

3  
4 Running Title: *Sex ratios: heritability and theory*

5  
6  
7  
8 **Does the lack of heritability of human sex ratios require a rethink of**  
9 **sex ratio theory? No: a response to Zietsch *et al.* 2020**

10  
11  
12  
13  
14 Steven Hecht Orzack, Fresh Pond Research Institute, Cambridge, MA 02140, USA. Email:  
15 orzack@freshpond.org (ORCID ID: 0000-0002-4993-3368)

16  
17 Ian C.W. Hardy\*, School of Biosciences, University of Nottingham, Sutton Bonington Campus,  
18 Loughborough, LE12 5RD, UK. Email: ian.hardy@nottingham.ac.uk (ORCID ID: 0000-  
19 0002-5846-3150)

20  
21  
22 *\*Corresponding author: Dr Ian C.W. Hardy, School of Biosciences, University of Nottingham,*  
23 *Sutton Bonington Campus, Loughborough, LE12 5RD, UK*  
24 *Tel: +44 (0) 115 9516177*  
25 *Email: ian.hardy@nottingham.ac.uk.*

26  
27 *From 1<sup>st</sup> April 2021: Department of Agricultural Sciences, P.O. Box 27, Viikki Campus,*  
28 *University of Helsinki, Finland*

29  
30 **Keywords:** Düsing-Fisher theory, heritability, human sex ratios, sex allocation.

32           Zietsch et al. (2020) estimated the heritability of the sex ratio at birth in humans by  
33 measuring the association between the sex ratios produced by over 14 million Swedish sibling  
34 pairs. The heritability estimate was 0.00058, with a 95% confidence interval of -0.00076 - 0.00196.  
35 They concluded that the sex ratio differences observed among the families of siblings are not due to  
36 genetic differences in the tendency to produce one sex more than the other. Zietsch et al. also  
37 concluded that this result renders (p.1) “Fisher’s principle untenable ... [as a framework] for  
38 understanding human offspring sex ratio”. Here, we discuss why the latter conclusion is incorrect.

39           Düsing (1884) created the theoretical framework from which our understanding of sex ratio  
40 evolution derives. This framework was then elaborated in important ways by, among others, Fisher  
41 (1930), Shaw and Mohler (1953), Shaw (1955, 1958), Kolman (1960), MacArthur (1965),  
42 Hamilton (1967), Leigh (1970), Charlesworth (1977, 1994), Kahn et al. (2015) and Argasinski and  
43 Broom (2020). Overviews of the current state of theory and its empirical application can be found  
44 in Charnov (1982), Bull and Charnov (1988), Karlin and Lessard (1986), Wrensch and Ebbert  
45 (1993), Hardy (2002) and West (2009). A key result of this theory is that there can be an “equal  
46 investment” equilibrium resulting from the action of natural selection in a randomly-mating  
47 population. It occurs when the cumulative resource invested in female offspring and the cumulative  
48 resource invested in male offspring are equal at the end of parental investment. If the ratio of  
49 resource investments is 1 and females and males have identical mortality rates, the equilibrium  
50 occurs when there are equal proportions of females and males in the mating pool of adults. This is  
51 often referred to as the 1:1 sex ratio equilibrium. If the cumulative resource investments are not  
52 equal, the evolutionary equilibrium is an unequal numerical sex ratio, with the more costly sex  
53 being in the minority.

54           What is the evolutionary process that can result in the evolution of the equal investment  
55 equilibrium? Consider the case when females and males are equally costly to produce and have  
56 identical mortality rates. If equal proportions of females and males are not present in the mating  
57 pool, parents that produce more of the rarer sex will leave more descendants. If the tendency to  
58 produce the rarer sex is inherited, these descendants will also produce more offspring of the rarer  
59 sex. This decreases the sex ratio bias in the mating pool formed by these offspring, which means  
60 that the advantage of producing the rarer sex decreases. This dynamic attains an evolutionary  
61 equilibrium only when both sexes have equal proportions in the mating pool. This equilibrium is  
62 consistent with the absence or presence of genetic variation influencing the sex ratio (see below).

63 Empirical investigations confirm that this process of “frequency-dependent” natural selection can  
64 result in the attainment of this evolutionary equilibrium (e.g., Conover and Van Voorhees 1990;  
65 Basolo 1994). Additional theory describes the conditions under which the equilibrium sex ratio  
66 produced by the population is predicted to be produced by each individual or mated pair (see  
67 Orzack and Hines 2005 and references therein). Zietsch et al. denote as “Fisher’s principle” the  
68 process by which individuals producing the rarer sex have an evolutionary advantage, which  
69 thereby increases the frequency of the sex they produce: we refer to it as the “Düsing-Fisher  
70 principle”.

71         For the Düsing-Fisher principle to cause the sex ratio to evolve, offspring sex ratio must be  
72 inherited from parents to offspring, at least in part, and there must be inherited variation among  
73 individuals or couples in regard to the offspring sex ratio they produce (the latter condition is that  
74 the trait be “heritable”, see Falconer and Mackay 1996 for the distinction between this condition  
75 and the condition that a trait be inherited). However, contrary to the claims of Zietsch et al. (2020),  
76 the Düsing-Fisher principle makes no inference that the sex ratio be heritable *at the evolutionary*  
77 *equilibrium*. For example, a 1:1 sex ratio equilibrium is consistent with, say, each individual having  
78 a genotype that causes them to produce the same 1:1 sex ratio (not heritable) or with half of them  
79 having a genotype that causes them to produce all daughters and half of them having a genotype  
80 that causes them to produce all sons (“maximally” heritable; cf., Patterson 1928). No implication  
81 about the realized importance of the Düsing-Fisher principle as an evolutionary explanation for the  
82 human sex ratio can be drawn from the fact that the sex ratio is not heritable in the Swedish sample.  
83 The evolutionary equilibrium arising from the Düsing-Fisher principle is like those arising in many  
84 other evolutionary contexts: the attainment of the equilibrium erases the evidence of the causal  
85 process that led to its evolution (e.g., Hartl et al. 1985). Therefore, Zietsch et al.’s results do not  
86 render the Düsing-Fisher principle inherently untenable as a framework for understanding the  
87 evolution of the human offspring sex ratio. In this context, we note that Zietsch et al. appear to  
88 assume that the absence of genetic variation for the sex ratio at birth implies that there is no genetic  
89 variation for the human sex ratio at any age, especially the later age at which the evolutionary  
90 equilibrium attained by the Düsing-Fisher principle might be attained. There is no reason that this  
91 assumption must be true, especially given the age-specificity of the expression of many traits (e.g.,  
92 Leips et al. 2006).

93           Zietsch et al. conclude (p. 6) that their results are consistent with “the simple explanation  
94 that variation in offspring sex ratio in humans is due to unbiased Mendelian segregation of sex  
95 chromosomes during spermatogenesis and unbiased fertilization”. This is correct, although it does  
96 not have precedence over the Düsing-Fisher principle as an evolutionary explanation. In human  
97 spermatogenesis, meiosis results in the production of statistically-equal proportions of gametes  
98 containing an X chromosome and of those containing a Y chromosome and equal numbers of  
99 females and males appear to be conceived (see results and discussion in Orzack et al. 2015). These  
100 outcomes could be the result of natural selection for “honest meiosis” (Leigh 1977) and thereby not  
101 arise from natural selection on the sex ratio in a direct sense. However, both processes of natural  
102 selection could operate or have operated simultaneously. It is also possible that the XY process of  
103 sex determination is an outcome of natural selection for a 1:1 sex ratio. Even if natural selection on  
104 the sex ratio was the sole evolutionary influence on the human sex ratio in the past, it is arguable  
105 that the extent to which the Düsing-Fisher principle, or other adaptive sex ratio processes, can  
106 operate currently is greatly limited by the presence of chromosomal sex determination (Williams  
107 1979). We note in this context that investigators seeking an adaptive explanation for the human sex  
108 ratio sometimes implicitly assume that it has evolved via natural selection within *Homo sapiens*.  
109 There is no compelling reason to think that this is true and there is evidence to indicate that it is not.  
110 For example, estimates of the sex ratio at birth vary among primates, but many are statistically  
111 similar to the male-bias observed in many human populations or to a 1:1 sex ratio at birth  
112 (Sugiyama 2004; White 2009; Bronikowski et al. 2016). Similarly, post-birth age-specific mortality  
113 rates are lower for females than for males in several primate species, just as in humans  
114 (Bronikowski et al. 2011). Evolutionary explanations for the sex ratios observed among primate  
115 species remain controversial (e.g., Schino 2004; Silk et al. 2005). Whatever the conclusion about  
116 the adaptive significance of sex ratios in other primates, it is essential to assess the influence of  
117 evolutionary history when attempting to understand the evolution of human sex ratios. Even if one  
118 assumes that the Düsing-Fisher principle is the evolutionary explanation for the human sex ratio,  
119 this does not identify when this process of natural selection occurred. It could, for example, have  
120 occurred when mammals evolved in the Mesozoic, when primates evolved in the Paleocene, or  
121 more recently when apes evolved in the Oligocene. If so, the sex ratio of *Homo sapiens* would be at  
122 least in part a result of past evolution, instead of being entirely a result of current evolution in  
123 human populations, and indeed this potential influence of past evolution is mentioned by Zietsch et  
124 al. (p. 7). Consideration of the influence of such “phylogenetic inertia” (Felsenstein 1985; Hansen

125 and Orzack 2005) is rare among analyses that attempt to compare the predictions of sex allocation  
126 theory to data from humans and other vertebrates and can render their conclusions ambiguous.

127 Finally, we comment more broadly on what is and is not known about the evolution of the  
128 human sex ratio. The sex ratio at birth in most populations is slightly, but significantly, biased  
129 towards males (Garenne 2002, 2008; Mathews and Hamilton 2005; Chao et al. 2019; Zietsch et al.  
130 2020) and thereafter is statistically equal for only a small portion of a cohort's existence. Neither  
131 fact can be interpreted as evidence for or against the Düsing-Fisher principle, and sex allocation  
132 theory more generally, given the absence of evidence about the empirical validity of the  
133 assumptions underlying the equal investment equilibrium. For example, there is extensive evidence  
134 for non-random mating within and between human populations but its influence on the evolutionary  
135 success of individuals or couples producing different sex ratios remains unclear. In addition, the age  
136 at which resource investment by parents ends is poorly known at best for humans and many other  
137 species. To this extent, the age(s) at which the observed sex ratio should be compared with the sex  
138 ratio predicted by the Düsing-Fisher principle are unknown.

139

## 140 **Conclusion**

141 Attaining a full understanding of the evolutionary basis for human sex ratio biology is  
142 challenging at best and is likely unattainable. Important reasons for this are the subtle sex ratio  
143 effects predicted for humans by sex ratio theory, cultural practices, such as son preference (e.g.,  
144 Malpani et al. 2002) and sex-balancing of families (e.g., Pennings 1996) that can obscure the  
145 influence of natural selection, plus ethical constraints on experimentation (Lazarus 2002; Mace and  
146 Jordan 2005; West and Burton-Chellew 2013; Hardy and Maalouf 2017; Gellatly 2020)

147 The substantial evidence provided by Zietsch et al. (2020) leaves little doubt that differences  
148 among siblings in regard to the sex ratio at birth of offspring they produce are not due to inherited  
149 differences. However, this absence of inherited variation is not evidence against the claim that  
150 Düsing-Fisher frequency-dependent selection has influenced the human sex ratio. Nonetheless, if  
151 and when this process of natural selection has influenced the human sex ratio remains unresolved.

152

153

154

155 **Acknowledgments**

156 We thank Brendan Zietsch, Andy Gardner, Loeske Kruuk, an anonymous associate editor, and two  
157 anonymous referees for comments. We also thank Jussi Lehtonen for discussion.

158

159 **Authors' contributions statement**

160 The order of authorship was determined randomly, with equal contributions.

161

162 **Ethics statement**

163 The authors know of no ethical concerns associated with this commentary.

164

165 **Data accessibility statement**

166 There are no data associated with this commentary.

167

168 **Competing interests statement**

169 The authors declare no competing interests.

170

171

172 **References**

173 Argasinski, K., and M. Broom. 2020: Towards a replicator dynamics model of age structured  
174 populations. *Journal of Mathematical Biology* In press.`

175 Basolo, A. L. 1994: The dynamics of Fisherian sex-ratio evolution: theoretical and experimental  
176 investigations. *American Naturalist* 144:473–490.

177 Bronikowski, A. M., J. Altmann, D. K. Brockman, M. Cords, L. M. Fedigan, A. Pusey, T. Stoinski,  
178 W. F. Morris, K. B. Strier, and S. C. Alberts. 2011: Aging in the natural world: comparative  
179 data reveal similar mortality patterns across primates. *Science* 331:1325–1328.

180 Bronikowski, A. M., M. Cords, S. C. Alberts, J. Altmann, D. K. Brockman, L. M. Fedigan, A.  
181 Pusey, T. Stoinski, K. B. Strier, and W. F. Morris. 2016: Female and male life tables for seven  
182 wild primate species. *Scientific Data* 3:160006.

183 Bull, J. J., and E. L. Charnov. 1988: How fundamental are Fisherian sex ratios? *Oxford Surveys in*  
184 *Evolutionary Biology* 5:96–135.

185 Chao, F., P. Gerland, A. R. Cook, and L. Alkema. 2019: Systematic assessment of the sex ratio at  
186 birth for all countries and estimation of national imbalances and regional reference levels.

187        Proceedings of the National Academy of Sciences 116:9303–9311.

188 Charlesworth, B. 1977: Population genetics, demography and the sex ratio. Pp.345–363 *in* F. B.

189        Christiansen and T. M. Fenchel, eds. *Measuring Selection in Natural Populations*. Springer

190        Verlag, Berlin.

191        ———. 1994: *Evolution in age-structured populations*. Cambridge University Press, New York.

192 Charnov, E. L. 1982: *The Theory of Sex Allocation*. Princeton University Press, Princeton.

193 Conover, D. O., and D. A. Van Voorhees. 1990: Evolution of a balanced sex ratio by frequency-

194        dependent selection in a fish. *Science* 250:1556–1558.

195 Düsing, C. 1884: Die Regulierung des Geschlechtsverhältnisses bei der Vermehrung der Menschen,

196        Tiere, und Pflanzen. *Jenaische Zeitschrift für Naturwissenschaft* 17:593–940.

197 Falconer, D. S., and T. F. C. Mackay. 1996: *Introduction to Quantitative Genetics*. Longman,

198        Essex,.

199 Felsenstein, J. 1985: Phylogenies and the comparative method. *The American Naturalist* 125:1–15.

200 Fisher, R. A. 1930: *The Genetical Theory of Natural Selection*. Clarendon Press, Oxford.

201 Garenne, M. 2002: Sex ratios at birth in African populations: a review of survey data. *Human*

202        *Biology* 74:889–900.

203        ———. 2008: Heterogeneity in the sex ratio at birth in European populations. *Genus* 64:99–108.

204 Gellatly, C. 2020: The sex ratio: A biological and statistical conundrum. *Current Biology*

205        30:R1261–R1263.

206 Hamilton, W. D. 1967: Extraordinary sex ratios. *Science* 156:477–488.

207 Hansen, T. F., and S. H. Orzack. 2005: Assessing current adaptation and phylogenetic inertia as

208        explanations of trait evolution: the need for controlled comparisons. *Evolution* 59:2063–2072.

209 Hardy, I. C. W. 2002: *Sex Ratios: Concepts and Research Methods*. Cambridge University Press,

210        Cambridge.

211 Hardy, I. C. W., and W. E. Maalouf. 2017: Partially-constrained sex allocation and the indirect

212        effects of assisted reproductive technologies on the human sex ratio. *Journal of Biosocial*

213        *Science* 49:281–291.

214 Hartl, D. L., D. E. Dykhuizen, and A. M. Dean. 1985: Limits of adaptation: the evolution of

215        selective neutrality. *Genetics* 111:655–674.

216 Kahn, A. T., M. D. Jennions, and H. Kokko. 2015: Sex allocation, juvenile mortality and the costs

217        imposed by offspring on parents and siblings. *Journal of Evolutionary Biology* 28:428–437.

218 Karlin, S., and S. Lessard. 1986: *Theoretical studies on sex ratio evolution*. Princeton University

219 Press, Princeton, N.J.

220 Kolman, W. A. 1960: The mechanism of natural selection for the sex ratio. *The American*  
221 *Naturalist* 94:373–377.

222 Lazarus, J. 2002: Human sex ratios: adaptations and mechanisms, problems and prospects. Pp.287–  
223 311 *in* I. C. W. Hardy, ed. *Sex Ratios: Concepts and Research Methods*. Vol. 1. Cambridge  
224 University Press, Cambridge.

225 Leigh, E. G. J. 1970: Sex ratio and differential mortality between the sexes. *American Naturalist*  
226 104:205–210.

227 ———. 1977: How does selection reconcile individual advantage with the good of the group?  
228 *Proceedings of the National Academy of Sciences* 74:4542–4546.

229 Leips, J., P. Gilligan, and T. F. C. Mackay. 2006: Quantitative trait loci with age-specific effects on  
230 fecundity in *Drosophila melanogaster*. *Genetics* 172:1595–1605.

231 MacArthur, R. H. 1965: Ecological consequences of natural selection. Pp.389–397 *in* T. H.  
232 Waterman and H. J. Morowitz, eds. *Theoretical and Mathematical Biology*. Blaisdell, New  
233 York.

234 Mace, R., and F. Jordan. 2005: The evolution of human sex-ratio at birth: a bio-cultural analysis.  
235 Pp.207–216 *in* R. Mace, C. J. Holden, and S. Shennan, eds. *The Evolution of Cultural*  
236 *Diversity: A Phylogenetic Approach*. University College London Press, London.

237 Malpani, A., A. Malpani, and D. Modi. 2002: Preimplantation sex selection for family balancing in  
238 India. *Human reproduction* 17:11–12.

239 Mathews, T. J., and B. E. Hamilton. 2005: Trend analysis of the sex ratio at birth in the United  
240 States. *National Vital Statistics Reports* 53:1–17.

241 Orzack, S. H., and W. G. S. Hines. 2005: The evolution of strategy variation: will an ESS evolve?  
242 *Evolution* 59:1183–1193.

243 Orzack, S. H., J. W. Stubblefield, V. R. Akmaev, P. Colls, S. Munné, T. Scholl, D. Steinsaltz, and  
244 J. E. Zuckerman. 2015: The human sex ratio from conception to birth. *Proceedings of the*  
245 *National Academy of Sciences* 112:E2102–E2111.

246 Patterson, J. T. 1928: Sexes in the cynipidae and male-producing and female-producing lines. *The*  
247 *Biological Bulletin* 54:201–211.

248 Pennings, G. 1996: Ethics of sex selection for family balancing: Family balancing as a morally  
249 acceptable application of sex selection. *Human Reproduction* 11:2339–2342.

250 Schino, G. 2004: Birth sex ratio and social rank: consistency and variability within and between

251 primate groups. *Behavioral Ecology* 15:850–856.

252 Shaw, R. F. 1955: The population genetics of the sex ratio. University of California, Berkeleypp.

253 ———. 1958: The theoretical genetics of the sex ratio. *Genetics* 43:149–163.

254 Shaw, R. F., and J. D. Mohler. 1953: The selective significance of the sex ratio. *The American*

255 *Naturalist* 87:337–342.

256 Silk, J. B., E. Willoughby, and G. R. Brown. 2005: Maternal rank and local resource competition

257 do not predict birth sex ratios in wild baboons. *Proceedings of the Royal Society B: Biological*

258 *Sciences* 272:859–864.

259 Sugiyama, Y. 2004: Demographic parameters and life history of chimpanzees at Bossou, Guinea.

260 *American Journal of Physical Anthropology* 124:154–165.

261 West, S. A. 2009: *Sex Allocation*. Princeton University Press, Princeton.

262 West, S. A., and M. N. Burton-Chellew. 2013: Human behavioral ecology. *Behavioral Ecology*

263 24:1043–1045.

264 White, F. J. 2009: Sex ratio at birth and age-reversed dominance among female *Varecia*. *Folia*

265 *Primatologica* 80:341–352.

266 Williams, G. C. 1979: The question of adaptive sex ratio in outcrossed vertebrates. *Proceedings of*

267 *the Royal Society of London B: Biological Sciences* 205:567–580.

268 Wrensch, D. L., and M. A. Ebbert. 1993: *Evolution and Diversity of Sex Ratio in insects and Mites*.

269 Chapman and Hall, New York,

270 Zietsch, B. P., H. Walum, P. Lichtenstein, K. J. H. Verweij, and R. Kuja-Halkola. 2020: No genetic

271 contribution to variation in human offspring sex ratio: a total population study of 4.7 million

272 births. *Proceedings of the Royal Society B: Biological Sciences* 287:20192849.

273