Delta\phi(\mu_1, \vec{\cancel{E}})$ distribution for signal and backgrounds at $\sqrt{s} = 1000$ GeV for final state: $2\ell + \cancel{E}$.

TABLE VII. Cross sections of the signal and various background channels for the leptonic decay of τ are shown in pb alongside the number of expected events for the individual channels at 500 fb^{-1} luminosity after applying each of the cuts **C0–C4** as listed in the text. $\text{NEV} \equiv$ number of events. All the numbers are presented for $\text{BR}(h \rightarrow \mu\tau) = 9.78 \times 10^{-3}$.

Process	σ [pb]	$\sqrt{s} = 1000 \text{ GeV}$				
		NEV ($\mathcal{L} = 500 \text{ fb}^{-1}$)				
		C0	C1	C2	C3	C4
$e^+e^- \rightarrow \nu_e \bar{\nu}_e h$	2.01×10^{-3}	202	201	187	182	179
$e^+e^- \rightarrow W^+W^-$	0.12714	19010	2331	266	151	127
$e^+e^- \rightarrow \tau^+\tau^-$	1.562×10^{-6}	1
$e^+e^- \rightarrow t\bar{t}$	0.0153	29	18	5	3	2
$e^+e^- \rightarrow ZZ$	3.188×10^{-3}	339	15	7	3	3
$e^+e^- \rightarrow Zh$	1.533×10^{-4}	4	4	4	2	2
$e^+e^- \rightarrow W^+W^-Z$	9.814×10^{-4}	154	75	53	23	21
$e^+e^- \rightarrow ZZZ$	9.51×10^{-6}	1	1	1	1	1
$e^+e^- \rightarrow t\bar{t}Z$	4.64×10^{-3}
$e^+e^- \rightarrow ZZh$	3.21×10^{-4}
$e^+e^- \rightarrow \ell jj\nu$	1.166	1	1	1	1	...

SM background. The cuts **C1**, **C2**, and **C3** are particularly effective in reducing this background. Besides, **C2** also reasonably reduces the two other potentially dominant channels, ZZ and WWZ . **C1** and **C2** are helpful in reducing the $t\bar{t}$ background. Overall, one can achieve a 3σ statistical significance at $\mathcal{L} \approx 30 \text{ fb}^{-1}$ which is a large improvement over the $\sqrt{s} = 250 \text{ GeV}$ analysis.

(2) Final state: $1\mu + 1\tau\text{-jet} + \cancel{E}$:

For the final state $1\mu + 1\tau\text{-jet} + \cancel{E}$ we have used the following kinematical cuts:

- (i) **D0**: In the final state, we demand one muon along with a jet that must be tagged as a τ jet. Any additional leptons and jets in the event including b jets have been vetoed.
- (ii) **D1**: The missing energy distribution is expected to be slightly on the softer side than that in the τ leptonic decay case. The normalized distribution of \cancel{E} has been shown in Fig. 9 for the signal as well as the same SM background channels with similar color coding as in Fig. 5. We demand $1000 \text{ GeV} > \cancel{E} > 500 \text{ GeV}$.
- (iii) **D2**: We demand that the visible invariant mass, that is, the visible mass of the muon and τ -jet system, should lie within the region $130 \text{ GeV} > M_{\mu\tau_{\text{had}}} > 70 \text{ GeV}$ following the distribution in Fig. 10.
- (iv) **D3**: We demand that the visible momentum, that is, the visible momentum of the muon and τ -jet system, should lie within the region $320 \text{ GeV} > p^{\text{vis}} > 20 \text{ GeV}$. Corresponding distribution is shown in Fig. 11.

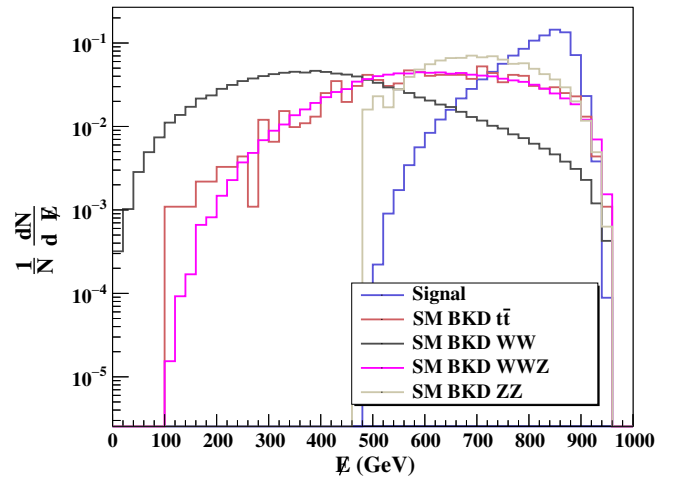


FIG. 9. Normalized \cancel{E} distribution for signal and backgrounds at $\sqrt{s} = 1000 \text{ GeV}$ for final state: $1\mu + 1\tau\text{-jet} + \cancel{E}$.

- (v) **D4**: In our signal events, we expect the missing energy vector $\vec{\cancel{E}}$ to be well separated from this τ jet. We demand $5.5 > \Delta R(\tau\text{-jet}, \vec{\cancel{E}}) > 1.5$. The normalized distribution of $\Delta R(\tau\text{-jet}, \vec{\cancel{E}})$ is shown in Fig. 12.

In Table VIII below we have presented the cut-flow numbers obtained from our collider simulation at $\sqrt{s} = 1000 \text{ GeV}$ and an integrated luminosity of $\mathcal{L} = 500 \text{ fb}^{-1}$ corresponding to our signal $1\mu + 1\tau\text{-jet} + \cancel{E}$ [with $\text{BR}(h \rightarrow \mu\tau) = 9.78 \times 10^{-3}$] as well as the different SM background channels.

It is evident from Table VIII that the dominant SM backgrounds are W^+W^- , ZZ , and W^+W^-Z . However, these contributions are effectively reduced by the cut **D1** and then gradually cut down by the [**D2–D4**]. It is worth noting that for the $e^+e^- \rightarrow \nu_e \bar{\nu}_e h$ production mode, we have used **C3** (for leptonic τ decay) and **D2** (for hadronic τ

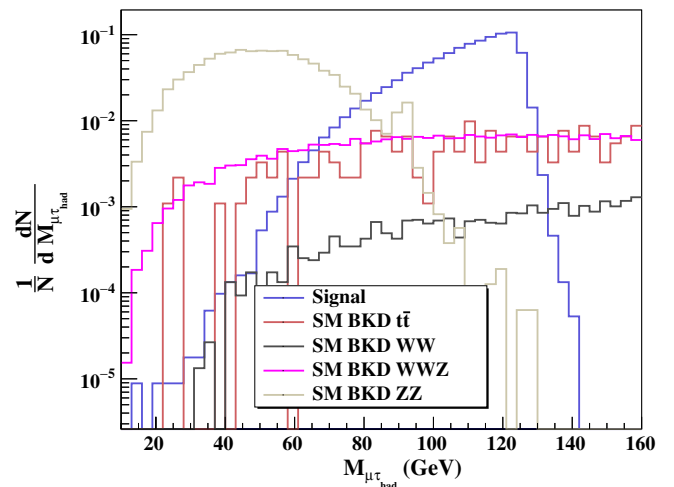


FIG. 10. Normalized $M_{\mu\tau_{\text{had}}}$ distribution for signal and backgrounds at $\sqrt{s} = 1000 \text{ GeV}$ for final state: $1\mu + 1\tau\text{-jet} + \cancel{E}$.

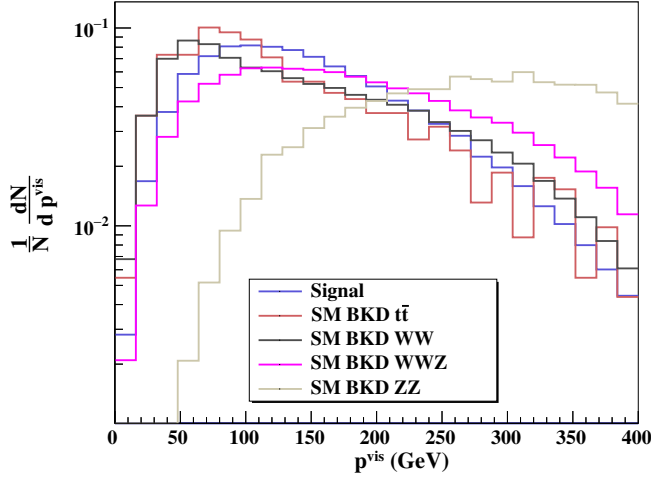


FIG. 11. Normalized p^{vis} distribution for signal and backgrounds at $\sqrt{s} = 1000$ GeV for final state: $1\mu + 1\tau\text{-jet} + \cancel{E}$.

decay) which restrict the visible invariant mass of the two lepton system and $\mu\text{-}\tau\text{-jet}$ system, respectively, and not on the collinear mass, as used for $e^+e^- \rightarrow Zh$ production mode. This is because the collinear mass cannot be constructed whenever there are additional source(s) of missing energy over and above τ decay. As the numbers in Table VIII indicate, a 3σ statistical significance may be obtained at a very low integrated luminosity of 12 fb^{-1} . This still is a slight improvement over what is obtained for the $2\ell + \cancel{E}$ final state.

Hence the $1\mu + 1\tau\text{-jet} + \cancel{E}$ final state at $\sqrt{s} = 1000$ GeV has the potential to probe the smallest $\text{BR}(h \rightarrow \mu\tau)$ ($\sim 10^{-4}$) than all other final states studied so far. The lowest possible branching ratios that can be probed at 3σ statistical significance with the two final states studied at this center-of-mass energy have been shown at three different integrated luminosities in Table IX.

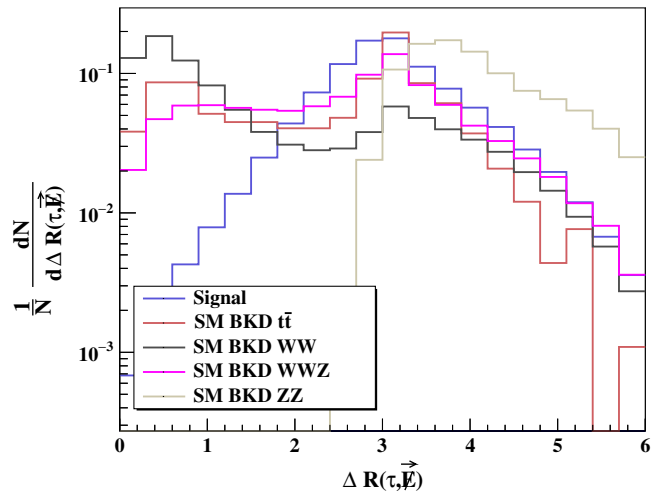


FIG. 12. Normalized $\Delta R(\tau\text{-jet}, \cancel{E})$ distribution for signal and backgrounds at $\sqrt{s} = 1000$ GeV for final state: $1\mu + 1\tau\text{-jet} + \cancel{E}$.

TABLE VIII. Cross sections of the signal and various background channels for hadronic decay of τ are shown in pb alongside the number of expected events for the individual channels at 500 fb^{-1} luminosity after applying each of the cuts **D0–D4** as listed in the text. $\text{NEV} \equiv$ number of events. All the numbers are presented for $\text{BR}(h \rightarrow \mu\tau) = 9.78 \times 10^{-3}$.

Process	σ [pb]	$\sqrt{s} = 1000$ GeV				
		NEV ($\mathcal{L} = 500 \text{ fb}^{-1}$)				
		D0	D1	D2	D3	D4
$e^+e^- \rightarrow \nu_e \bar{\nu}_e h$	2.01×10^{-3}	226	226	221	209	201
$e^+e^- \rightarrow W^+W^-$	0.12714	4778	1413	59	56	48
$e^+e^- \rightarrow \tau^+\tau^-$	1.562×10^{-6}
$e^+e^- \rightarrow t\bar{t}$	0.0153	9	7	1	1	1
$e^+e^- \rightarrow ZZ$	3.188×10^{-3}	25	25	3
$e^+e^- \rightarrow Zh$	1.533×10^{-4}	7	6	2	1	1
$e^+e^- \rightarrow W^+W^-Z$	9.814×10^{-4}	32	24	4	3	3
$e^+e^- \rightarrow ZZZ$	9.51×10^{-6}
$e^+e^- \rightarrow t\bar{t}Z$	4.64×10^{-3}
$e^+e^- \rightarrow ZZh$	3.21×10^{-4}
$e^+e^- \rightarrow \ell j j \nu$	1.166	634	113	1	1	1

Note that the collider analyses presented so far at two different center-of-mass energies have been performed for specific choices of a_Z and a_W . Although the allowed ranges of these parameters are quite constrained as discussed in Sec. III A, it would be interesting to see how the collider reach in terms of the relevant branching ratio varies along their whole allowed ranges. We have depicted this below in Fig. 13.

The red color indicates the 3σ reach of $\text{BR}(h \rightarrow \mu\tau)$ at 350 fb^{-1} and 250 fb^{-1} luminosities at $\sqrt{s} = 250$ GeV and 1000 GeV, respectively. Similarly, the blue and cyan colors indicate the reach of the same at 500 fb^{-1} and 1000 fb^{-1} luminosities at both of the center-of-mass energies. As evident from the plots, the branching ratio does not vary much so as to make any visible changes in the predicted results over the presently allowed regions of a_Z and a_W .

C. Prospects of higher-dimensional operators

As discussed earlier, introducing effective operators may enhance the prospects of probing even smaller $\text{BR}(h \rightarrow \mu\tau)$

TABLE IX. Lowest branching ratio that can be probed with 3σ statistical significance for the two different final states (arising from leptonic and hadronic decay of τ) at $\sqrt{s} = 1000$ GeV. The last column indicates the BR reach when the event rates of these two final states are combined.

$\mathcal{L}(\text{fb}^{-1})$	BR in $(2\ell + \cancel{E})$	BR in $(\mu + \tau_{\text{had}} + \cancel{E})$	Combined BR
250	3.16×10^{-3}	1.58×10^{-3}	1.62×10^{-3}
500	2.15×10^{-3}	1.11×10^{-3}	1.11×10^{-3}
1000	1.44×10^{-3}	7.22×10^{-4}	7.58×10^{-4}

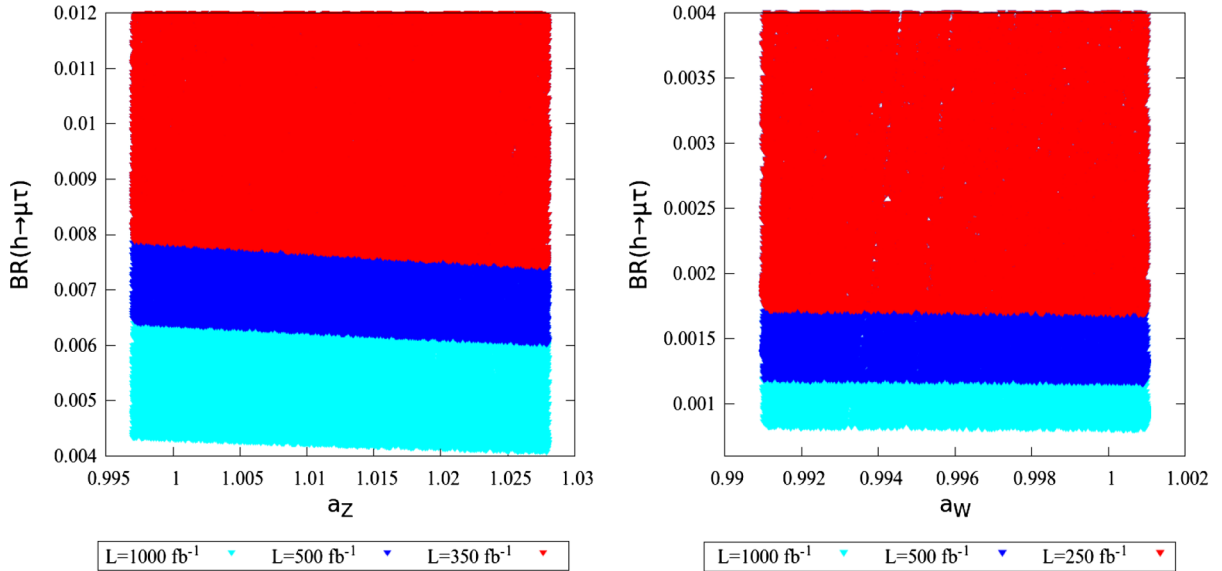


FIG. 13. The 3σ reach of $\text{BR}(h \rightarrow \mu\tau)$ at $\sqrt{s} = 250$ GeV and 1000 GeV over the allowed ranges of a_z and a_W , respectively, at different integrated luminosities.

by enhancing the production cross section of the Higgs boson due to their momentum-dependent Lorentz structures. From Table II it can be seen that all four non-zero f_n 's, i.e., f_W , f_B , f_{WW} , f_{BB} , can modify the hZZ interaction ($g_{hZZ}^{(1)}, g_{hZZ}^{(2)}$). On the other hand, f_W and f_{WW} can modify the hWW interaction. Since the sole purpose of introducing these operators is to assess whether they can improve the reach on smaller $\text{BR}(h \rightarrow \mu\tau)$, we first proceed to study how much enhancement in the Higgs boson production cross section one can expect from the presence of these operators. To determine that, we have used conservative values of f_n 's for our analysis, compared to their maximally allowed values as mentioned in Table III. Non-zero values of f_n 's result in enhancement of the Higgs production cross section and allow us to probe even smaller $\text{BR}(h \rightarrow \mu\tau)$. Higgs production cross sections for some sample values of f_n 's are given in Table X. Less

TABLE X. Production cross sections (σ_{prod}) of Higgs boson at $\sqrt{s} = 250$ GeV and $\sqrt{s} = 1000$ GeV for some sample values of f_n with $\Lambda = 1$ TeV.

Couplings	Values of the couplings	σ_{prod} at $\sqrt{s} = 250$ GeV in pb	σ_{prod} at $\sqrt{s} = 1000$ GeV in pb
f_B	-3.4	0.2514	...
	11.0	0.2329	...
f_{BB}	-2.78	0.2503	...
	0.283	0.2466	...
f_W	-5.8	0.2737	0.1959
	14.5	0.187	0.3059
f_{WW}	-1.86	0.2814	0.2256
	0.5	0.2463	0.2284

conservative, 2σ allowed values of f_n 's as mentioned in Table III would thus indeed improve the reach of the e^+e^- collider in probing the lowest possible branching ratio.

As can be seen from Table X, an enhancement in the $e^+e^- \rightarrow Zh$ production cross section at $\sqrt{s} = 250$ GeV is obtained for a sample value $f_{WW} = -1.86$ (the value of f_{WW} being compatible with electroweak precision observables and signal strengths mentioned earlier), while keeping f_W , f_B , and f_{BB} zero. For the sake of the improvement

TABLE XI. Cross sections of the signal and various background channels for leptonic decay of τ are shown in pb alongside the number of expected events for the individual channels at 500 fb^{-1} luminosity after applying each of the cuts C0–C4 as listed in the text. NEV \equiv number of events. All the numbers are presented for $f_W = 14.0$, $\text{BR}(h \rightarrow \mu\tau) = 9.78 \times 10^{-3}$.

Process	σ [pb]	$\sqrt{s} = 1000$ GeV (with HDO)				
		NEV ($\mathcal{L} = 500 \text{ fb}^{-1}$)				
		C0	C1	C2	C3	C4
$e^+e^- \rightarrow \nu_e \bar{\nu}_e h$	2.691×10^{-3}	276	274	258	250	245
$e^+e^- \rightarrow W^+W^-$	0.12714	19010	2331	266	151	127
$e^+e^- \rightarrow \tau^+\tau^-$	1.562×10^{-6}	1
$e^+e^- \rightarrow t\bar{t}$	0.0153	29	18	5	3	2
$e^+e^- \rightarrow ZZ$	3.188×10^{-3}	339	15	7	3	3
$e^+e^- \rightarrow Zh$	1.533×10^{-4}	4	4	4	2	2
$e^+e^- \rightarrow W^+W^-Z$	2.38×10^{-4}	39	33	28	10	10
$e^+e^- \rightarrow ZZZ$	9.51×10^{-6}	1	1	1	1	1
$e^+e^- \rightarrow t\bar{t}Z$	4.64×10^{-3}
$e^+e^- \rightarrow ZZh$	3.21×10^{-4}
$e^+e^- \rightarrow \ell j j \nu$	1.166	1	1	1	1	...

TABLE XII. Cross sections of the signal and various background channels for hadronic decay of τ are shown in pb alongside the number of expected events for the individual channels at 500 fb^{-1} luminosity after applying each of the cuts **D0–D4** as listed in the text. $\text{NEV} \equiv$ number of events. All the numbers are presented for $f_W = 14.0$, $\text{BR}(h \rightarrow \mu\tau) = 9.78 \times 10^{-3}$.

Process	$\sqrt{s} = 1000 \text{ GeV}$ (with HDO)					
	σ [pb]	NEV ($\mathcal{L} = 500 \text{ fb}^{-1}$)				
		D0	D1	D2	D3	D4
$e^+e^- \rightarrow \nu_e\bar{\nu}_e h$	2.691×10^{-3}	315	315	305	276	267
$e^+e^- \rightarrow W^+W^-$	0.12714	4778	1413	59	56	48
$e^+e^- \rightarrow \tau^+\tau^-$	1.562×10^{-6}
$e^+e^- \rightarrow t\bar{t}$	0.0153	9	7	1	1	1
$e^+e^- \rightarrow ZZ$	3.188×10^{-3}	25	25	3
$e^+e^- \rightarrow Zh$	1.533×10^{-4}	7	6	2	1	1
$e^+e^- \rightarrow W^+W^-Z$	2.38×10^{-4}	8	7	2	2	2
$e^+e^- \rightarrow ZZZ$	9.51×10^{-6}
$e^+e^- \rightarrow t\bar{t}Z$	4.64×10^{-3}
$e^+e^- \rightarrow ZZh$	3.21×10^{-4}
$e^+e^- \rightarrow \ell jj\nu$	1.166	634	113	1	1	1

of results, we have narrowed down the collinear mass cut [**A3**, **B3**] (mentioned earlier) a little and varied M_{coll} as $(m_h + 12) \text{ GeV} > M_{\text{coll}} > (m_h - 12) \text{ GeV}$. However, the enhancement can be at most by a factor ≈ 1.10 , which is not enough to increase the signal significance sufficiently so as to improve upon our results obtained for $\sqrt{s} = 1000 \text{ GeV}$ analysis.³ Similarly for the $e^+e^- \rightarrow \nu_e\bar{\nu}_e h$ production channel, an enhancement in the cross section is obtained for the sample value $f_W = 14.5$ keeping all the other f_n 's zero at $\sqrt{s} = 1000 \text{ GeV}$. We have subsequently carried a detailed simulation for this case. The basic and selection cuts ([**C0–C4**] and [**D0–D4**]) are the same as before. The results are presented in Tables **XI** and **XII** for the final states $2\ell + \cancel{E}$ and $1\mu + 1\tau\text{-jet} + \cancel{E}$, respectively.

The signal and backgrounds will remain the same as before. At $\sqrt{s} = 1000 \text{ GeV}$, the signal cross section increases from $2.01 \times 10^{-3} \text{ pb}$ (earlier scenario) to $2.691 \times 10^{-3} \text{ pb}$, and all the background cross sections except W^+W^-Z remain unaltered as can be seen from Tables **XI** and **XII**. The numbers are presented for $\mathcal{L} = 500 \text{ fb}^{-1}$ and $\text{BR}(h \rightarrow \mu\tau) = 9.78 \times 10^{-3}$ as before.

Table **XIII** shows slight improvement in probing $\text{BR}(h \rightarrow \mu\tau)$. The combined result from the two channels gives the best reach of the branching ratio ($\approx 5.83 \times 10^{-4}$),

³Our analysis reveals that the combination of the two final states at $\sqrt{s} = 250 \text{ GeV}$ with an integrated luminosity of 1000 fb^{-1} results in a reach of $\text{BR}(h \rightarrow \mu\tau) \approx 2.69 \times 10^{-3}$ which is barely smaller by a factor of ≈ 2 compared to that obtained in the absence of f_{WW} .

TABLE XIII. Lowest branching ratio that can be probed with 3σ statistical significance for the two different final states (arising from leptonic and hadronic decay of τ) at $\sqrt{s} = 1000 \text{ GeV}$ with $f_W = 14.0$. The last column indicates the BR reach when the event rates of these two final states are combined.

$\mathcal{L}(\text{fb}^{-1})$	BR in $(2\ell + \cancel{E})$	BR in $(\mu + \tau_{\text{had}} + \cancel{E})$	Combined BR
250	2.15×10^{-3}	1.23×10^{-3}	1.19×10^{-3}
500	1.49×10^{-3}	8.51×10^{-4}	8.33×10^{-4}
1000	1.05×10^{-3}	5.91×10^{-4}	5.83×10^{-4}

which is an improvement by a factor of ≈ 1.24 over that obtained in the absence of f_{WW} , and it is the best reach obtained at the e^+e^- collider at 1000 GeV .

It can therefore be concluded that at $\sqrt{s} = 1000 \text{ GeV}$ and $\mathcal{L} = 1000 \text{ fb}^{-1}$, the e^+e^- collider provides at least 2 orders of magnitude improvement in probing the $h \rightarrow \mu\tau$ branching ratio as compared to the existing limits at LHC. It is because of its relatively clean environment. At $\sqrt{s} = 1000 \text{ GeV}$, the number of signals surviving is much larger than the number of total backgrounds after applying all the cuts. This enhances the signal significance and 3σ significance is achieved at very low luminosity for the fixed value of $\text{BR}(h \rightarrow \mu\tau) = 9.78 \times 10^{-3}$. Thus the branching ratio as small as $\sim 10^{-4}$ can be probed by enhancing the integrated luminosity.

V. SUMMARY AND CONCLUSIONS

The objective of this work was to study the collider aspects of one of these possible non-standard decay modes, namely, $h \rightarrow \mu\tau$, and examine the possible reach of the corresponding branching ratio at future e^+e^- colliders. Collider simulation has been performed at $\sqrt{s} = 250 \text{ GeV}$ and 1000 GeV at three projected integrated luminosities, i.e., $\mathcal{L} = 350(250) \text{ fb}^{-1}$, 500 fb^{-1} , 1000 fb^{-1} . We have explored different possible final states arising from both leptonic and hadronic decays of the τ . We have looked for the smallest possible $\text{BR}(h \rightarrow \mu\tau)$ that can be probed at the 3σ level. We have also combined the event rates of different possible final states at the same center-of-mass energy to improve the reach. Two different scenarios have been considered separately for this purpose, with two different types of modifications at the production level of Higgs boson. The first scenario includes modification of the hVV interaction with multiplicative factors only (achieved by scaling the vertex factor), whereas effective operators with new Lorentz structures have been introduced in the second scenario. While introducing the effective operators, we have chosen the effective couplings (f_n) in a somewhat conservative manner, though the production cross section of the Higgs boson gets enhanced. In principle, one can also use the values of f_n 's (allowed by the 2σ constraints), which could lead to a larger production cross section and would be useful in probing even lower branching ratios.

At $\sqrt{s} = 250$ GeV, $e^+e^- \rightarrow Zh$ is the main production mode of the Higgs boson. The lowest branching ratio that can be probed at the 3σ level is $\approx 4.09 \times 10^{-3}$ at an integrated luminosity, $\mathcal{L} = 1000$ fb $^{-1}$. The result improves slightly after including the effective operators instead of simply scaling the hVV vertices, though the order of magnitude of the lowest detectable branching ratio remains the same.

At $\sqrt{s} = 1000$ GeV, the reach of $\text{BR}(h \rightarrow \mu\tau)$ is much better owing to the large Higgs production cross section in the $e^+e^- \rightarrow h\nu_e\bar{\nu}_e$ mode. Combining the signal rates in the two aforementioned final states at this center-of-mass energy, one can probe $\text{BR}(h \rightarrow \mu\tau)$ down to $\approx 5.83 \times 10^{-4}$ with a 3σ statistical significance at $\mathcal{L} = 1000$ fb $^{-1}$. This is the best reach so far, which an e^+e^- collider can achieve,

and is smaller by nearly 2 orders of magnitude than what is obtained from the latest LHC data.

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