

1 MULTI-LOCUS INTERACTIONS AND THE BUILD-UP OF REPRODUCTIVE ISOLATION

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15 **Keywords:** multi-locus interactions, networks, speciation, reproductive isolation, epistasis, incompatibility

16

17 Abstract

18

19 All genes interact with other genes, and their additive effects and epistatic interactions affect an organism's
20 phenotype and fitness. Recent theoretical and empirical work has advanced our understanding of the role of multi-
21 locus interactions in speciation. However, relating different models to one another and to empirical observations is
22 challenging. This review focuses on multi-locus interactions that lead to reproductive isolation (RI) through reduced
23 hybrid fitness. We first review theoretical approaches and show how recent work incorporating a mechanistic
24 understanding of multi-locus interactions recapitulates earlier models, but also makes novel predictions concerning
25 the build-up of RI. These include high variance in the build-up rate of RI among taxa, the emergence of strong
26 incompatibilities producing localised barriers to introgression, and an effect of population size on the build-up of RI.
27 We then review recent experimental approaches to detect multi-locus interactions underlying RI using genomic
28 data. We argue that future studies would benefit from overlapping methods like Ancestry Disequilibrium scans,
29 genome scans of differentiation and analyses of hybrid gene expression. Finally, we highlight a need for further
30 overlap between theoretical and empirical work, and approaches that predict what kind of patterns multi-locus
31 interactions resulting in incompatibilities will leave in genome-wide polymorphism data.

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35 Introduction

36

37 No gene works in isolation. Instead, genes interact with other genes and regulatory factors resulting in both additive
38 effects and epistatic interactions (see Box 1 for definitions), which underlie phenotype and fitness. Consequently
39 evolution, speciation and adaptation can be strongly influenced by interactions among multiple loci. In this review
40 we are interested in the role of multi-locus interactions (see Box 1) in the build-up of reproductive isolation (RI).

41 Much of the theoretical basis for understanding the evolution of RI is founded on epistasis and the concept of gene
42 interactions. Bateson (1), Dobzhansky (2) and Muller (3) all suggested a model where two populations may become
43 incompatible if they undergo substitutions at two interacting loci that are only 'tested' in hybrids (BDM
44 incompatibilities or BDMIs, see Part 1). Gene interactions underlying RI are conventionally considered in the context
45 of intrinsic RI, but interactions also play a role in the evolution of extrinsic isolation and divergence of 'ecological
46 speciation genes'. Multi-locus interactions will tend to underlie most traits, including those under ecological
47 selection, and strong selection on one locus could lead to co-evolution with other interacting loci. Multi-locus
48 interactions play a role both in the beginning and later in the speciation process. However, as RI accumulates, the
49 more loci are likely to be involved, and therefore the more important it is to consider the possible interactions
50 between loci in contributing to strong RI.

51

52 Empirical evidence shows that the nature of multi-locus interactions, such as the structure of interaction networks
53 (see Box 1), and co-evolution of interacting partners can have consequences for phenotype and fitness. For example,
54 in the yeast genome, most genes interact with a fairly small number of others, but other genes are 'hubs' with very
55 large numbers of interaction partners (4). Hub genes tend to have stronger fitness consequences when mutated in
56 comparison to loci with fewer interactions (5–7) potentially leading to different consequences for RI. The structure
57 of multi-locus interactions also influences where epistasis, and thus genetic incompatibilities, are likely to arise.
58 Incompatibilities might be likely to involve loci that function in the same biological process or protein complex, as
59 suggested by enrichment of negative fitness epistasis in a yeast mutation study (8).

60

61 Our growing empirical understanding of gene regulation and protein interactions has inspired conceptual
62 expansions to the initial BDMI model. At the same time, genome-wide empirical studies are being utilised to
63 understand the role of multi-locus interactions in RI, as discussed in Part 2. In this paper we bring together both
64 theoretical and empirical approaches to understand how multi-locus interactions could drive the build-up of RI. Our
65 review has three parts. First, we discuss different theoretical approaches that have been used to explore the
66 possible roles of multi-locus interactions in speciation with an aim to link the different approaches at a conceptual
67 level. We discuss their key findings and insights, and evaluate where additional modelling could further extend our
68 knowledge. In the second part we turn to empirical studies and approaches that can shed light on the role of multi-

69 locus interactions in the build-up of RI, highlighting the challenges with current methods. In the last part we
70 conclude by identifying fruitful avenues for the future, particularly bringing together both theoretical and empirical
71 work in this field and using genome-scale simulations as a tool to bridge between theory and observation.

72

73 **Box 1. Definitions.**

74

75 By **multi-locus interactions** we mean physical or statistical pairwise or higher order interactions among two or more
76 genomic loci. We are especially interested in scenarios that involve interactions between more than two loci. By **loci**
77 we mean either genes or regulatory sequences. Physical, direct interactions among the loci can take the form of
78 protein-protein interactions (**PPI**), or regulation through interactions between DNA, RNA or protein molecules (9).

79 Our focus is on interactions that have an epistatic effect on fitness. By **epistatic effect on fitness** we mean
80 that the fitness effect of an allele is dependent on alleles at other loci (or in some cases sites within a locus interact
81 epistatically, e.g. (10,11)). For epistatically interacting alleles, their combined fitness effect deviates from linearity or
82 additivity. Epistasis on the level of fitness can be caused either by epistatic effects on phenotypic traits, or by additive
83 effects that themselves have nonlinear effects on fitness. Epistatic fitness effect could arise due to physical interaction
84 among loci. However, physical interactions among the loci do not necessarily translate into epistatic effects for fitness
85 and likewise, epistatic effects for fitness can arise between loci that do not interact at physical level. For instance,
86 alleles at two genes that contribute to the same trait via different pathways, or act as upstream regulators of the same
87 pathway, can have epistatic effects on fitness without directly interacting with each other. To date we know very little
88 about how interactions between loci at the molecular level (e.g. regulatory or protein-protein interactions) translate
89 into epistasis that is relevant for specific traits or individual fitness.

90 Interactions between loci can be represented as a network (see regulatory network in Figure 1). **A network**
91 represents the configuration of direct pairwise interactions between the elements, so that network nodes are the
92 interacting elements and links correspond to their interactions. Although only direct interactions are shown as links
93 in the network, it also determines possible indirect interaction pathways: nodes that are connected via some path
94 through the network can in principle influence one another. In most networks, such paths can be traced between
95 almost all nodes. The paths are typically rather short, with only a few intermediate nodes (12,13), which can be
96 thought to facilitate indirect interactions. There are also many other network features that play important roles for
97 dynamics taking place on networks. One is the existence of highly connected **hubs** (a node that has many more
98 connections than other nodes) and related **broad or power-law connectivity distributions**, reflecting heterogeneity
99 in the number of interaction partners between nodes (see, e.g., (14)), which can have strong effects on processes
100 mediated by the network (see, e.g., (15)). Further, similarly to most other real-world networks, biological networks
101 are usually sparse (see, e.g., (13)). Note that the general term 'network' does not, however, necessarily imply that the
102 above-described features are present.

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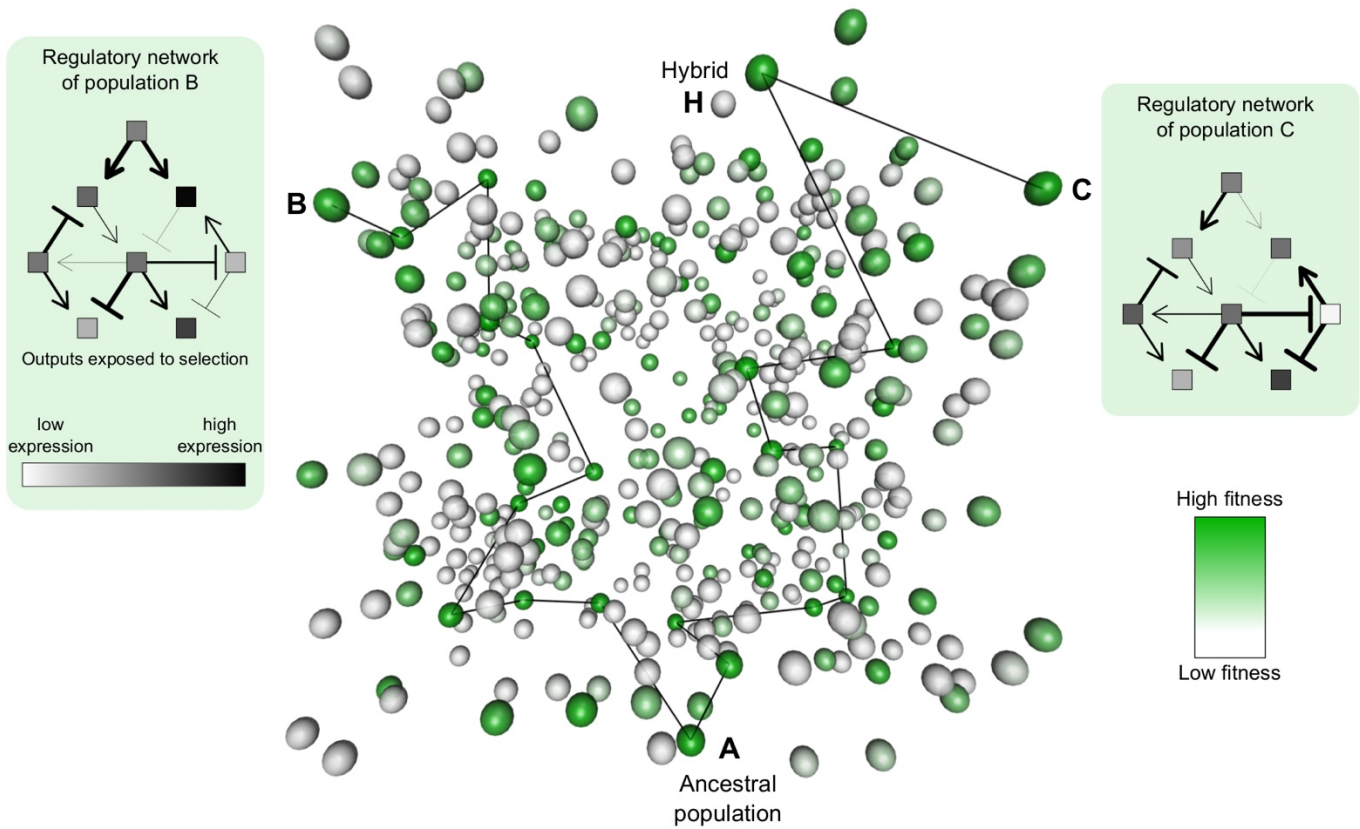
105 **PART 1: Theoretical models: How could multi-locus interactions influence speciation?**

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107 Models of post-zygotic isolation that incorporate epistatic interactions assume that mutations that have positive or
108 neutral fitness effects in the parent populations can cause reduced fitness when combined in hybrids. Alleles from
109 divergent populations may also be beneficial when combined in hybrids, but in this article we focus on interactions

110 with reduced fitness. This outcome can be modelled in several different ways. Many models focus on the
111 evolutionary processes and spatial setting by which reduced hybrid fitness can come about, but fewer studies
112 modelling multi-locus interactions explore the population genetic outcomes under ongoing hybridisation. One of the
113 challenges in speciation research is therefore to determine how the different models relate to each other and to
114 natural populations studied by empiricists. In this section we discuss insights from models of speciation accounting
115 for multi-locus interactions without functional information on interactions, as well as those that incorporate our
116 growing mechanistic understanding of multi-locus interactions (i.e. PPI and regulatory networks). We highlight their
117 main similarities and differences as well as conclusions about the emergence and maintenance of RI. We do not
118 address the extensive modelling in the context of ecological speciation, where divergent selection on multiple loci
119 that are each independently selected can lead to RI despite the homogenising effect of gene flow (16–18). In the
120 models accounting for multi-locus interactions that we address here, speciation occurs as a side-effect of
121 substitutions that may be fixed through drift or selection, depending on the model. Whether or not gene flow is
122 present also varies among models (as described below), but there is no assumption of antagonism between local
123 adaptation and gene flow, which is a common feature of ecological speciation models.

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129 **Figure 1. Networks and fitness landscapes.** Conceptual representation of a high-dimensional fitness landscape with an example
130 of regulatory network evolution leading to RI. Each sphere in the high-dimensional genotype cloud (central panel) represents a
131 possible genotype combination for a multi-locus interaction network (see regulatory network in the side panel). However, not
132 all possible genotype combinations are shown as in reality, the number of possible combinations will be extremely vast. The
133 number of combinations arises because each gene can be mutated in a vast number of different ways, each with different
134 effects on how they interact with other genes in the network. Colours indicate that fitnesses vary among genotype
135 combinations. While fitness landscapes are usually depicted in two or three dimensions, in reality they represent much higher-
136 dimensional space, in which each dimension corresponds to the range of possible genotypes at one locus. This high-
137 dimensionality creates more opportunities for populations to traverse genotype space without crossing regions of low fitness
138 ((19), and see the main text). Our depiction is intended to represent an arbitrary number of dimensions, although only three
139 dimensions are plotted. Black lines indicate two possible paths along which the network could evolve while retaining high
140 fitness from an ancestral population 'A' to daughter populations 'B' and 'C'. A black line between two spheres represents a
141 single mutational step, so that spheres distant in the three plotted dimensions can be adjacent in a dimension that is not
142 plotted. A hypothetical gene regulatory network is indicated for populations B and C. In the network, all genes can alter the
143 expression of certain other genes through up (pointed arrows) or down (flat arrows) regulation. Fitness is determined by the
144 expression levels of two output genes. A hypothetical recombinant hybrid individual 'H' is indicated to show that combining
145 elements of the networks of populations B and C can result in reduced hybrid fitness.

146

147 1.1 Epistasis underlying RI can be modelled without mechanistic knowledge of multi-locus interactions

148

149 Probably the best-known class of models considers the direct impact of inter-locus interactions on hybrid fitness. In
150 Bateson-Dobzhansky-Muller Incompatibilities (BDMIs) (1–3,20), substitutions that occur independently (either in
151 two separate populations, or consecutively in one of the populations (21), through drift or selection) are never
152 tested together, due to allopatry, until being combined in a hybrid, whereupon their interaction can lead to reduced
153 fitness (i.e. epistasis). BDMI models have allowed predictions about how RI builds up over time. Assuming a fixed
154 probability of a new substitution in population 1 leading to an incompatibility with an allele from population 2,
155 incompatibilities should emerge at a rate proportional to the square of the number of differences between diverging
156 populations. This leads to a faster than linear increase in the number of incompatibilities with genetic differences,
157 the so-called 'snowball' effect (22,23). However, as these approaches tend to only consider the number of
158 incompatibilities, they do not allow predictions about the fitness of recombinant hybrids (i.e. F2s or backcrosses, but
159 see (24)). Therefore, they are limited in their ability to predict the strength of a barrier to gene flow in the face of
160 ongoing hybridisation (25).

161

162 Fitness reduction in hybrids caused by new combinations of alleles was also modelled by Wright (26,27) using the
163 idea of a fitness landscape, a multidimensional space in which each dimension represents the range of possible

164 genotypes at a given locus. Each point in the landscape therefore represents a combination of alleles at multiple loci
165 with a certain fitness. For a polygenic trait, there will inevitably be multiple combinations of alleles that combine to
166 produce a phenotype of optimal fitness in a given environment, even when the alleles contribute to the phenotype
167 additively. In other words, the landscape will have multiple 'peaks' with similar high fitness (27,28). These peaks can
168 alternatively be represented as points of high fitness in a genotype space, as in Figure 1 (see also (29)). RI can arise
169 between two populations that are both under stabilising selection for the same optimal phenotype, but which shift
170 to different genotypic peaks of high fitness. This can occur through genetic drift followed by compensatory evolution
171 at other loci (so called nearly neutral, or 'quasi-neutral' divergence) (27,28). Hybrids that carry a previously untested
172 combination of genotypes may thus fall into a region of the landscape with lower fitness. If all loci affect a trait
173 additively, F1 hybrids between parents with different high-fitness genotypes should also be fit, but F2s and other
174 recombinant hybrids can be unfit due to segregation of distinct alleles from each parent that sum to an unfit
175 phenotype when brought together (i.e. 'segregation variance' (30): a combination of additively acting alleles results
176 in an epistatic effect on fitness). However, the emergence of RI under this model is slow (28) and at most linear with
177 time (30). A more recent extension shows how adding explicit epistatic interactions in the phenotypic effects of pairs
178 of loci can lead to faster than linear emergence of RI, with reduced F1 fitness as well as increased segregation
179 variance in recombinant hybrids (31).

180
181 The visual representation of a fitness landscape with multiple peaks of similarly high fitness separated by deep
182 'valleys' has been criticised for failing to represent the true nature of a fitness landscape under high dimensionality.
183 As the dimensionality of the landscape increases, i.e. when more loci contribute to fitness (as is the case for many
184 traits), so does the probability that high fitness peaks are reachable through a series of small mutational steps
185 without passing through regions of reduced fitness (19) (see Figure 1 for an example of a high-dimensional fitness
186 landscape). In other words, peaks of high fitness are likely to be connected by neutral ridges in the higher
187 dimensions. Gavrillets and Gravner (32) envisaged a 'holey landscape' represented as a flat plane interspersed with
188 holes, thus implying that there are very many combinations of genotypes that have equally high fitness, but these
189 are interspersed by combinations that have low fitness (32). As in the original BDMI models (1–3), the evolution of RI
190 is not impeded by a requirement that parental populations traverse regions of low fitness. Increasing the
191 dimensionality of the genotype space will make divergence by drift easier, so that in a multidimensional holey
192 landscape, only a few substitutions may be necessary to result in RI and speciation (32).

193
194 A final approach for modelling the fitness consequences of hybridisation without the need to consider explicit
195 mechanistic knowledge on multi-locus interactions is Fisher's Geometric Model (25,33,34). This approach defines
196 the fitness landscape in terms of phenotype space rather than genotype space. Substitutions are represented as
197 steps through phenotype space, either toward or away from the fitness optimum, potentially in more than one

198 dimension due to pleiotropy. Since each substitution can happen at a different locus, this model allows the
199 assumption of an infinitely large number of loci affecting fitness (25). The phenotype and fitness of any hybrid or
200 backcross can be computed by combining phenotypic changes experienced by each of the parental populations. A
201 key factor that affects the predictions of FGM is the shape of the fitness landscape. For example, Barton (25)
202 assumed a quadratic decline in fitness away from the optimum, and found that strong incompatibilities are unlikely
203 to arise by stabilising selection acting on the phenotype with drift changing the underlying genotype. However,
204 Fraïsse et al. (34) showed that using a different shape of the fitness landscape with a plateau of high fitness allows
205 the accumulation of larger effect substitutions that lead to stronger fitness decreases in recombinant hybrids. By
206 adjusting the shape of the fitness landscape, FGM can account for many empirical patterns in speciation studies,
207 including some that are not well explained by other models (34,35). One of these is that FGM predicts that severe
208 loss of fitness occurs only if multiple factors are introgressed together, especially when recipient genotypes are well
209 adapted (34). In contrast to Orr's (22) treatment of BDMIs, FGM does not predict the snowball effect, although it can
210 generate an 'apparent snowball effect' when the introgressed regions contain a large number of divergent sites.
211 Finally, FGM may be applied to answer questions in speciation that do not relate to incompatibilities per se, like
212 whether divergence arose by drift or selection (36).

213

214 1.2 Models that incorporate a mechanistic understanding of multi-locus interactions

215

216 One possible criticism that applies to all of the models described above is that it is often difficult to make the
217 connection from the theoretical model to the biological context in which loci interact to produce a phenotype (i.e. a
218 mechanistic genotype-phenotype map). Below we discuss several recent efforts to model the emergence of
219 incompatibilities while considering the nature of protein-protein or gene regulatory interactions and how they
220 produce phenotypes. Such models can reveal whether adding functional and more mechanistic details of multi-locus
221 interactions allows for additional insights.

222

223 *1.2.1 Incompatibilities can accumulate by drift in redundant gene regulatory networks*

224

225 A growing understanding of gene regulation has inspired mechanistic models that test whether evolution of
226 regulatory networks can lead to RI (10,37–40). These models allow complex non-additive gene effects and are
227 conceptually similar to fitness landscape models (27,28,31) in that fitness is determined by the combined effect of
228 all loci contributing to a trait or collection of traits that are exposed to selection (i.e. the level or spatial distribution
229 of expression of one or more genes). Because gene regulation tends to be somewhat redundant, populations can
230 evolve and accumulate incompatibilities under directional selection towards the same optimum, by taking different
231 mutational steps (38), or under stabilising selection, through drift and compensatory evolution (10,37,39). In the

232 models of developmental and gene regulatory pathways, this process by which the underlying genetic basis of the
233 trait can change even if the output phenotype remains the same has been termed 'system drift' ((41), see also (42)),
234 but it is conceptually the same as drift under stabilizing selection in fitness landscape models (Section 1.1) (25). The
235 key characteristic of regulatory networks that allow for this system drift is their redundancy, the fact that multiple
236 genotypic states can lead to the same fit outcome. Schiffman and Ralph (40) show analytically that nearly all gene
237 interaction networks are likely to share this property. While the role of system drift in regulatory networks has not
238 been demonstrated in the context of RI, experimental studies have demonstrated the existence of networks of
239 phenotypically stable genotypes within which a population may move (e.g. (43)), and rewiring of genetic pathways
240 and changes in gene function underlying unchanged phenotypes (44).

241

242 *1.2.2 The number of connections and their distribution affect the rate and variance of accumulation of*
243 *incompatibilities, and which genes are likely to be involved*

244

245 Orr's extension to the BDMI model (22) assumed a fixed probability of an incompatibility with each substitution in
246 the diverging populations, meaning all loci could potentially interact with all others. However, this is probably
247 unrealistic as not all genes within an organism interact with each other (but see (45)). Livingstone et al. (46)
248 considered a network model based on the observed PPI network in yeast, with a broad connectivity distribution (i.e.
249 power-law-like network topology, see Box 1), in other words some genes were hubs with many interactions and
250 other genes were less interactive (see regulatory network in Figure 1). This leads to a slowing in the quadratic
251 growth of incompatibilities by a factor that equals the fraction of node pairs that are connected in the network, i.e.
252 the density of interactions, with lower density leading to slower increase in incompatibilities. Similarly, simulations
253 (47) show that areas of the network with high densities of interactions are predicted to accumulate incompatibilities
254 at faster rates in comparison to areas where interactions are sparse. However, this process may be opposed by
255 slower rates of substitutions at the more highly connected nodes due to pleiotropic constraint (5), as has been
256 repeatedly observed in both gene co-expression networks and PPI networks (see e.g. (7,48–50). Thus the rate of
257 accumulation of incompatibilities may be dramatically slowed compared to the snowball model (51)). Another
258 important consideration is the variance in the rate of accumulation of incompatibilities. Orr and Turelli (23)
259 investigated the effect of stochasticity in substitution rate and effect size on fitness, but to date studies have not
260 considered additional variance in the build-up of RI introduced by the power-law-like network topology. This type of
261 network topology could increase the variance in the rate of accumulation of RI, compared to networks of a similar
262 size, but with more evenly distributed connectedness. This means that species pairs could differ strongly in the rate
263 at which RI builds up, despite similar network topologies. Thus, the structure of interaction networks alone could
264 partly help explain why the strength of RI can differ dramatically between species pairs with similar genetic distance
265 (52), without invoking any additional differences between the species pairs.

266

267 *1.2.3 Co-evolution within a network and within-population positive epistasis can create strong localised barriers that*
268 *are persistent in the face of gene flow*

269

270 While early models of BDMs (1–3) consider only the deleterious consequences of epistasis, several recent studies
271 have explored the consequences of beneficial interactions, which could arise among loci that participate within the
272 same physical interaction network (53,54). Co-evolution between interacting loci (55) could occur through multiple
273 successive steps. The breaking of the resulting within-population ‘positive epistasis’ (53) in hybrids can lead to
274 effective species barriers. This has been shown in population genetic studies that examine the fate of
275 incompatibilities in the face of gene flow - a consideration that was often ignored in the past. Unlike BDMs in their
276 original formulation (where fit ancestral combination can be recovered by recombination), incompatibilities that
277 result from multi-step co-evolution in both populations are stable under gene flow, because fit recombinant
278 genotypes cannot be recreated. This is because ancestral alleles have been lost from both populations, or species, in
279 the process of multi-step co-evolution (24,54). Another relevant aspect of positive within-population epistasis is that
280 it becomes more likely as speciation progresses and more differences accumulate, analogous to the ‘snowball’
281 effect, but for positive interactions. This increases the chances that mutations whose direct effects are deleterious
282 can fix if their positive epistatic or pleiotropic effects outweigh their direct negative effects. Such mutations would
283 cause strongly negative fitness consequences when these positive epistatic effects are broken in hybrids. As a result,
284 within-population epistasis could explain a snowball-like effect that occurs not due to an acceleration in the *number*
285 of new incompatibilities, but due to increasing *strength* of negative fitness consequences with time (53).

286

287 *1.2.4 The mechanistic basis of interactions can be used to determine the shape of the fitness landscape*

288

289 The potential for system drift in an interaction network (e.g. regulatory network) depends on the number of
290 genotypes via which the network can produce phenotypes of equivalent fitness, and how accessible these
291 genotypes are through mutations. This information is equivalent to the shape of the fitness landscape. Models that
292 capture the biophysics of transcription factor-binding (10,39,56,57) implicitly define a fitness landscape, with an
293 important property: there are inherently many more ways to produce a moderately fit binding site than an optimally
294 fit one, implying large regions of genotype space of moderate fitness. There will therefore be more potential for
295 system drift in populations with sub-optimal regulatory pathways, such as small populations in which purifying
296 selection is less efficient. This highlights the value of models that consider the genotype-phenotype map: earlier
297 models using a fixed probability that a pair of substitutions will be incompatible found no effect of population size
298 when speciation is driven by drift alone (20). A perhaps counterintuitive result is that in large populations it is
299 phenotypes under the weakest selection that are most likely to accumulate the incompatibilities, as those are the

300 ones where genetic drift can still lead to the system drift (10). However, it remains to be studied how general such
301 predictions will be under different assumptions about the strength of selection and number of loci contributing to
302 the trait, and their precise interactions (note the criticisms of low-dimensional fitness landscapes in 1.1 above).

303

304 *Summary of PART 1*

305

306 Theoretical approaches to study the accumulation of RI vary in their level of mechanistic detail, generality and
307 tractability. From the existing theoretical work, some key findings on the role of multi-locus interactions in the build-
308 up of RI emerge. Broadly speaking, models with and without a mechanistic understanding of multi-locus interactions
309 both show that redundancy in the genotype (i.e. the fact that the same phenotype can be produced by multiple
310 combinations of genotypes) allows incompatibilities to accumulate. In both contexts, predictions about how easily
311 different genotypes can be reached through neutral evolution, and therefore how rapidly strong RI can evolve, are
312 determined by the shape of the fitness landscape. Taking into account the mechanistic understanding and structure
313 of multi-locus interactions allows for some additional insights. First, the mechanistic basis of interactions could itself
314 predict the shape of the fitness landscape, and therefore affect the likelihood of incompatibility accumulation.

315 Future work should aim to understand how features of realistic genotype-phenotype maps relate to features of
316 abstract fitness landscapes (58), and incorporate the empirical advances in understanding fitness landscapes (59,60)
317 into the theoretical models of speciation. Second, the number of interactions between loci influence the rate of
318 accumulation of incompatibilities, and heterogeneity in interactions within a network (*i.e.* some nodes are highly
319 connected, whereas others are not) could result in high variance in the rate of accumulation of incompatibilities and
320 in speciation probability. This should be explored in further theoretical work. Third, insights from the mechanistic
321 models could allow us to predict not only which kinds of loci are most likely to harbour incompatibilities (e.g. highly
322 connected, central nodes or nodes that connect modules) but also whether the incompatibilities are likely to persist
323 in the face of gene flow. Models that investigate the persistence of incompatibilities in the face of ongoing gene flow
324 are necessary to reveal the long-term consequences of incompatibilities for RI, and should therefore be a focus of
325 future work. Furthermore, in light of this special issue (see Introductory article), future work should compare
326 scenarios where RI is weak to those of strong RI, and study whether the role of different types of incompatibilities in
327 increasing RI differs between them. Finally, to be able to determine which models are most compatible with natural
328 systems we need tools to connect predictions from theories to empirical patterns seen in genome-wide data. This
329 could be achieved with simulations (54,61), which are discussed in more detail in Part 3. Next, we will discuss how
330 multi-locus interactions can be examined in empirical speciation studies.

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332

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334 **PART 2: How can multi-locus interactions be investigated in experimental speciation studies?**

335

336 Mapping of incompatibility loci using classical genetic techniques in model organisms have revealed how epistatic
337 fitness effects can produce strong reproductive barriers. For example, *Nup160* in *Drosophila* interacts with one or
338 more unknown additional factors in the autosomal background (62), and *DM2* that underlies hybrid necrosis in
339 *Arabidopsis* interacts with at least five different loci causing necrosis and problems in hybrids (63,64). In a few cases,
340 these mapping approaches have been extended to whole chromosome or whole genome scale (65,66), revealing
341 that there may be thousands of incompatibilities, many of which may have small effects, that contribute to species
342 barriers. However, such studies are limited not only in their resolution but also to species where elaborate crossing
343 experiments are possible. Recent developments in our ability to acquire genome-wide genetic or expression data for
344 population samples of non-model organisms now provide the potential to extend this field to detect signatures of
345 multi-locus interactions in non-model systems. In this section, we discuss genomic studies of naturally admixed
346 populations as well as hybrid gene misexpression studies that reveal putatively disrupted protein-protein or
347 regulatory interactions. We describe what such studies are beginning to reveal about the nature of species barriers,
348 and we also highlight challenges in using these approaches.

349 2.1 Admixed populations represent natural experiments where epistasis could be detected

350 Hybrid zones and admixed populations in which fit and unfit combinations of alleles continue to segregate in a single
351 population provide enhanced power and resolution to identify interactions that shape hybrid fitness. Turner and Harr
352 (67) performed a genome-wide association study (GWAS) for traits associated with sterility in the house mouse hybrid
353 zone. They found that most sterility-associated loci interact with more than one partner locus, and suggested that the
354 variation in effect size among loci is correlated with the number of different networks in which the gene participates.
355 These findings imply that models of speciation in which all pairs of loci can potentially interact (with a fixed probability of
356 producing an incompatibility) (22,23) are inaccurate, and models in which only certain interactions are possible (46) are
357 more likely to be realistic, due to the actual structure of the interactions.

358 When traits under selection in hybrids are not known, it is still possible to exploit admixed populations using naive scans
359 for the effects of epistatic selection. Ancestry Disequilibrium ('AD') scans attempt to identify pairs of loci at which there
360 are excessive statistical associations between allelic ancestry in admixed populations (68,69). In principle, AD scans could
361 identify pairs of interacting loci that lead to fitness breakdown in hybrids and thereby reveal the architecture of barriers
362 to gene flow and, together with genome annotation, the possible gene networks that underlie the barriers. Due to the
363 requirement of fertile hybrids and enough divergence to cause negative epistasis, AD scans are likely to be most useful
364 mid to later rather than early on in the speciation process. However, within-species detection of weak epistatic
365 incompatibilities can be achieved with sufficient power (68), and may be particularly sensitive when candidate loci are

366 known, such as mitochondria and their nuclear interacting partners (70). Using an AD scan, Pool (68) found evidence for
367 epistasis and hub-like (one-to-many) interactions causing reduced fitness in an admixed *Drosophila melanogaster*
368 population. One shortfall of AD scans is that they require existing polymorphism at both loci in the admixed population in
369 order to detect ancestry disequilibrium. Therefore, the strongest incompatibilities may go undetected as selection could
370 already have led to the fixation of one parental genotype at both loci, leaving only the weaker incompatibilities to be
371 detected (61,68,71). Other concerns are that multiple testing of all possible pairs of loci leads to a high likelihood of false
372 positives just due to chance, and that the AD scans assume random mating within the population, as non-random mating
373 will also result in statistical association between unlinked regions of the genome in mixed populations. These issues can
374 be partly alleviated by examining the overlap between candidate incompatibilities in independent admixed populations
375 (69), identification of 'hub-like' interactions that involve the same gene multiple times; or investigating whether the
376 candidate genes are known to participate in the same pathways (68). For example, a recent study documented signatures
377 of epistatic selection on archaic introgression in humans by combining information on introgressed genes, their co-
378 segregation and functional information about the biological pathways in which they function (72).

379 2.2 Genome scans combined with additional functional information could reveal multi-locus interactions

380 Even when natural hybrids are rare or absent, analysis of genetic differentiation along the genome between diverging
381 populations can reveal loci at which selection has resisted genetic exchange between the populations in the past,
382 therefore indicating likely loci contributing to the genomic barrier (73–76). Genome scans are easy to perform, and in
383 contrast to AD scans do not require that pairs of incompatible alleles are segregating as polymorphisms in a hybrid
384 population. Furthermore, genome scans are uniquely able to detect signals of weak selection accumulated over multiple
385 generations which could be missed by experimental studies or AD scans that focus on selection over a single generation
386 (77). However, genome scans become less useful the further the speciation process proceeds as the signatures of
387 selection against foreign alleles may be difficult to distinguish from those of confounding processes such as purifying
388 selection acting within the diverging lineages (78–80). Estimating effective migration rate instead of divergence along the
389 genome holds promise to increase our understanding of later stages of the speciation process in the future (18,76,77).
390 Unlike incompatibilities that are also involved in local adaptation, those incompatibilities whose fitness effects depend
391 only on the genetic background will not necessarily produce localised barriers that persist in the face of gene flow,
392 particularly if it is possible to 'rescue' hybrid fitness through recombination to regenerate fit combinations of alleles
393 (24,54,81). By contrast, incompatibilities that emerge through multi-step co-evolution between interacting loci in both
394 populations can generate persistent, localised barriers to gene flow (54). Therefore, this form of co-evolved
395 incompatibility is most likely to be detectable by genome scans.

396 Unlike AD scans, differentiation scans do not directly reveal whether epistasis between loci underlies barriers to gene
397 flow. Instead, the genome scan can be used as a first step in inference, after which other methods are needed to test for

398 interactions at the molecular level, or epistasis. One approach to make these links is to test whether candidate barrier
399 loci show experimental evidence for epistasis in natural or artificial hybrids. Such an epistatic interaction has been
400 demonstrated between loci underlying plumage divergence in crows (82). Another approach is to ask whether the
401 candidate loci show interactions at the molecular level, which could be a potential indicator of epistatic interactions, an
402 approach utilized by Kulmuni et al. (83). Using information from the String database (84) they found that a large
403 proportion of putative barrier loci identified between hybridizing species of wood ants are known to form part of a single
404 interaction network in *Drosophila*. Interestingly, random samples from the same marker set (including loci not thought to
405 be involved in barriers), identified similar interactivity. This might imply that any large-enough gene set would include
406 many members known to interact biologically, hampering the identification of true epistatic interactions underlying RI.
407 There are also empirical methods to detect protein-protein interactions, like pull-down assays (reviewed in (85)), that can
408 be utilized after identification of candidate genes. However, we still know very little about how interactions between loci
409 at the molecular level translate into epistasis that is relevant for specific traits or individual fitness.

410

411 2.3 Gene expression can be utilized to find disrupted gene regulation in hybrids

412

413 Phenotypic evolution and adaptation involve divergence in gene regulation. Particularly early in divergence,
414 regulatory differences appear to accumulate more rapidly than amino acid substitutions in protein sequences
415 (86,87). Gene expression is controlled by cis- and trans-acting factors, and co-evolution between regulatory factors
416 within a lineage can result in misexpression and breakdown in hybrids (55,88). These findings are consistent with
417 models described in Part 1.2, in which regulatory changes can emerge at multiple loci without a change in the
418 overall phenotype. The combination of such diverged regulatory networks in hybrids can cause their gene
419 expression profiles to be distinct from those of both parental populations. Several recent studies have described
420 gene 'mis-regulation' in hybrids (e.g. (89–93)). Mis-regulation in F1 hybrids is indicative of epistasis that could
421 underlie reduced hybrid fitness, and therefore RI. Although hundreds or even thousands of individual genes can be
422 misexpressed in hybrids, these differences could come about through modifications at a smaller number of key
423 regulatory nodes in complex networks (94). This is shown by Turner et al. (93) who mapped interactions between
424 expression QTLs and genotypes in the case of house mouse hybrid sterility. They found complex regulatory
425 interactions across the genome, with a single eQTL interacting with 17 to >1000 partners, suggesting that regulatory
426 divergence at many genes could be explained by evolution of a relatively small number of master regulators. Gene
427 expression data can also be used to reveal networks of co-expressed genes (95). Comparing co-expression networks
428 in hybrids and parental populations can reveal whole networks disrupted in hybrids as opposed to individual genes
429 (96). While gene expression studies in hybrids reveal possible candidates for gene interactions underlying speciation,
430 they do not directly demonstrate the fitness consequences of changes in hybrid expression. Indeed, hybrids are
431 sometimes more fit than the parental populations. Making the links between regulatory interactions, hybrid

432 misexpression and fitness can be achieved by comparing multi-locus genotypes and their gene expression patterns
433 in fit and unfit classes of hybrids (93).

434

435 *Summary of PART 2*

436 Future studies that combine genome scan, AD scan and gene expression analyses in hybrids are likely to help in detecting
437 interactions underlying RI. Using any one of these approaches alone can be biased by false positives or confounding
438 signals, but overlapping information from multiple approaches can help to narrow down candidate interactions. Genome
439 scans will be most useful early on in speciation, AD scans later on in the process (provided admixed populations are
440 available) and hybrid misexpression and co-expression network studies potentially informative at any point in the
441 speciation continuum. Where possible, signatures of selection against incompatible combinations of alleles could be
442 measured in real-time, e.g. by comparing early and late developmental stages, which could provide further evidence for
443 interactions (97). On top of that, if the time window of hybrid breakdown is known, gene co-expression network analyses
444 could identify networks disrupted in hybrids. A completely opposite approach to these different types of scans would be
445 to investigate classes of loci with high or low levels of known physical interactions and characterize average levels of
446 differentiation and inferred rates of effective gene flow for these. As Shih (47) demonstrated with undirected (e.g. PPI)
447 networks, this data can reveal whether physically highly connected genes are more likely to be involved in interactions
448 disrupted by mutations than less connected genes on average. Finally, in the future there is a clear need for approaches
449 connecting mechanistic understanding of gene interactions, population genetic theory and empirical genomic data.

450

451 **PART 3: Conclusions and future directions**

452

453 The idea that gene interactions and epistasis are central to speciation is over a century old. Much of the progress has
454 been made by modelling epistasis without a detailed mechanistic understanding of gene interactions. Recent
455 models that explicitly consider the structure of multi-locus interactions and how they produce phenotypes, have in
456 many ways recapitulated earlier results, but have allowed prediction of some novel patterns that are consistent with
457 empirical data. These include a high variance in the rate of build-up of RI among taxa, the emergence of strong
458 incompatibilities that produce localised barriers to introgression, and an effect of population size on the build-up of
459 RI. Experimental approaches that use genome-scale data have proved useful to detect putative interactions leading
460 to epistatic fitness effects and RI, but they have generally been utilized in isolation. Combining ancestry
461 disequilibrium (AD) scans, genome scans, hybrid gene expression and assays of hybrid phenotypes and fitness could
462 overcome the shortfalls of individual methods in the future, and provide stronger evidence for the involvement of
463 particular loci in interactions resulting in hybrid breakdown. In addition to identifying particular interactions,
464 ultimately, one would like to test predictions from theory using empirical genomic data. In order to do this, we need

465 to predict what kind of patterns incompatibilities will leave in genome-wide polymorphism data, if any. Thus, we
466 propose a key need for the future: studies and tools that link between theory and experimental studies. Cross-talk
467 between theory and empirical work can facilitate interpreting genome scan results, for example, but also help point
468 to gene characteristics (like pleiotropy) that should be enriched among barrier loci.

469

470 Future studies should help bridge theory and empirical work by answering the following needs. First, there is a need
471 to test the persistence of multi-locus incompatibilities in the face of long-term gene flow, which is likely in nature
472 and will determine what patterns incompatibilities could leave in genomic data (54). An additional aim here is to
473 determine whether genomic approaches would have sufficient power to detect multi-locus incompatibilities (61).
474 Second, there is a need for testable predictions about the patterns different processes of incompatibility
475 accumulation leave at the genomic level. This is important as models incorporating different selective and genetic
476 mechanisms (snowball models, system drift models, tipping point models (98) etc.) may predict similar broad-scale
477 patterns, such as faster than linear accumulation of incompatibilities at some point of the speciation process.
478 However, different processes of incompatibility accumulation may leave different signatures in the genome. For
479 example, neutral or nearly neutral processes are unlikely to cause large selective sweeps in genomes, as have been
480 seen under local adaptation based on few major effect loci (99). Third, there is a need to model highly-polygenic and
481 pleiotropic genome-wide architecture of traits (*i.e.* the omnigenic model (45)) leading to incompatibilities. This is
482 relevant, because the effects of such a complex polygenic architecture will be distinct from the effects of
483 architectures with fewer loci. Indeed, even polygenic models without interactions can reveal non-linearities not
484 observed in models with small numbers of loci (98). Finally, there is a need to model the temporal time scale to
485 understand the processes occurring early versus later in the build-up of RI, as the relative role of multi-locus
486 interactions could change as speciation progresses.

487

488 One potential tool to bridge between theory and observed genomic data are simulations. This is now achievable
489 thanks to the availability of efficient tools for both coalescent (100) and forward genetic (101) simulations in a
490 genome-wide setting with large numbers of selected loci and complex selection regimes (101). Simulations could
491 begin to answer how incompatibilities arising from multi-locus interactions translate into patterns that could be
492 detected in population genomic studies, an approach that was successfully utilized e.g. in (54). Furthermore, studies
493 not focusing on epistasis per se have successfully employed simulations to investigate RI in a genome- or
494 chromosome-wide setting (16,102–104). Importantly, simulations also allow us to account for the noisy nature of
495 genomic data: each speciation event represents a single realisation of a stochastic evolutionary process (105).
496 Simulations could be utilized in conjunction with empirical data to fit different models of incompatibility
497 accumulation, gene flow and demography to make inferences about the nature of real species barriers, and

498 importantly ask if the observed data could be explained by a neutral model. They could potentially allow
499 distinguishing diagnostic differences between multi-locus incompatibilities and confounding processes.

500 Looking beyond speciation, there is also a need to better understand multi-locus interactions. How do protein interaction
501 networks relate to regulatory networks and how do these translate into fitness landscapes? How do multi-locus
502 interactions evolve over short and long evolutionary time scales and how do changes in network topology and
503 connectivity affect phenotypes and fitness? Much progress in this direction has been made recently (e.g. (7,8,106–108)).

504

505 **Acknowledgments**

506

507 We would like to thank Dorothea Lindtke, Tobias Uller, Pierre Nouhaud, two anonymous reviewers and the editor
508 Anja Westram for useful feedback that greatly improved our manuscript.

509

510 **References**

511

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