**p-p, p-Λ, and Λ-Λ correlations studied via femtoscopy in pp reactions at √s = 7 TeV**

S. Acharya et al.*
(ALICE Collaboration)

(Received 29 June 2018; revised manuscript received 19 November 2018; published 13 February 2019)

We report on the first femtoscopic measurement of baryon pairs, such as p-p, p-Λ, and Λ-Λ, measured by ALICE at the Large Hadron Collider (LHC) in proton-proton collisions at √s = 7 TeV. This study demonstrates the feasibility of such measurements in pp collisions at ultrarelativistic energies. The femtoscopy method is employed to constrain the hyperon-nucleon and hyperon-hyperon interactions, which are still rather poorly understood. A new method to evaluate the influence of residual correlations induced by the decays of resonances and experimental impurities is hereby presented. The p-p, p-Λ, and Λ-Λ correlation functions were fitted simultaneously with the help of a new tool developed specifically for the femtoscopy analysis in small colliding systems: Correlation Analysis Tool using the Schrödinger equation (CATS). Within the assumption that in pp collisions the three particle pairs originate from a common source, its radius is found to be equal to r0 = 1.125 ± 0.018 (stat) ±0.058 (syst) fm. The sensitivity of the measured p-Λ correlation is tested against different scattering parameters, which are defined by the interaction among the two particles, but the statistics is not sufficient yet to discriminate among different models. The measurement of the Λ-Λ correlation function constrains the phase space spanned by the effective range and scattering length of the strong interaction. Discrepancies between the measured scattering parameters and the resulting correlation functions at LHC and RHIC energies are discussed in the context of various models.

DOI: 10.1103/PhysRevC.99.024001

I. INTRODUCTION

Traditionally femtoscopy is used in heavy-ion collisions at ultrarelativistic energies to investigate the spatial-temporal evolution of the particle emitting source created during the collision [1,2]. Assuming that the interaction for the employed particles is known, a detailed study of the geometrical extension of the emission region becomes possible [3–10].

If one considers smaller colliding systems such as proton-proton (pp) at TeV energies and assumes that the particle emitting source does not show a strong time dependence, one can reverse the paradigm and exploit femtoscopy to study the final-state interaction (FSI). This is especially interesting in the case where the interaction strength is not well known as for hyperon-nucleon (Y-N) and hyperon-hyperon (Y-Y) pairs [11–19]. Hyperon-nucleon and hyperon-hyperon interactions are still rather poorly experimentally constrained and a detailed knowledge of these interactions is necessary to understand quantitatively the strangeness sector in the low-energy regime of quantum-chromodynamics (QCD) [20].

Hyperon-nucleon (p-Λ and p-Σ) scattering experiments have been carried out in the 1960s [21–23] and the measured cross sections have been used to extract scattering lengths and effective ranges for the strong nuclear potential by means of effective models such as the extended-soft-core (ESC08) baryon-baryon model [24] or by means of chiral effective field theory (χEFT) approaches at leading order (LO) [25] and next-to-leading order (NLO) [26]. The results obtained from the above-mentioned models are rather different, but all confirm the attractiveness of the Λ-nucleon (Λ-N) interaction for low hyperon momenta. In contrast to the LO results, the NLO solution claims the presence of a negative phase shift in the p-Λ spin singlet channel for Λ momenta larger than p_Λ > 600 MeV/c. This translates into a repulsive core for the strong interaction evident at small relative distances. The same repulsive interaction is obtained in the p-wave channel within the ESC08 model [24].

The existence of hypernuclei [27] confirms that the N-Λ is attractive within nuclear matter for densities below nuclear saturation ρ0 = 0.16 fm⁻³. An average value of U(ρ = ρ0, k = 0) ≈ −30 MeV [27], with k the hyperon momentum in the laboratory reference system, is extracted from hypernuclear data on the basis of a dispersion relation for hyperons in a baryonic medium at ρ0.

The situation for the Σ hyperon is currently rather unclear. There are some experimental indications for the formation of Σ hypernuclei [28,29] but different theoretical approaches predict both attractive and repulsive interactions depending on the isospin state and partial wave [24,26,30]. The scarce experimental data for this hypernucleus prevents any validation of the models.

A Σ-hypernucleus candidate was detected [31] and ongoing measurements suggest that the N-Σ interaction is weakly attractive [32]. A recent work by the Lattice HAL-QCD...
The femtoscopy technique was employed by the STAR Collaboration to study $\Lambda$-$\Lambda$ correlations in Au-Au collisions at $\sqrt{s_{\text{NN}}} = 200$ GeV [16]. First a shallow repulsive interaction was reported for the $\Lambda$-$\Lambda$ system, but in an alternative analysis, where the residual correlations were treated more accurately [38], a shallow attractive interaction was confirmed. These analyses demonstrate the limitations of such measurements in heavy-ion collisions, where the source parameters are time dependent and the emission time might not be the same for all hadron species.

The need for more experimental data to study the hyperon-nucleon, hyperon-hyperon, and even the hyperon-nucleon-nucleon interaction has become more crucial in recent years due to its connection to the modeling of astrophysical objects such as neutron stars [39–42]. In the inner core of these objects the appearance of hyperons is a possible scenario since their creation at finite density becomes energetically favored in comparison with a purely neutron matter composition [41]. However, the appearance of these additional degrees of freedom leads to a softening of the nuclear matter equation of state (EOS) [43] making the EOS incompatible with the observation of neutron stars as heavy as two solar masses [44,45]. This goes under the name of the hyperon puzzle. Many attempts were made to solve this puzzle, e.g., by introducing three-body forces for $\Lambda$NN leading to an additional repulsion that can counterbalance the large gravitational pressure and finally allow for larger neutron star masses [46–49]. A repulsive core for the two-body forces would also stiffen the EOS containing hyperons. In order to constrain the parameter space of such models a detailed knowledge of the hyperon-nucleon, including $\Sigma$ and $\Xi$ states, and of the hyperon-nucleon-nucleon interaction is mandatory.

A detailed description of the ALICE detector and its performance in the LHC Run 1 (2009-2013) is given in Refs. [54,55]. The inner tracking system (ITS) [54] consists of six cylindrical layers of high-resolution silicon detectors placed radially between 3.9 and 43 cm around the beam pipe. The two innermost layers are silicon pixel detectors (SPD) and cover the pseudorapidity range $|\eta| < 2$. The time projection chamber (TPC) [56] provides full azimuthal coverage and allows charged particle reconstruction and identification (PID) via the measurement of the specific ionization energy loss $dE/dx$ in the pseudorapidity range $|\eta| < 0.9$. The time-of-flight (TOF) [57] detector consists of multigap resistive plate chambers covering the full azimuthal angle in $|\eta| < 0.9$. The PID is obtained by measuring the particle’s velocity $\beta$. The above-mentioned detectors are immersed in a $B = 0.5$ T solenoidal magnetic field directed along the beam axis. The V0 are small-angle plastic scintillator detectors used for triggering and placed on either side of the collision vertex along the beam line at $+3.3$ m and $-0.9$ m from the nominal interaction point, covering the pseudorapidity ranges $2.8 < \eta < 5.1$ (V0-A) and $-3.7 < \eta < -1.7$ (V0-C).

II. DATA ANALYSIS

In this paper we present results from studies of the $p-p$, $p-\Lambda$, and $\Lambda-\Lambda$ correlations in $pp$ collisions at $\sqrt{s} = 7$ TeV employing the data collected by ALICE in 2010 during the LHC Run 1. Approximately $3.4 \times 10^8$ minimum bias events have been used for the analysis, before event and track selection. A detailed description of the ALICE detector and its performance in the LHC Run 1 (2009-2013) is given in Refs. [54,55]. The inner tracking system (ITS) [54] consists of six cylindrical layers of high-resolution silicon detectors placed radially between 3.9 and 43 cm around the beam pipe. The two innermost layers are silicon pixel detectors (SPD) and cover the pseudorapidity range $|\eta| < 2$. The time projection chamber (TPC) [56] provides full azimuthal coverage and allows charged particle reconstruction and identification (PID) via the measurement of the specific ionization energy loss $dE/dx$ in the pseudorapidity range $|\eta| < 0.9$. The time-of-flight (TOF) [57] detector consists of multigap resistive plate chambers covering the full azimuthal angle in $|\eta| < 0.9$. The PID is obtained by measuring the particle’s velocity $\beta$. The above-mentioned detectors are immersed in a $B = 0.5$ T solenoidal magnetic field directed along the beam axis. The V0 are small-angle plastic scintillator detectors used for triggering and placed on either side of the collision vertex along the beam line at $+3.3$ m and $-0.9$ m from the nominal interaction point, covering the pseudorapidity ranges $2.8 < \eta < 5.1$ (V0-A) and $-3.7 < \eta < -1.7$ (V0-C).

A. Event selection

The minimum bias interaction trigger requires at least two out of the following three conditions: two pixel chips hit in the outer layer of the silicon pixel detectors, a signal in V0-A, a signal in V0-C [55]. Reconstructed events are required to have at least two associated tracks and the distance along the beam axis between the reconstructed primary vertex and the nominal interaction point should be smaller than 10 cm. Events with multiple reconstructed SPD vertices are considered as pileup. In addition, background events are rejected using the correlation between the number of SPD clusters and the tracklet multiplicity. The tracklets are constrained to the primary vertex, and hence a typical background event is characterized by a large amount of SPD clusters but only few tracklets, while a pileup event contains a larger number of
clusters at the same tracklet multiplicity. After application of these selection criteria, about $2.5 \times 10^8$ events are available for the analysis.

### B. Proton candidate selection

To ensure a high-purity sample of protons, strict selection criteria are imposed on the tracks. Only particle tracks reconstructed with the TPC without additional matching with hits in the ITS are considered in the analysis in order to avoid biases introduced by the nonuniform acceptance in the ITS. However, the track fitting is constrained by the independently reconstructed primary vertex. Hence, the obtained momentum resolution is comparable to that of globally reconstructed tracks, as demonstrated in Ref. [55].

The selection criteria for the proton candidates are summarized in Table I. The selection on the number of reconstructed TPC clusters serves to ensure the quality of the track, to assure a good $p_T$ resolution at large momenta and to remove fake tracks from the sample. To enhance the number of protons produced at the primary vertex, a selection is imposed on the distance of closest approach (DCA) in both beam ($z$) and transverse ($xy$) directions. In order to minimize the fraction of protons originating from the interaction of primary particles with the detector material, a low transverse momentum cutoff is applied [58]. At high $p_T$ a cutoff is introduced to ensure the purity of the proton sample, as the purity drops below 80% for larger $p_T$ due to the decreasing separation power of the combined TPC and TOF particle identification.

For particle identification both the TPC and the TOF detectors are employed. For low momenta ($p < 0.75$ GeV/c) only the PID selection from the TPC is applied, while for larger momenta the information of both detectors is combined since the TPC does not provide a sufficient separation power in this momentum region. The combination of TPC and TOF signals is done by employing a circular selection criterion $p_T > 0.3$ GeV/c and a $\eta$ rejection $|\eta| < 0.8$. The purity of the proton sample, the $n_{\pi,}\text{combined}$ value found to be smaller, the proton hypothesis and thus the track is rejected. With these selection criteria a $p_T$-averaged proton purity of 99% is achieved. The purity remains above 99% for $p_T < 2$ GeV/c and then decreases to 80% at the momentum cutoff of 4.05 GeV/c.

### C. $\Lambda$ candidate selection

The weak decay $\Lambda \rightarrow p\pi^-$ (BR = 63.9%, $c\tau = 7.3$ cm [59]) is exploited for the reconstruction of the $\Lambda$ candidate, and accordingly the charge-conjugate decay for the $\bar{\Lambda}$ identification. The reconstruction method forms so-called $V_0$ decay candidates from two charged particle tracks using a procedure described in Ref. [60]. The selection criteria for

---

**TABLE I. Proton (top) and $\Lambda$ candidate (bottom) selection criteria.**

<table>
<thead>
<tr>
<th>Selection criterion</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Proton selection criteria</td>
<td></td>
</tr>
<tr>
<td>Pseudorapidity</td>
<td>$</td>
</tr>
<tr>
<td>Transverse momentum</td>
<td>$0.5 &lt; p_T &lt; 4.05$ GeV/c $n_{\text{TPC}} &gt; 80$</td>
</tr>
<tr>
<td>TPC clusters</td>
<td></td>
</tr>
<tr>
<td>Crossed TPC pad rows</td>
<td>$n_{\text{crossed}} &gt; 70$ (out of 159)</td>
</tr>
<tr>
<td>Findable TPC clusters</td>
<td>$n_{\text{crossed}}/n_{\text{findable}} &gt; 0.83$</td>
</tr>
<tr>
<td>Tracks with shared TPC clusters</td>
<td>Rejected</td>
</tr>
<tr>
<td>Distance of closest approach $xy$</td>
<td>$</td>
</tr>
<tr>
<td>Distance of closest approach $z$</td>
<td>$</td>
</tr>
<tr>
<td>Particle identification</td>
<td></td>
</tr>
<tr>
<td>$n_{\sigma,\text{TPC}}$</td>
<td>$&lt; 3$ for $p &lt; 0.75$ GeV/c</td>
</tr>
<tr>
<td>$n_{\sigma,\text{combined}}$</td>
<td>$&lt; 3$ for $p &gt; 0.75$ GeV/c</td>
</tr>
<tr>
<td>Lambda selection criteria</td>
<td></td>
</tr>
<tr>
<td>Daughter track selection criteria</td>
<td></td>
</tr>
<tr>
<td>Pseudorapidity</td>
<td>$</td>
</tr>
<tr>
<td>TPC clusters</td>
<td>$n_{\text{TPC}} &gt; 70$</td>
</tr>
<tr>
<td>Distance of closest approach</td>
<td>$\text{DCA} &gt; 0.05$ cm</td>
</tr>
<tr>
<td>Particle identification</td>
<td>$</td>
</tr>
<tr>
<td>$V_0$ selection criteria</td>
<td></td>
</tr>
<tr>
<td>Transverse momentum</td>
<td>$p_T &gt; 0.3$ GeV/c</td>
</tr>
<tr>
<td>$</td>
<td>\text{DCA}_{xy,i}</td>
</tr>
<tr>
<td>Transverse radius of the decay vertex $r_{xy}$</td>
<td>$0.2 &lt; r_{xy} &lt; 100$ cm</td>
</tr>
<tr>
<td>DCA of the daughter tracks at the decay vertex</td>
<td>$\text{DCA}(p, \pi) &lt; 1.5$ cm</td>
</tr>
<tr>
<td>Pointing angle $\alpha$</td>
<td>$\cos \alpha &gt; 0.99$</td>
</tr>
<tr>
<td>$K^0$ rejection</td>
<td>$0.48 &lt; M_{\pi^+\pi^-} &lt; 0.515$ GeV/c$^2$</td>
</tr>
<tr>
<td>$\Lambda$ selection</td>
<td>$</td>
</tr>
</tbody>
</table>
the Λ candidates are summarized in Table I. The V_0 daughter tracks are globally reconstructed tracks and, in order to maximize the efficiency, selected by a broad particle identification cut employing the TPC information only. Additionally, the daughter tracks are selected by requiring a minimum impact parameter of the tracks with respect to the primary vertex. After the selection all positively charged daughter tracks are combined with a negatively charged partner to form a pair. The resulting Λ vertex \( l_{\text{vertex}, i} = x, y, z \) is then defined as the point of closest approach between the two daughter tracks. This distance of closest approach of the two daughter tracks with respect to the Λ decay vertex DCA(\( |p, \pi \)) is used as an additional quality criterion of the Λ candidate.

The Λ momentum is calculated as the sum of the daughter momenta. A minimum transverse momentum requirement on the Λ candidate is applied to reduce the contribution of fake candidates. Finally, a selection is applied on the opening angle \( \alpha \) between the Λ momentum and the vector pointing from the primary vertex to the secondary V_0 decay vertex. The rather broad PID selection of the daughter tracks introduces a residual pion contamination of the proton daughter sample. In order to emulate the combinatorial background, the obtained values are divided by the product of the corresponding single-particle probabilities

\[
C(p_1, p_2) = \frac{P(p_1, p_2)}{P(p_1) \cdot P(p_2)}.
\]

(1)

These probabilities are directly related to the inclusive Lorentz invariant spectra \( P(p_1, p_2) = E_1 E_2 d^3N / p_1 d^3p_2 \) and \( P(p_1, 2) = E_1 E_2 d^3N / p_1 d^3p_2 \). In absence of a correlation signal the value of \( C(p_1, p_2) \) equals unity.

Approximating the emission process and the momenta of the particles, the size of the particle emitting source can be studied. Following [2], Eq. (1) can then be rewritten as

\[
C(k^*) = \int d^3r^* S(r^*) |\psi(r^*, k^*)|^2.
\]

(2)

where \( k^* \) is the relative momentum of the pair defined as \( k^* = \frac{1}{2} \cdot |p_1^* - p_2^*| \), with \( p_1^* \) and \( p_2^* \) the momenta of the two particles in the pair rest frame (PRF, denoted by the *), \( S(r^*) \) contains the distribution of the relative distance of particle pairs in the pair rest frame, the so-called source function, and \( \psi(r^*, k^*) \) denotes the relative wave function of the particle pair. The latter contains the particle interaction term and determines the shape of the correlation function. In this work, the \( p-p \) correlation function, which is theoretically well understood, is employed to obtain the required information about the source function and this information will be used to study the \( p-\Lambda \) and \( \Lambda-\Lambda \) interaction.

In order to relate the correlation function to experimentally accessible quantities, Eq. (1) is reformulated [2] as

\[
C(k^*) = \mathcal{N} \frac{A(k^*)}{B(k^*)}.
\]

(3)

The distribution of particle pairs from the same event is denoted with \( A(k^*) \) and \( B(k^*) \) is a reference sample of uncorrelated pairs. The latter is obtained using event mixing techniques, in which the particle pairs of interest are combined from single particles from different events. To avoid acceptance effects of the detector system, the mixing procedure is conducted only between particle pairs stemming from events with similar \( z \) position of the primary vertex and similar multiplicity [2]. The normalization parameter for mixed and same event yields \( \mathcal{N} \) is chosen such that the mean value of the correlation function equals unity for \( k^* \in [0.2, 0.4] \) GeV/c.

As correlation functions of all studied baryon-baryon pairs, i.e., \( p-p, p-\Lambda, \) and \( \Lambda-\Lambda, \) exhibit identical behavior compared to background ratio of 20 and 25 at a

![FIG. 1. Invariant mass distribution of \( p\pi^- (\pi\pi^+) \) to obtain the \( \Lambda(\bar{\Lambda}) \) signal. The dashed lines set the selection width used in the analysis.](image)
to those of their respective antibaryon-antibaryon pairs, the corresponding samples are combined to enhance the statistical significance. Therefore, in the following \( p-p \) denotes the combination of \( p-p \oplus \bar{p}-\bar{p} \), and accordingly for \( p-\Lambda \) and \( \Lambda-\Lambda \).

### A. Decomposition of the correlation function

The experimental determination of the correlation function is distorted by two distinct mechanisms. The sample of genuine particle pairs includes misidentified particles and feed-down particles from strong and weak decays.

In this work a new method to separate all the individual components contributing to a measured correlation signal is proposed. The correlation functions arising from resonances or impurities of the sample are weighted with the so-called \( \lambda \) parameters and in this way are taken into account in the total correlation function of interest

\[
C(k^*) = 1 + \lambda_{\text{genuine}} \cdot [C_{\text{genuine}}(k^*) - 1] \\
+ \sum_{ij} \lambda_{ij} [C_{ij}(k^*) - 1],
\]

where the \( i, j \) denote all possible impurity and feed-down contributions. These \( \lambda \) parameters can be obtained employing exclusively single-particle properties such as the purity and feed-down probability. The underlying mathematical formalism is outlined in the Appendix.

For the case of \( p-p \) correlation the following contributions must be taken into account:

\[
\{pp\} = pp + p\Lambda p + p\Lambda \Lambda + p\Sigma^+ p + p\Sigma^+ \Sigma^+ + p\Lambda p\Sigma^+ + p\bar{p} + p\bar{p}\Lambda + p\bar{p}\Sigma^+ + p\bar{p}.
\]

where \( \bar{X} \) refers to misidentified particles of species \( X \). \( p\Lambda \), and \( p\Sigma^+ \) correspond to protons stemming from the weak decay of the corresponding hyperons. The \( \Sigma \to \Lambda \pi \to p\pi \pi \) decays are explicitly considered in the feed-down contribution of the \( p-\Lambda \) correlation and hence are omitted in Eq. (5) to avoid double counting. As shown in Appendix, the fraction of primary protons and their feed-down fractions are required to calculate the \( \lambda \) parameters of the different contributions to Eq. (5). The information about the origin of the protons, i.e., whether the particles are of primary origin, originating from feed down or from the interactions with the detector material, is obtained by fitting Monte Carlo (MC) templates to the experimental distributions of the distance of closest approach of the track to the primary vertex. The MC templates and the purity are extracted from \textsc{pythia} [61] simulations using the Perugia 2011 tune [62], which were filtered through the ALICE detector and the reconstruction algorithm [54]. The \( p_T \) averages are then calculated by weighting the quantities of interest by the respective particle yields \( dN/dp_T \). The resulting fraction of primary protons averaged over \( p_T \) is 87% (where in this fraction we also include the protons stemming from strong decays of broad resonances), with the other 13% of the total yield associated to weak decays of resonances and the contribution from the detector material is found to be negligible.

The feed down from weakly decaying resonances is evaluated by using cross sections from \textsc{pythia} and for the proton sample consists of the \( \Lambda \) (70%) and \( \Sigma^+ \) (30%) contributions. The individual contributions to the total correlation function are presented in Table II.

The decomposition of the \( p-\Lambda \) correlation function is conducted in a similar manner as for the \( p-p \) pair, however,
considering the purities and feed-down fractions of both particles
\[ \{p\Lambda\} = p\Lambda + p\Lambda + p\Lambda + p\Lambda + p\Lambda + p\Lambda + p\Lambda + p\Lambda + p\Lambda + p\Lambda + p\Lambda + p\Lambda + p\Lambda + p\Lambda.
\]
The \( \Lambda \) purity is obtained from fits to the invariant mass spectra in eight bins of \( p_T \) and defined as \( S/(S + B) \), where \( S \) denotes the actual signal and \( B \) the background. The feed-down contribution is determined from MC template fits of the experimental distributions of the cosine pointing angle, in which a total of four templates are considered corresponding to direct, feed-down, material, and impurity contributions. The production probability \( dN/dp_T \) is employed in order to obtain \( p_T \) weighted average values.

Around 73\% of the \( \Lambda s \) are primaries (where in this fraction we also include the \( \Lambda \) stemming from strong decays of broad resonances) and 23\% originate from weakly decaying resonances, which is in line with the values quoted in Ref. [63]. The remaining yield is associated to combinatorial background and \( \Lambda s \) produced in the detector material. The main contribution to the feed-down fraction is expected to originate from the \( \Sigma \) states with no preference for the neutral or the charged, respectively. This hypothesis is supported by PYTHIA simulations where the secondary \( \Lambda s \) arise from the weak decay of the \( \Sigma^0 \) (48\%) and \( \Sigma^- \) (49\%) resonances. The remaining contribution in the simulation arises from the \( \Sigma^+ \), which, however, is treated separately. Since the latter decays electromagnetically almost exclusively into \( \Lambda \gamma \) [59], it has a very short life time and cannot be experimentally differentiated from the sample of primary \( \Lambda s \). Measurements of the ratio \( R_{\Sigma^+/\Lambda} = \sigma_{\Sigma^0}/\sigma_{\Lambda} \) have obtained values around 1/3 [64–67], however, with large uncertainties for hadronic collisions at high energies. For lack of better estimates the value of 1/3 is used in the following. The resulting \( \lambda \) parameters for the \( p-\Lambda \) pair are shown in Table II.

For the \( \Lambda-\Lambda \) correlation function the following pair contributions are taken into account:
\[ \{\Lambda\Lambda\} = \Lambda\Lambda + \Lambda\Lambda + \Lambda\Lambda + \Lambda\Lambda + \Lambda\Lambda + \Lambda\Lambda + \Lambda\Lambda + \Lambda\Lambda + \Lambda\Lambda + \Lambda\Lambda + \Lambda\Lambda + \Lambda\Lambda + \Lambda\Lambda + \Lambda\Lambda.
\]
The resulting \( \lambda \) parameters are shown in Table II. Notable is that the actual pair of interest contributes only to about one-third of the signal, while pair fractions involving in particular \( \Sigma^0 \) and \( \Xi^- \) give a significant contribution. The statistical uncertainties of these parameters are negligible and their influence on the systematic uncertainties will be evaluated in Sec. IV.

Possible effects that were considered in this analysis and that could be influencing the source are either the decay of strong resonances, or a \( m_T \) scaling. The latter is related to collective effects and may result in a non-Gaussian behavior of the source. The \( p-p \) correlation function is here considered as a benchmark since the theoretical description of the interaction is well established. The good agreement between the \( m_T \) integrated data and the femtoscopic fit demonstrates that the assumption of a Gaussian source is pertinent. A comparison of the \( m_T \) distribution for \( p-p \) and \( p-\Lambda \) pairs shows a good agreement between the two. The limited experimental sample, however, does not allow conducting a differential analysis yet.

Additionally, we have considered the effect of the strong decays such as \( \Delta \to N + \pi \) and \( N^* \to \Lambda + K \) on the production of protons and \( \Lambda \). Since the \( \Delta \) and \( N^* \) resonances have typical widths above 120 MeV the decay length is in the order of 1 fm so that the decay particles do still experience the final-state interaction with the neighboring particles as the primaries do. We estimate that about 65\% of all primary protons and \( \Lambda \) stem from the strong decay of resonances [68] and we have simulated how the source could be modified by such effects. A difference of 5\% in the results of the Gaussian fit is found when comparing \( p-p \) to \( p-\Lambda \) pairs. These effects are in the same order of the present uncertainty on the radius and are herewith neglected. A quantitative study including all resonances is planned in the analysis of the LHC Run 2 sample.

B. Detector effects

The shape of the experimentally determined correlation function is affected by the finite momentum resolution. This is taken into account when the experimental data are compared to model calculations in the fitting procedure by transforming the modeled correlation function, see Eq. (15), to the reconstructed momentum basis.

When tracks of particle pairs involved in the correlation function are almost collinear, i.e., have a low \( k^* \), detector effects can affect the measurement. No hint for track merging or splitting is found and therefore no explicit selection criteria are introduced.

C. Nonfemtoscopic background

For sufficiently large relative momenta \( (k^* > 200 \text{ MeV}/c) \) and increasing separation distance, the FSI among the particles is suppressed and hence the correlation function should approach unity. As shown in Fig. 2, however, the measured correlation function for \( p-p \) and \( p-\Lambda \) exhibits an increase for \( k^* \) larger than about 200 MeV/c for the two systems. Such nonfemtoscopic effects, probably due to energy-momentum conservation, are in general more pronounced in small colliding systems where the average particle multiplicity is low [2]. In the case of meson-meson correlations at ultrarelativistic energies, the appearance of long-range structures in the correlation functions for moderately small \( k^* \) \( (k^* < 200 \text{ MeV}/c) \) is typically interpreted as originating from minijetlike structures [50,69].

PYTHIA also shows the same nonfemtoscopic correlation for larger \( k^* \) but fails to reproduce quantitatively the behavior shown in Fig. 2, as already observed for the angular correlation of baryon-baryon and antibaryon-antibaryon pairs [58].

Energy-momentum conservation leads to a contribution to the signal, which can be reproduced with a formalism described in Ref. [70] and is accordingly also considered in
this work. Therefore, a linear function \( C(k^*)_{\text{nonfemto}} = ak^* + b \) where \( a, b \) are fit parameters, is included to the global fit as \( C(k^*) = C(k^*)_{\text{femto}} \times C(k^*)_{\text{nonfemto}} \) to improve the description of the signal by the femtoscopic model. The fit parameters of the baseline function are obtained in \( k^* \in [0.3, 0.5] \text{ GeV/c} \) for \( p-p \) and \( p-\Lambda \) pairs. For the case of the \( \Lambda-\Lambda \) correlation function, the uncertainties of the data do not allow to additionally add a baseline, which is therefore omitted in the femtoscopic fit.

**D. Modeling the correlation function**

1. *Genuine correlation function*

For the \( p-p \) correlation function the Coulomb and the strong interaction as well as the antisymmetrization of the wave functions are considered [71]. The strong interaction part of the potential is modeled employing the Argonne \( v_{18} \) potential considering the \( s \) and \( p \) waves. The source is assumed to be isotropic with a Gaussian profile of radius \( r_0 \). The resulting Schrödinger equation is then solved with the CATS [53].

In the case of \( p-\Lambda \) and \( \Lambda-\Lambda \) we employ the Lednický and Lyuboshitz analytical model [72] to describe these correlation functions. This model is based on the assumption of an isotropic source with Gaussian profile

\[
S(r_0) = \frac{1}{(4\pi r_0^2)^{3/2}} \exp\left(-\frac{r^2}{4r_0^2}\right),
\]

where \( r_0 \) is the size of the source. Additionally, the complex scattering amplitude is evaluated by means of the effective range approximation

\[
f(k^*)^S = \left(\frac{1}{f_0^S} + \frac{1}{2} d_0^S k^* S - ik^* \right)^{-1},
\]

with the scattering length \( f_0^S \), the effective range \( d_0^S \) and \( S \) denoting the total spin of the particle pair. In the following, the usual sign convention of femtoscopy is employed where an attractive interaction leads to a positive scattering length. With these assumptions the analytical description of the correlation function for uncharged particles [72] reads

\[
C(k^*)_{\text{Lednicky}} = 1 + \sum_S \psi_S \left[ \frac{1}{2} \left| f(k^*)^S \right|^2 \left(1 - \frac{d_0^S}{2\sqrt{\pi} r_0}\right) \right.
\]

\[
\left. + 2 \text{Re} f(k^*)^S \tilde{F}_1(Q_{inv} r_0) - \frac{\text{Im} f(k^*)^S}{r_0} \tilde{F}_2(Q_{inv} r_0) \right] (10)
\]

where \( \text{Re} f(k^*)^S [\text{Im} f(k^*)^S] \) denotes the real (imaginary) part of the complex scattering amplitude, respectively. The \( \tilde{F}_1(Q_{inv} r_0) \) and \( \tilde{F}_2(Q_{inv} r_0) \) are analytical functions resulting from the approximation of isotropic emission with a Gaussian source and the factor \( \psi_S \) contains the pair fraction emitted into a certain spin state \( S \). For the \( p-\Lambda \) pair unpolarized emission is assumed. The \( \Lambda-\Lambda \) pair is composed of identical particles and hence additionally quantum statistics needs to be considered, which leads to the introduction of an additional term to the Lednický model, as employed, e.g., in Ref. [16].

While the CATS framework can provide an exact solution for any source and local interaction potential, the Lednický-Lyuboshitz approach uses the known analytical solution outside the range of the strong interaction potential and takes into account its modification in the inner region in an approximate way only. That is why this approach may not be valid for small systems.

2. *Residual correlations*

Table II demonstrates that a significant admixture of residuals is present in the experimental sample of particle pairs. A first theoretical investigation of these so-called residual correlations was conducted in Ref. [73]. This analysis relies on the procedure established in Ref. [19], where the initial correlation function of the residual is calculated and then transformed to the new momentum basis after the decay.

For the \( p-p \) channel only the feed down from the \( p-\Lambda \) correlation function is considered, which is obtained by fitting the \( p-\Lambda \) experimental correlation function and then transforming it to the \( p-p \) momentum basis. All contributions are weighted by the corresponding \( \lambda \) parameters and the modeled correlation function for this pair \( C_{\text{model},p-p}(k^*) \) can be written...
as

\[ C_{\text{model},p-p}(k^*) = 1 + \lambda_{pp} \cdot [C_{pp}(k^*) - 1] + \lambda_{pp,a}[C_{pp,a}(k^*) - 1]. \]  

(11)

All other residual correlations are assumed to be flat.

For the \( p-\Lambda \), residual correlations from the \( p-\Sigma^0 \), \( p-\Xi \), and \( \Lambda-\Lambda \) pairs are taken into account. As the \( \Lambda-\Lambda \) correlation function is rather flat no further transformation is applied. The \( p-\Sigma^0 \) correlation function is obtained using predictions from Ref. [74].

As the decay products of the reaction \( \Xi \rightarrow \Lambda \pi \) are charged and therefore accessible by ALICE, we measure the \( p-\Xi \) correlation function. The experimental data are parametrized with a phenomenological function

\[ C_{p-\Xi}(k^*) = 1 + \frac{\exp(-k^*a_\Xi)}{k^*a_\Xi}, \]  

(12)

where the parameter \( a_\Xi \) is employed to scale the function to the data and has no physical meaning. Its value is found to be \( a_\Xi = 3.88 \) fm.

The modeled correlation function \( C_{\text{model},p-\Lambda}(k^*) \) for the pair is obtained by

\[
C_{\text{model},p-\Lambda}(k^*) = 1 + \lambda_{p\Lambda}[C_{p\Lambda}(k^*) - 1] \\
+ \lambda_{p\Lambda,a}[C_{p\Lambda,a}(k^*) - 1] \\
+ \lambda_{p\Lambda,\pi}[C_{p\Lambda,\pi}(k^*) - 1].
\]  

(13)

As the present knowledge on the hyperon-hyperon interaction is scarce, in particular regarding the interaction of the \( \Lambda \) with other hyperons, all residual correlations feeding into the \( \Lambda-\Lambda \) correlation function are considered to be consistent with unity,

\[ C_{\text{model},\Lambda-\Lambda}(k^*) = 1 + \lambda_{\Lambda\Lambda}[C_{\Lambda\Lambda}(k^*) - 1]. \]  

(14)

It should be noted, that the residual correlation functions, after weighting with the corresponding \( \lambda \) parameter, transformation to the momentum base of the correlation of interest and taking into account the finite momentum resolution, only barely contribute to the total fit function.

3. Total correlation function model

The correlation function modeled according to the considerations discussed above is then multiplied by a linear function to correct for the baseline as discussed in Sec. III C and weighted with a normalization parameter \( \mathcal{N} \)

\[ C_{\text{tot}}(k^*) = \mathcal{N} \cdot (a + b \cdot k^*) \cdot C_{\text{model}}(k^*), \]  

(15)

where \( C_{\text{model}}(k^*) \) incorporates all considered theoretical correlation functions, weighted with the corresponding \( \lambda \) parameters as discussed in Secs. III A and III D.

The inclusion of a baseline is further motivated by the presence of a linear but nonflat correlation observed in the data outside the femtosopic region (see Fig. 2 for \( k^* \in [0.3, 0.5] \) GeV/c). When attempting to use a higher-order polynomial to model the background, the resulting curves are still compatible with a linear function, while their interpolation into the lower \( k^* \) region leads to an overall poorer fit quality.

IV. SYSTEMATIC UNCERTAINTIES

A. Correlation function

The systematic uncertainties of the correlation functions are extracted by varying the proton and \( \Lambda \) candidate selection criteria according to Table III. Due to the low number of particle pairs, in particular at low \( k^* \), the resulting variations of the correlation functions are in general much smaller than the statistical uncertainties. In order to still estimate the systematic uncertainties the data are rebinned by a factor of 10. The systematic uncertainty on the correlation function is obtained by computing the ratio of the default correlation function to the one obtained by the respective cut variation. Whenever this results in two systematic uncertainties, i.e., by a variation up and downwards, the average is taken into account. Then all systematic uncertainties from the cut variations are summed up quadratically. This is then extrapolated to the finer binning of the correlation function by fitting a polynomial of second order. The obtained systematic uncertainties are found to be largest in the lowest \( k^* \) bin. The individual contributions in
that bin are summarized in Table III and the resulting total systematic uncertainty accounts to about 4% for \( p-p \), 1% for \( p-\Lambda \), and 2.5% for \( \Lambda-\Lambda \). Variations of the proton DCA selection are not taken into account for the computation of the systematic uncertainty since it dilutes (enhances) the correlation signal by introducing more (less) secondaries in the sample. This effect is recaptured by a change in the \( \lambda \) parameter.

### B. Femtoscopic fit

To evaluate the systematic uncertainty of the femtoscopic fit, and hence on the measurement of the radius \( r_0 \), the fit is performed applying the following variations. Instead of the common fit, the radius is determined separately from the \( p-p \) and \( p-\Lambda \) correlation functions. \( \Lambda-\Lambda \) is excluded because it imposes only a shallow constraint on the radius, in particular since the scattering parameters are unconstrained for the fit. Furthermore, the input to the \( \lambda \) parameters are varied by 25%, while keeping the purity and the fraction of primaries and secondaries constant since this would correspond to a variation of the particle selection and thus would require a different experimental sample as discussed above. Additionally, all fit ranges of both the femtoscopic and the baseline fits are varied individually by up to 50% and 10%, respectively. The lower bound of the femtoscopic fit is always left at its default value. For the \( p-\Lambda \) correlation function the dependence on the fit model is studied by replacing the Lednický and Lyuboshitz analytical model with the potential introduced by Bodmer, Usmani, and Carlson [75] for which the Schrödinger equation is explicitly solved using CATS. Additionally, the fit for the \( p-p \) and \( p-\Lambda \) correlation function is performed without the linear baseline. The radius is determined for 2000 random combinations of the above-mentioned variations. The resulting distribution of radii is not symmetric and the systematic uncertainty is therefore extracted as the boundaries of the 68% confidence interval around the median of the distribution and accounts to about 4% of the determined radius.

V. RESULTS

The obtained \( p-p \), \( p-\Lambda \), and \( \Lambda-\Lambda \) correlation functions are shown in Fig. 3. For each of the correlation functions we do not observe any minijet background in the low \( k^* \) region, as observed in the case of neutral [76] and charged [51] kaon pairs and charged pion pairs [50]. This demonstrates that the femtoscopic signal in baryon-baryon correlations is dominant in ultrarelativistic \( pp \) collisions. The signal amplitude for the \( p-p \) and \( p-\Lambda \) correlations are much larger than the one observed in analogous studies from heavy-ion collisions [1,12,13,15], due to the small particle emitting source formed in \( pp \) collisions. The signal amplitude for the \( k^* \) dependence on the fit correlation and the Lednický model for the \( p-p \) correlation exceeds the value expected considering only quantum statistic effects, the limited amount of data of the herewith presented sample does not allow us to draw strong conclusions on the attractive nature of the \( \Lambda-\Lambda \) interaction [27,38].

The experimental data are fitted using CATS and hence the exact solution of the Schrödinger equation for the \( p-p \) correlation and the Lednický model for the \( p-\Lambda \) and \( \Lambda-\Lambda \) correlation. The three fits are done simultaneously and in this way the source radius is extracted and different scattering parameters for the \( p-\Lambda \) and \( \Lambda-\Lambda \) interactions can be tested. While in the case of the \( p-p \) and \( p-\Lambda \) correlation function the existence of a baseline is clearly visible in the data, the low amount of pairs in the \( \Lambda-\Lambda \) channel do not allow for such a conclusion. Therefore, the baseline is not included in the model for the \( \Lambda-\Lambda \) correlation function.

The simultaneous fit is carried out by using a combined \( \chi^2 \) and with the radius as a free parameter common to all correlation functions. The fit range is \( k^* \in [0, 0.16] \text{ GeV}/c \) for \( p-p \) and \( k^* \in [0, 0.22] \text{ GeV}/c \) for \( p-\Lambda \) and \( \Lambda-\Lambda \). Hereafter we adopt the convention of positive scattering lengths for attractive interactions and negative scattering lengths for
repulsive interactions. The $p$-$\Lambda$ strong interaction is modeled employing scattering parameters obtained using the next-to-leading order expansion of a chiral effective field theory at a cutoff scale $\Lambda = 600$ MeV [26]. The simultaneous fit of the $p$-$p$, $p$-$\Lambda$, and $\Lambda$-$\Lambda$ correlation functions yields a common radius of $r_0 = 1.125 \pm 0.018$ (stat) $^{+0.058}_{-0.035}$ (syst) fm.

The blue line in the left panel in Fig. 3 shows the result of the femtoscopic fit to the $p$-$p$ correlation function using the Argonne $v_{18}$ potential that describes the experimental data in a satisfactory way. The red curve in the central panel shows the result of the NLO calculation for $p$-$\Lambda$. In the case of $\Lambda$-$\Lambda$ (right panel), the yellow curve represents the femtoscopic fit with free scattering parameters. The width of the femtoscopic fits corresponds to the systematic uncertainty of the correlation function discussed in Sec. IV.

After the fit with the NLO scattering parameters has converged, the $p$-$\Lambda$ correlation function for the same source size is compared to the data using various theoretically obtained scattering parameters [25,26,77–83] as summarized in Table IV. The degree of consistency is expressed in the number of standard deviations $n_\sigma$, as displayed in Fig. 4 together with an overview of the present knowledge about the $\Lambda$-$\Lambda$ interaction. For a detailed overview of the currently available models see, e.g., Ref. [38], from which we have obtained the collection of standard deviations $n_\sigma$, as displayed in Fig. 4. The resulting correlation functions obtained by employing the Lednický and Lyuboshitz analytical model [72] and considering also the secondaries and impurities contributions are compared to the data. The degree of consistency is expressed in the number of standard deviations $n_\sigma$, as displayed in Fig. 4 together with an overview of the present knowledge about the $\Lambda$-$\Lambda$ interaction. For a detailed overview of the currently available models see, e.g., Ref. [38], from which we have obtained the collection of scattering parameters. Additionally to the Nijmegen meson exchange models mentioned above, the data are compared to various other theoretical calculations. An exemplary boson-exchange potential is Ehime [84,85], whose strength is fitted to the outdated double hypernuclear bound energy, $\Delta B_{\Lambda,\Lambda} = 4$ MeV [86] and accordingly known to be too attractive. As an exemplary quark model including baryon-baryon interactions with meson exchange effects, the fss2 model [87,88] is used. Moreover, the potentials by Filikhin and Gal (FG) [89] and by Hiyama, Kamimura, Motoba, Yamada, and Yamamoto (HK-MYY) [90], which are capable of describing the NAGARA event [36] are employed.

In contrast to the $p$-$\Lambda$ case, the agreement with the data increases with every revision of the Nijmegen potential, while the introduction of the extended soft core slightly increases the deviation. In particular solution NSC97f yields the overall

<table>
<thead>
<tr>
<th>Model</th>
<th>$f_0^{=0}$ (fm)</th>
<th>$f_0^{=1}$ (fm)</th>
<th>$d_0^{=0}$ (fm)</th>
<th>$d_0^{=1}$ (fm)</th>
<th>$n_\sigma$</th>
</tr>
</thead>
<tbody>
<tr>
<td>ND [77]</td>
<td>1.77</td>
<td>2.06</td>
<td>3.78</td>
<td>3.18</td>
<td>1.1</td>
</tr>
<tr>
<td>NF [78]</td>
<td>2.18</td>
<td>1.93</td>
<td>3.19</td>
<td>3.358</td>
<td>1.1</td>
</tr>
<tr>
<td>NSC89 [79]</td>
<td>2.73</td>
<td>1.48</td>
<td>2.87</td>
<td>3.04</td>
<td>0.9</td>
</tr>
<tr>
<td></td>
<td>a 0.71</td>
<td>2.18</td>
<td>5.86</td>
<td>2.76</td>
<td>1.0</td>
</tr>
<tr>
<td></td>
<td>b 0.9</td>
<td>2.13</td>
<td>4.92</td>
<td>2.84</td>
<td>1.0</td>
</tr>
<tr>
<td></td>
<td>c 1.2</td>
<td>2.08</td>
<td>4.11</td>
<td>2.92</td>
<td>1.0</td>
</tr>
<tr>
<td>NSC97 [80]</td>
<td>d 1.71</td>
<td>1.95</td>
<td>3.46</td>
<td>3.08</td>
<td>1.0</td>
</tr>
<tr>
<td></td>
<td>e 2.1</td>
<td>1.86</td>
<td>3.19</td>
<td>3.19</td>
<td>1.1</td>
</tr>
<tr>
<td></td>
<td>f 2.51</td>
<td>1.75</td>
<td>3.03</td>
<td>3.32</td>
<td>1.0</td>
</tr>
<tr>
<td>ESC08 [81]</td>
<td>2.7</td>
<td>1.65</td>
<td>2.97</td>
<td>3.63</td>
<td>0.9</td>
</tr>
<tr>
<td></td>
<td>LO [25]</td>
<td>1.91</td>
<td>1.23</td>
<td>1.4</td>
<td>2.13</td>
</tr>
<tr>
<td></td>
<td>NLO [26]</td>
<td>2.91</td>
<td>1.54</td>
<td>2.78</td>
<td>2.72</td>
</tr>
<tr>
<td></td>
<td>A [82]</td>
<td>1.56</td>
<td>1.59</td>
<td>1.43</td>
<td>3.16</td>
</tr>
<tr>
<td></td>
<td>J04 [83]</td>
<td>2.56</td>
<td>1.66</td>
<td>2.75</td>
<td>2.93</td>
</tr>
<tr>
<td></td>
<td>J04c [83]</td>
<td>2.66</td>
<td>1.57</td>
<td>2.67</td>
<td>3.08</td>
</tr>
<tr>
<td></td>
<td>$\chi$EFT</td>
<td>2.7</td>
<td>1.65</td>
<td>2.97</td>
<td>3.63</td>
</tr>
</tbody>
</table>

The table shows the result of the $\chi$EFT calculation for $d_0$ and $f_0$, as displayed in Fig. 4.
best agreement with the data. The correlation function modeled using scattering parameters of the Ehime model, which is known to be too attractive deviates by about two standard deviations from the data.

For an attractive interaction (positive $f_0$) the correlation function is pushed from the quantum statistics distribution for two fermions (correlation function equal to 0.5 for $k^* = 0$) to unity. As a result within the current uncertainties the $\Lambda$-$\Lambda$ correlation function is rather flat and close to 1 and this lack of structure makes it impossible to extract the two scattering parameters with a reasonable uncertainty. This means that even by increasing the data by a factor 10, as expected from the RUN2 data, it will be very complicated to constrain precisely the region $f_0 > 0$.

As for the region of negative scattering length $f_0$ this is connected in scattering theory either to a repulsive interaction or to the existence of a bound state close to the threshold and a change in the sign of the scattering length. Since the $\Lambda$-$\Lambda$ interaction is known to be slightly attractive above the threshold [36], the measurement of a negative scattering lengths would strongly support the existence of the H-dibaryon. Notably the correlation function modeled employing the scattering parameters obtained by the STAR Collaboration in Au-Au collisions at $\sqrt{s_{NN}} = 200$ GeV [16] and all the secondaries and impurities contributions deviates by 6.8 standard deviations from the data. This is also shown by the cyan curve displayed in the right panel of Fig. 3, which is obtained using the source radius and the $\lambda$ parameters from this analysis and the scattering parameters from Ref. [16]. On the other hand these parameters and all those corresponding to the gray-shaded area in Fig. 4 lead to a negative genuine $\Lambda$-$\Lambda$ correlation function if the Lednický model is employed. The total correlation function that is compared to the experimental data is not negative because the impurities and secondaries contributions lead to a total correlation function that is always positive. This means that the combination of large effective ranges and negative scattering lengths translate into unphysical correlation functions, for small colliding systems as $pp$. This effect is not immediate visible in larger colliding system such as Au-Au at $\sqrt{s_{NN}} = 200$ GeV measured by STAR, where the obtained correlation function does not become negative. This demonstrates that these scattering parameters intervals combined with the Lednický model are not suited to describe the correlations functions measured in small systems. One could test the corresponding local potentials with the help of CATS [53], since the latter does not suffer from the limitations of the Lednický model due to the employment of the asymptotic solution. On the other hand we have directly compared the correlation functions obtained employing CATS and the $\Lambda$-$\Lambda$ local potentials reported in [38] with the correlation functions obtained using the corresponding scattering parameters and the Lednický model. For the typical source radii of 1.3 fm the deviations are within 10%. This disfavours the region of negative scattering lengths and large effective ranges for the $\Lambda$-$\Lambda$ correlation.

This study is the first measurement with baryon pairs in $pp$ collisions at $\sqrt{s} = 7$ TeV, while other femtoscopic analyses were conducted with neutral [76] and charged [51] kaon pairs and charged pion pairs [50] with the ALICE experiment. The radius obtained from baryon pairs is found to be slightly larger than that measured from meson-meson pairs at comparable transverse mass as shown in Fig. 5.

VI. SUMMARY

This paper presents the first femtoscopic measurement of $p-p$, $p-\Lambda$, and $\Lambda-\Lambda$ pairs in $pp$ collisions at $\sqrt{s} = 7$ TeV. No evidence for the presence of minijet background is found and it is demonstrated that this kind of study with
baryon-baryon and antibaryon-antibaryon pairs is feasible. With a newly developed method to compute the contributions arising from impurities and weakly decaying resonances to the correlation function from single particles quantities only, the genuine correlation functions of interest can be extracted from the signal. These correlation functions contribute with 74% for p-p, 47% for p-Λ, and 30% for Λ-Λ to the total signal. A simultaneous fit of all correlation functions with a femtoscopic model featuring residual correlations stemming from the above-mentioned effects yields a radius of the particles emitting source of \( r_0 = 1.125 \pm 0.018 \text{ (stat)}^{+0.038}_{-0.035} \text{ (syst)} \) fm. For the first time, the Argonne \( v_{18} \) NN potential with the \( s \) and \( p \) waves was used to successfully describe the \( p-p \) correlation and so obtain a solid benchmark for our investigation. For the case of the \( p-\Lambda \) correlation function, the NLO parameter set obtained within the framework of chiral effective field theory is consistent with the data, but other models are also found to be in agreement with the data. The present pair data in the \( \Lambda-\Lambda \) channel allows us to constrain the available scattering parameter space. Large effective ranges \( d_0 \) in combination with negative scattering parameters lead to unphysical correlations if the Lednický model is employed to compute the correlation function. This also holds true for the average values published by the STAR collaboration in \( \text{Au-Au} \) collisions at \( \sqrt{s_{NN}} = 200 \text{ GeV} \), that are found to be incompatible with the measurement in \( pp \) collisions within the Lednický model. The larger data sample of the LHC Run 2 and Run 3, where we expect up to a factor ten and 100 more data respectively, will enable us to extend the method also to \( \Sigma \), \( \Xi \), and \( \Omega \) hyperons and thus further constrain the hyperon-nucleon interaction.

ACKNOWLEDGMENTS

The ALICE Collaboration would like to thank all its engineers and technicians for their invaluable contributions to the construction of the experiment and the CERN accelerator teams for the outstanding performance of the LHC complex. The ALICE Collaboration gratefully acknowledges the resources and support provided by all Grid centers and the Worldwide LHC Computing Grid (WLCG) collaboration. The ALICE Collaboration acknowledges the following funding agencies for their support in building and running the ALICE detector: A. I. Alikhanyan National Science Laboratory (Yerevan Physics Institute) Foundation (ANSL), State Committee of Science and World Federation of Scientists (WFS), Armenia; Austrian Academy of Sciences and Nationalstiftung für Forschung, Technologie und Entwicklung, Austria; Ministry of Communications and High Technologies, National Nuclear Research Center, Azerbaijan; Conselho Nacional de Desenvolvimento Científico e Tecnológico (CNPq), Universidade Federal do Rio Grande do Sul (UFRGS), Financiadora de Estudos e Projetos (Finep) and Fundação de Amparo à Pesquisa do Estado de São Paulo (FAPESP), Brazil; Ministry of Science & Technology of China (MSTC), National Natural Science Foundation of China (NSFC) and Ministry of Education of China (MOEC), China; Ministry of Science and Education, Croatia; Ministry of Education, Youth and Sports of the Czech Republic, Czech Republic; The Danish Council for Independent Research | Natural Sciences, the Carlsberg Foundation and Danish National Research Foundation (DNRF), Denmark; Helsinki Institute of Physics (HIP), Finland; Commissariat à l’Energie Atomique (CEA) and Institut National de Physique Nucléaire et de Physique des Particules (IN2P3) and Centre National de la Recherche Scientifique (CNRS), France; Bundesministerium für Bildung, Wissenschaft, Forschung und Technologie (BMBF) and GSI Helmholtzzentrum für Schwerionenforschung GmbH, Germany; General Secretariat for Research and Technology, Ministry of Education, Research and Religions, Greece; National Research, Development and Innovation Office, Hungary; Department of Atomic Energy Government of India (DAE), Department of Science and Technology, Government of India (DST), University Grants Commission, Government of India (UGC) and Council of Scientific and Industrial Research (CSIR), India; Indonesian Institute of Science, Indonesia; Centro Fermi - Museo Storico della Fisica e Centro Studi e Ricerche Enrico Fermi and Istituto Nazionale di Fisica Nucleare (INFN), Italy; Institute for Innovative Science and Technology, Nagasaki Institute of Applied Science (IIIT), Japan Society for the Promotion of Science (JSPS) KAKENHI and Japanese Ministry of Education, Culture, Sports, Science and Technology (MEXT), Japan; Consejo Nacional de Ciencia (CONACYT) y Tecnología, through Fondo de Cooperación Internacional en Ciencia y Tecnología (FONCICYT) and Dirección General de Asuntos del Personal Académico (DGAPA), Mexico; Nederlandse Organisatie voor Wetenschappelijk Onderzoek (NWO), Netherlands; The Research Council of Norway, Norway; Commission on Science and Technology for Sustainable Development in the South (COMSATS), Pakistan; Pontificia Universidad Católica del Perú, Peru; Ministry of Science and Higher Education and National Science Centre, Poland; Korea Institute of Science and Technology Information (KISTI), Republic of Korea; Ministry of Education and Scientific Research, Institute of Atomic Physics and Romanian National Agency for Science, Technology and Innovation, Romania; Joint Institute for Nuclear Research (JINR), Ministry of Education and Science of the Russian Federation and National Research Centre Kurchatov Institute, Russia; Ministry of Education, Science, Research and Sport of the Slovak Republic, Slovakia; National Research Foundation of South Africa, South Africa; Centro de Aplicaciones Tecnológicas y Desarrollo Nuclear (CEADEN), Cubaenergía, Cuba and Centro de Investigaciones Energéticas, Medioambientales y Tecnológicas (CIEMAT), Spain; Swedish Research Council (VR) and Knut & Alice Wallenberg Foundation (KAW), Sweden; European Organization for Nuclear Research, Switzerland; National Science and Technology Development Agency (NSDTA), Suranaree University of Technology (SUT) and Office of the Higher Education Commission under NRU project of Thailand, Thailand; Turkish Atomic Energy Agency (TAEK), Turkey; National Academy of Sciences of Ukraine, Ukraine; Science and Technology Facilities Council (STFC), United Kingdom; National Science Foundation of the United States of America (NSF) and United...
The impurity is particles of that species. For each particle different subsets \( N_F \) simulations or MC template fits. The product of the two reads

\[
i = i \in [1, \ldots, N_F] \leq i \leq N_F + N_M \text{ should be associated with feed-down contributions and } N_F + 1 \leq i \leq N_F + N_M \text{ should be associated with impurities, where } N_F \text{ is the number of feed-down channels and } N_M \text{ the number of impurity channels. In the present work we assume that all impurity channels contribute with a flat distribution to the total correlation, therefore we do not study differentially the origin of the impurities and combine them in a single channel, i.e., } N_M = 1. \]

Further we define

\[
X_F = \sum_{i=1}^{N_F} X_i, \tag{A1}
\]
as the total number of particles that stem from feed down and

\[
X_M = \sum_{i=N_F+1}^{N_F+N_M} X_i, \tag{A2}
\]
as the total number of particles that were misidentified (i.e., impurities). \( X_0 \) is the number of correctly identified primary particles that are of interest for the femtoscopy analysis.

The purity \( \mathcal{P} \) is the fraction of correctly identified particles, not necessarily primary, to the total number of particles in the sample [Eq. (A3)].

\[
\mathcal{P}(X) = (X_0 + X_F)/X. \tag{A3}
\]
The impurity is

\[
\mathcal{P}(X) = X_M/X. \tag{A4}
\]

For the later discussion it is beneficial to combine the two definitions and refer to the purity as

\[
\mathcal{P}(X) = \begin{cases} 
\mathcal{P}(X) = (X_0 + X_F)/X & \text{for } i \leq N_F, \\
\mathcal{P}(X) = X_M/X & \text{else.}
\end{cases} \tag{A5}
\]

Another quantity of interest will be the channel fraction \( f_i \), which is defined as the fraction of particles originating from the \( i \)th channel relative to the total number of either correctly identified or misidentified particles:

\[
f_i = \begin{cases} 
X_i/(X_0 + X_F) & \text{for } i \leq N_F, \\
X_i/X_M & \text{else.}
\end{cases} \tag{A6}
\]

As discussed in the main body of the paper both the purity and the channel fractions can be obtained either from MC simulations or MC template fits. The product of the two reads

\[
P(X_i) = \mathcal{P}(X_i)f(X_i) = \frac{X_i}{X}. \tag{A7}
\]

Next we will relate \( \mathcal{P}(X_i) \) and \( f(X_i) \) to the correlation function between particle pairs, which is defined as

\[
C(XY) = \frac{N(XY)}{M(XY)}, \tag{A8}
\]

where \( N \) and \( M \) are the yields of an XY particle pair in same and mixed events respectively. Note that this is a raw correlation function, which is not properly normalized. The normalization is discussed in the main body of the paper, but is irrelevant in the current discussion and it will be omitted. Both \( N \) and \( M \) are yields, which can be decomposed into the sum of their ingredients. Using the previously discussed notion of different channels of origin

\[
N(XY) = \sum_{i,j} N(X_iY_j) = \sum_{i,j} N(X_iY_j) \tag{A9}
\]

\[
M(XY) = \sum_{i,j} M(X_iY_j) \tag{A10}
\]

Hence the total correlation function becomes:

\[
C(XY) = \frac{\sum_{i,j} N(X_iY_j)}{M(XY)} = \frac{\sum_{i,j} N(X_iY_j)}{M(X_iY_j) M(X_iY_j)} \tag{A11}
\]

\[
= \sum_{i,j} \frac{N(X_iY_j)}{M(X_iY_j) M(X_iY_j)} C_{i,j}(XY) \lambda_{i,j}(XY), \tag{A12}
\]

where \( C_{i,j}(XY) \) is the contribution to the total correlation of the \( i,j \)th channel of origin of the particles X,Y and \( \lambda_{i,j}(XY) \) is the corresponding weight coefficient. How to obtain the individual functions \( C_{i,j}(XY) \) is discussed in the main body of the paper. The weights \( \lambda_{i,j} \) can be derived from the purities and channel fractions of the particles X and Y. This is possible since \( \lambda_{i,j} \) depends only on the mixed event sample for which the underlying assumption is that the particles are not correlated. In that case the two-particle yield \( M(XY) \) can be factorized and according to Eq. (A11) the \( \lambda \) coefficients can be expressed as

\[
\lambda_{i,j}(XY) = \frac{M(X_iY_j)}{M(X_iY_j)} = \frac{M(X_i)}{M(X) M(Y)} = P(X_i)P(Y_j). \tag{A13}
\]

The last step follows directly from Eq. (A7) applied to the mixed event samples of X and Y. Equation (A7) relates \( P \) to the known quantities \( \mathcal{P} \) and \( f \), hence the \( \lambda \) coefficients can be rewritten as

\[
\lambda_{i,j}(XY) = \mathcal{P}(X_i)f(X_i)\mathcal{P}(Y_j)f(Y_j). \tag{A14}
\]

We would like to point out that due to the definition of \( P(X_i) \) the sum of all \( \lambda \) parameters is automatically normalized to unity.


G. Agakishiev et al. (HADES Collaboration), pp and $\pi\pi$ intensity interferometry in collisions of $\mathrm{Ar} + \mathrm{KCl}$ at 1.76A-GeV, Eur. Phys. J. A 47, 63 (2011).


M. M. Aggarwal et al. (WA98 Collaboration), arXiv:0709.2477 [nucl-ex].


J. Adam et al. (ALICE Collaboration), Centrality dependence of pion freeze-out radii in Pb-Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV, Phys. Rev. C 93, 024905 (2016).


G. Agakishiev et al. (HADES Collaboration), Lambda-p femtoscopic correlations in $\mathrm{Ar} + \mathrm{KCl}$ at 1.76 A GeV, Phys. Rev. C 82, 021901 (2010).


T. Nagae et al., Observation of a $^4\text{He}$ Bound State in the $^4\text{He}(K^-,\pi^-)$ Reaction at 600 MeV/c, Phys. Rev. Lett. 80, 1605 (1998).

H. Nemura et al., Baryon interactions from lattice QCD with physical masses—strangeness $S=-1$ sector —, EPJ Web Conf. 175, 05030 (2018).

K. Nakazawa et al., The first evidence of a deeply bound state of Xi-14N system, Prog. Theor. Exp. Phys. 2015, 033D02 (2015).


[76] B. Abelev et al. (ALICE Collaboration), $K^0\bar{K}^0$ correlations in pp collisions at $\sqrt{s} = 7$ TeV from the LHC ALICE experiment, Phys. Lett. B 717, 151 (2012).


S. Acharya, et al.

143Wigner Research Centre for Physics, Hungarian Academy of Sciences, Budapest, Hungary
144Yale University, New Haven, Connecticut, United States
145Yonsei University, Seoul, Republic of Korea

aDeceased.
bDipartimento DET del Politecnico di Torino, Turin, Italy.
cM. V. Lomonosov Moscow State University, D. V. Skobeltsyn Institute of Nuclear, Physics, Moscow, Russia.
dDepartment of Applied Physics, Aligarh Muslim University, Aligarh, India.
eInstitute of Theoretical Physics, University of Wroclaw, Poland.