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Phriksee, Anirut

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Weak lensing analysis of CODEX clusters using dark energy camera legacy survey: mass–richness relation

Anirut Phriksee,^{1,2★} Eric Jullo,¹ Marceau Limousin,¹ HuanYuan Shan,³
Alexis Finoguenov,⁴ Siramas Komonjinda,^{5,6} Suwicha Wannawichian^{5,6}
and Utane Sawangwit⁷

¹Aix Marseille Univ, CNRS, CNES, LAM, 13388 Marseille, France

²Ph.D. Program in Physics, Department of Physics and Materials Science, Faculty of Science, Chiang Mai University, 50200 Chiang Mai, Thailand

³Shanghai Astronomical Observatory, 200030 Shanghai, China

⁴Department of Physics, University of Helsinki, 00014 Helsinki, Finland

⁵Department of Physics and Materials Science, Faculty of Science, Chiang Mai University, 50200 Chiang Mai, Thailand

⁶Research Center in Physics and Astronomy, Faculty of Science, Chiang Mai University, 50200 Chiang Mai, Thailand

⁷National Astronomical Research Institute of Thailand, 50180 Chiang Mai, Thailand

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ABSTRACT

We present the weak-lensing analysis of 279 CODEX clusters using imaging data from 4200 deg² of the DECam Legacy Survey (DECaLS) Data Release 3. The cluster sample results from a joint selection in X-ray, optical richness in the range $20 \leq \lambda < 110$, and redshift in the range $0.1 \leq z \leq 0.2$. We model the cluster mass (M_{200c}) and the richness relation with the expression $\langle M_{200c} | \lambda \rangle \propto M_0 (\lambda/40)^{F_\lambda}$. By measuring the CODEX cluster sample as an individual cluster, we obtain the best-fitting values, $M_0 = 3.24^{+0.29}_{-0.27} \times 10^{14} M_\odot$, and $F_\lambda = 1.00^{+0.22}_{-0.22}$ for the richness scaling index, consistent with a power-law relation. Moreover, we separate the cluster sample into three richness groups; $\lambda = 20$ –30, 30–50, and 50–110, and measure the stacked excess surface mass density profile in each group. The results show that both methods are consistent. In addition, we find an excellent agreement between our weak lensing based scaling relation and the relation obtained with dynamical masses estimated from cluster member velocity dispersions measured by the SDSS-IV/SPIDERS team. This suggests that the cluster dynamical equilibrium assumption involved in the dynamical mass estimates is statistically robust for a large sample of clusters.

Key words: gravitational lensing: weak – galaxy: clusters: general – large-scale structure of Universe.

1 INTRODUCTION

Presently, the most accurate model to describe the universe is called the lambda cold dark matter (Λ CDM) model, also known as the standard cosmological model. Observations suggest that baryons represent a few percent of the energy content of matter in the universe. The rest, identified as dark energy and dark matter, remains today relatively unexplained (e.g. Planck Collaboration XIII 2016a). Dark energy is responsible for the recent acceleration in the expansion of the universe. Assuming it would be homogeneous and isotropic, the accelerated expansion would imply this medium to have a negative pressure. Other models rather propose to modify the equations of general relativity on the largest scales of the universe to account for the accelerating expansion. Dark matter, probably

an elementary particle still to be discovered, accumulates in large structures of the universe, such as galaxies, clusters of galaxies and cosmic filaments under the effect of gravity.

Galaxy clusters, the last structures formed in the universe, are very exciting objects for cosmological studies. First, they have a well-defined mass function, whose shape reflects the value of cosmological parameters (Press & Schechter 1974; Warren et al. 2006; Tinker et al. 2008; Bhattacharya et al. 2011; Despali et al. 2016; McClintock et al. 2019b). Secondly, numerical simulations predict characteristic density profile (e.g. NFW profile; Navarro, Frenk & White 1996, 1997; Limousin et al. 2013; Diemer & Kravtsov 2014; Bose et al. 2017, Einasto profile; Einasto 1965; Hayashi & White 2008; Diemer & Kravtsov 2014), sub-halo mass function and triaxiality (Becker & Kravtsov 2011; Angulo et al. 2012; Noh & Cohn 2012), which depend on the properties of the dark matter particles, although in reality, astrophysical effects tend to mask these effects (e.g. Newman et al. 2013). Finally, their gas-

★ E-mail: anirut.phriksee@cmu.ac.th

mass ratios reflect the cosmological content (e.g. Allen et al. 2008; Mantz et al. 2016a).

Due to their complex internal physical processes, and their extreme masses, galaxy-clusters have been observed at all wavelengths from X-ray to radio, and large surveys now give us a comprehensive view of their distribution and evolution with time. Cluster mass can be determined from their X-ray brightness, temperature (e.g. Sarazin 1986; Rosati, Borgani & Norman 2002; Donahue et al. 2014), or Sunyaev–Zel’dovich effect (SZE) in the radio domain (e.g. Bleem et al. 2015; Planck Collaboration XXIV 2016b).

Galaxy cluster richness provides another estimate for cluster masses, based on the number of cluster member galaxies. The red-sequence Matched-filter Probabilistic Percolation (redMaPPer) method determines cluster richness from the number of galaxies in an aperture, distributed in a red-sequence in a colour–magnitude diagram (Rykoff et al. 2014). The tight correlation between cluster richness and masses determined by other methods demonstrates the reliability of this estimator (Saro et al. 2015, 2017; Farahi et al. 2016; Mantz et al. 2016b; Geach & Peacock 2017; Melchior et al. 2017; Simet et al. 2017; Murata et al. 2018, 2019; McClintock et al. 2019a; Raghunathan et al. 2019).

Assuming an NFW mass profile and a range of anisotropy profiles, it is also possible to determine cluster masses with the Jean equation and spectroscopic redshifts of cluster member galaxy (Biviano et al. 2013; Mamon, Biviano & Boué 2013; Munari et al. 2013). This estimation is based on the assumption that galaxy clusters are in the hydrostatic equilibrium state. However, some biases might affect the estimated mass due to complex physical processes or the non-equilibrium states in galaxy clusters, for instance, the infall motion of outer galaxy members (Falco et al. 2013). The cross study between the dynamical analysis and weak lensing analysis helps to probe the assumption that galaxy clusters are in the equilibrium state (e.g. Smith et al. 2016).

Among all the methods to estimate cluster masses, gravitational lensing is recognized as the one with the least amount of assumptions regarding physical processes. In this respect, many methods are calibrated on gravitational lensing measurements (e.g. Mandelbaum et al. 2006; Johnston et al. 2007). Recently, the mass–richness relation of redMaPPer clusters has been estimated in the 10000 deg² of the Sloan Digital Sky Survey (Zu & Mandelbaum 2015; Simet et al. 2017; Murata et al. 2018), the Dark Energy Survey Science Verification (DES-SV) data (Melchior et al. 2017), and with the Dark Energy Survey Year 1 data (McClintock et al. 2019a).

Weak lensing analysis requires high quality and deep imaging data. The measured galaxy ellipticities are affected by different kinds of noises (telescope, instrument, atmosphere, etc.) that need to be taken into account. Building on the experience of previous experiments (e.g. Mandelbaum et al. 2005; Heymans et al. 2012; Miller et al. 2013), we now have several procedures to characterize and correct these effects. Weak lensing analysis also requires a good knowledge of source redshift distribution. Photometric redshifts require multiband imaging, but also calibration techniques, for instance, based on spectroscopic surveys (e.g. Laigle et al. 2016 in the COSMOS field).

In this paper, we present a weak lensing analysis of the CONstrain Dark Energy with X-ray galaxy clusters (CODEX) sample. We produce our lensing catalogue, based on the photometric catalogues produced by the Dark Energy Camera Legacy Survey (DECaLS) Data Release 3. This imaging survey covers 4200 deg² in *grz* bands, and partly overlaps with the CODEX catalogue footprint. The CODEX cluster sample is the intersection between the redMaPPer cluster sample, and clusters identified by detecting overdensities in

X-ray observations from the *ROSAT* All-Sky Survey (RASS; Voges et al. 1999). This catalogue is supposed to be less contaminated by fake detections, and thus more reliable to constrain cosmological parameters. We measure the lensing signal around 279 CODEX clusters selected in the redshift range $0.1 \leq z \leq 0.2$. We use these measurements to estimate the parameters of the scaling relation that relates to the lensing mass and the richness of the clusters. We compare our scaling relation based on weak lensing with the one determined from the dynamics of the galaxies observed in spectroscopy presented in Capasso et al. (2019).

The structure of this paper is as follows. In Section 2, we describe the preparation of the DECaLS data for the shear measurement and the CODEX cluster catalogue. We summarize the method used for the weak lensing analysis in Section 3 and the data analysis in Section 4. Section 5 reports on the results from the weak lensing measurement and also the comparison with the dynamical analysis in Section 5.3. In Section 6, we conclude and discuss future work and analysis.

Throughout the paper, we adopt a concordance Λ CDM model with the cosmological values : $\Omega_m = 0.3$, $\Omega_\Lambda = 0.7$, $\sigma_8 = 0.8$, $n_s = 0.965$, and a Hubble constant $H_0 = 100 h \text{ km s}^{-1} \text{ Mpc}^{-1}$ with $h = 0.7$. Errors are quoted on the 68 per cent confidence level.

2 DATA

In this study, we use the data from the Dark Energy Camera Legacy Survey (DECaLS) Data Release 3 overlapping with the CODEX cluster catalogue. We describe the preparation of the DECaLS shear catalogue from the DECaLS DR3 data in Section 2.1, and the CODEX clusters catalogue in Section 2.2.

2.1 DECaLS

The Dark Energy Camera Legacy Survey (DECaLS)¹ uses the Dark Energy camera installed on the Blanco 4 meters telescope, located at the Cerro Tololo Inter-American Observatory in Chile. This imaging survey is part of the Dark Energy Spectroscopic Instrument (DESI) Legacy Imaging Survey (Dey et al. 2019). It provides the optical imaging for targeting 2/3 of the DESI footprint at declination Dec. < 32. DR3 (PI: D. Schlegel and A. Dey)² includes the images observed from 2014 August to 2016 March and also incorporates data from the Dark Energy Survey (DES) acquired between 2012 September and 2016 March. We note that only DECaLS data were used for this study. The DECaLS DR3 data contain the images covering 4300 deg² in *g* band, 4600 deg² in *r* band and 8100 deg² in *z* band. In total 4200 deg² has been observed in all three optical bands.

In Fig. 1, we show the depth of the DECaLS DR3 objects in three optical bands; *g*, *r*, and *z*. The DECaLS is about 1.5 to 2.0 mag deeper than SDSS in *r* band (Dey et al. 2019). Forced photometry is performed with the tool Tractor (Lang, Hogg & Schlegel 2014).

In the DECaLS DR3 catalogue, the sources from the Tractor catalogue are separated into five morphological models; point sources (PSF), simple galaxies (SIMP), DeVaucouleurs (DEV), exponential (EXP), and composite model (COMP). Sky-subtracted images are stacked in five different ways: one stack per band, one ‘flat’ spectral energy distribution (SED) stack of all bands, one ‘red’ SED stack of all bands ($g - r = 1 \text{ mag}$ and $r - z = 1 \text{ mag}$). Sources

¹<http://www.legacysurvey.org>

²DECam programs ID: 2013A-0741 and 2014B-0404.

Figure 1. The depth of the DECaLS DR3 objects in three optical bands from the DECaLS DR3.

above 6σ detection limit in any stack are kept as candidates. PSF (delta function) and SIMP models are adjusted on individual images convolved by their own PSF models. PSF models for the individual exposure are determined with the tool PSFEx (Bertin 2011).

A source is retained if its penalized χ^2 is improved by 25; sources below this threshold are removed. Then, the source is classified as the better of PSF or SIMP, unless adjusting a DEV or EXP profile improves the χ^2 by 9 (approximately 3σ improvement). A source is upgraded as COMP (composite between DEV and EXP model), if the penalized χ^2 improves by another 9. These selections imply that any extended source classification corresponds to at least a 5.8σ detection, and a 6.5σ detection for the COMP model.

2.1.1 Bias correction

Galaxy ellipticity parameters ε_1 and ε_2 are free parameters of the SIMP, DEV, EXP, and COMP models. They are estimated by a joint fit on the three optical grz bands. We model potential measurement bias with a multiplicative (m) and additive bias (c) (e.g. Heymans et al. 2012; Miller et al. 2013). The additive bias is known to arise from residuals in the anisotropic PSF correction, and depends on galaxy sizes. The multiplicative bias arises from shear measurement, which can be generated by many effects, such as measurement method, blending, and crowding. (see e.g. Euclid Collaboration 2019). In order to calibrate the DECaLS DR3 shear catalogue, we cross-match the DECaLS objects with the Canada France Hawaii

Telescope (CFHT) Stripe 82 objects and compute the correction parameters. The CFHT Stripe 82 (CS82) is a survey covering ≈ 170 square degrees of the Sloan Digital Sky Survey (SDSS) Stripe 82 in the equatorial region of the South Galactic Cap. Imaging data are of high quality and have been obtained in excellent seeing conditions between 0.4 and 0.8 arcsec with an average of 0.59 arcsec. It was primarily designed for lensing analysis (see e.g. Shan et al. 2014; Liu et al. 2015).

For each model SIMP, EXP, and DEV, we compute the correction parameters defined by

$$\varepsilon_i^{\text{obs}} = (1 + m_i) \varepsilon_i^{\text{true}} + c_i; i = 1, 2, \quad (1)$$

where ε^{obs} is the observed shape of the source and $\varepsilon^{\text{true}}$ is the true shape. For the multiplicative bias, we define the correction factor which is given by

$$1 + m = \frac{a_0 \exp(-a_1 \times r_g \times \text{magz})}{\log_{10} \text{magz}}, \quad (2)$$

where r_g is a radius of the objects, magz is a magnitude of the object in the z band, a_0 and a_1 are the result from the fitting with the CS82 data described in Appendix A. In Fig. 2, we plot the sky coverage of the DECaLS DR3 shear catalogue with the galaxy density. We also compute the effective weighted galaxy number density (Heymans et al. 2012) of DECaLS galaxies which is similar to the distribution in Fig. 2, higher density in South Galactic Cap (e.g. Stripe 82 region). This is a little larger than the data from the Sloan Digital Sky Survey (SDSS) which has a source density of about 1.5 galaxies per square arcminute (Mandelbaum et al. 2005). We mention that many sources are discarded because Tractor is not specific to shape measurement. In addition, we excluded the SIMP object in the DECaLS shear catalogue for our weak lensing analysis because the result in calibrating with the CS82 provided high correction values, as shown in Table A1.

2.1.2 Redshift distribution

In this section, we describe how we compute the redshift distribution of the DECaLS sources. We use the photometric redshifts measured in the COSMOS field (Laigle et al. 2016). The photometric redshifts of the COSMOS 2015 catalogue are computed by using the ‘Le Phare’ program with a chi-square fitting method between the theoretical and observed photometric catalogue same as Ilbert et al. (2013). We match each source of the DECaLS catalogue in position with the COSMOS catalogue, with maximum separation of 1 arcsec. We manage to match 100 per cent of the DECaLS shear catalogue

Figure 2. A source density distribution of the DECaLS DR3 shear catalogue and the samples of CODEX clusters (black dots) in equatorial coordinates.

Figure 3. The photometric redshift distribution of DECaLS sources from the COSMOS 2015 catalogue with the probability function (blue solid line) defined by equation (3).

Figure 4. The demonstration of an amplitude correction by using the probability distribution function of DECaLS DR3 sources from the COSMOS 2015 catalogue to correct the contaminating foreground galaxies.

with the COSMOS 2015 catalogue and compute the histogram of the photometric redshift distribution for the DECaLS DR3 shear catalogue as shown in Fig. 3. We model the photometric redshift distribution by fitting with the following probability distribution function

$$P(z_s) \propto A \left(\frac{z_s}{z_0} \right)^{B-1} \exp \left[-\frac{1}{2} \left(\frac{z_s}{z_0} \right)^2 \right], \quad (3)$$

and find good agreement as seen in Fig. 3. We obtain the fitting parameters, $A = 2.261 \pm 0.172$, $B = 1.801 \pm 0.173$, and $z_0 = 0.432 \pm 0.035$. This function is used to calculate the excess mass density profile as described in Section 3.1.1. In Fig. 3, we show the comparison between the redshift distribution of the DECaLS sources from the COSMOS 2015 catalogue and the probability function defined in equation (3).

In our analysis, we consider all galaxies along the line of sight. Given the limited colour information in our galaxy sample, we do not remove the foreground galaxies from the shear measurement. We did not find any selection in colour to yield a higher signal-to-noise ratio in the lensing measurement than the case of no removal of the foreground galaxies.

By construction, foreground galaxies contain no lensing signal. Therefore on average, they decrease the amplitude of the lensing signal. To quantify the impact of the contamination by foreground

Figure 5. Comparison of the SDSS richness's estimated by the redMaPPer algorithm within 3 arcmin from the X-ray centre (λ_{SDSS}) and at the optically identified centre (λ_{OPT}) of the CODEX clusters in the DECaLS DR3 survey footprint.

galaxies, we compare the integrated lensing critical surface densities Σ_{cr} defined in equation (14)), when we include all galaxies ($z_{\text{source}} > 0$), and when we remove galaxies located in front of a cluster at redshift z_{cluster} . In Fig. 4, we show the amplitude correction (A) defined as

$$A \text{ (per cent)} = \frac{\Sigma_{\text{cr}}(z_{\text{source}} > 0) - \Sigma_{\text{cr}}(z_{\text{source}} > z_{\text{cluster}})}{\Sigma_{\text{cr}}(z_{\text{source}} > 0)} \times 100 \text{ per cent}. \quad (4)$$

We find that the amplitude correction increases quickly with cluster redshift. However, in the ideal case where we could remove foreground galaxies, the lensing signal would only be increased by ≈ 4 per cent. This is marginal, given that our signal-to-noise ratio at $R = 5 h^{-1} \text{Mpc}$ is about $S/N = 10$. None the less, since this amplitude correction increases quickly, it prevents us from studying the mass–richness relation for clusters at redshift $z_{\text{cluster}} > 0.2$.

2.2 Weak lensing sample of CODEX clusters

The CODEX cluster catalogue is constructed by identifying faint (selected down to a 4σ significance of a source detection on spatial scales of 3–12 arcmin) X-ray sources in the *ROSAT* All Sky Survey data (Voges et al. 1999) using redMaPPer algorithm (Rykoff et al. 2014). The catalogue contains a cluster redshift, a richness, a position of the optical centre, selected according to the redMaPPer rules, but constrained to be within 3 arcmin from the X-ray centre, and a catalogue of member galaxies. The set of redMaPPer parameters identified at the optical centre are notated using the OPT suffix ($z_{\lambda, \text{OPT}}$, λ_{OPT} , and etc.). Cluster richness is evaluated at two positions, the X-ray (λ_{SDSS}) and the optical (λ_{OPT}). The results of the SDSS-IV spectroscopic follow-up using the catalogue of member galaxies show a high degree of cluster confirmation at $z < 0.4$ (Clerc et al. 2016), which covers the redshift range used in this work (SDSS-IV; Dawson et al. 2016; Blanton et al. 2017). The results of a similar catalogue construction in DES (Klein et al. 2018) show that for the redshift range considered here ($0.1 \leq z_{\text{cluster}} \leq 0.2$), the use of a richness cut $\lambda \geq 20$ results in the catalogue pure at 99 per cent. In Fig. 5, we compare the two CODEX cluster richness estimates in the DECaLS DR3 footprint. We observe a scatter of about 20 per cent at richness $\lambda_{\text{OPT}} = 20$, which decreases to ~ 5 per cent at $\lambda_{\text{OPT}} = 120$. In the following, we use redMaPPer parameters with the OPT suffix for the lensing

analysis, because it yields higher signal-to-noise measurements. Clerc et al. (2016) highlighted that z_{OPT} is systematically larger than the redshift obtained in spectroscopy with the SPIDERS data, for clusters at redshift $z_{\text{OPT}} < 0.1$. This will affect the richness estimate, as the aperture for galaxy selection requires distance information taken from the redshift. For this reason, we select clusters at redshift $0.1 \leq z \leq 0.2$, and optical richness $20 \leq \lambda_{\text{OPT}} < 110$ as shown in Fig. 6. This way, we exclude low richness clusters, which might be contaminated by projected structures along the line of sight.

We cross-match the CODEX clusters with the area of the DECaLS DR3 data and select the galaxy clusters located in the DECaLS DR3 survey footprint. The final subsample of CODEX clusters contains 279 clusters for our weak lensing analysis.

3 MODELIZATION

3.1 Mass profile

To ease comparison with previous works, we use the Navarro–Frenk–White profile (Navarro et al. 1996, hereafter NFW profile) to model the dark matter halo of the galaxy cluster, complemented by a second term that accounts for the correlated matter distribution at large scale. In practice, we use the excess surface mass density as an estimator (Mandelbaum et al. 2005), which is given by two terms,

$$\Delta \Sigma(R) = \Delta \Sigma_{\text{1h}}^{\text{NFW}}(R) + \Delta \Sigma_{\text{2h}}(R). \quad (5)$$

We measured the signal in the radius range $1.0 \leq R < 30.0 \text{ Mpc}$, to avoid the miscentring effect at small scale and to maximize the constraints by increasing the number of bins at large scale as discussed in Appendix B.

3.1.1 NFW profile

Numerical simulation is an effective tool to probe the large-scale structure problems. Navarro et al. (1996) used the N -body simulation in the cold dark matter cosmogony to investigate the density profile of the dark matter haloes that obeys the following double power-law form,

$$\rho_{\text{NFW}}(r) = \frac{\delta_c \rho_c}{(r/r_s)(1 + r/r_s)^2}, \quad (6)$$

where r is the distance from the cluster centre in three dimensions, r_s is the scale radius characteristic of the distribution of matter in the cluster, and δ_c is the linear overdensity threshold at which a halo collapse is defined as

$$\delta_c = \frac{200}{3} \frac{c^3}{[\ln(1+c) - c/(1+c)]}, \quad (7)$$

where c is the dimensionless parameter which is called the concentration parameter. The critical density of the universe can be written as

$$\rho_c = \frac{3}{800\pi} \frac{M_{200c}}{r_{200}^3}, \quad (8)$$

where M_{200c} is the cluster mass equal to the total mass inside that radius (r_{200}) or 200 times the critical density of the universe. We assume that, on average, galaxy clusters are spherically symmetric, therefore the tangential shear of background sources at the redshift z_s induced by the cluster lens at the redshift z_l is given by

$$\gamma_t(R) \equiv \frac{\bar{\Sigma}(< R) - \bar{\Sigma}(R)}{\Sigma_{\text{cr}}(z_l, z_s)} = \frac{\Delta \Sigma(R)}{\Sigma_{\text{cr}}(z_l, z_s)}, \quad (9)$$

where $\bar{\Sigma}(R)$ is the mean surface density at the radius R ,

$$\bar{\Sigma}(R) = \bar{\rho}_m \int_{-\infty}^{\infty} \xi_{\text{1h}}^{\text{NFW}} \left(\sqrt{R^2 + \chi^2} \right) d\chi, \quad (10)$$

and $\bar{\Sigma}(< R)$ is the mean surface density inside that radius,

$$\bar{\Sigma}(< R) = \frac{2}{R^2} \int_0^R \bar{\Sigma}(R') R' dR', \quad (11)$$

and $\Delta \Sigma(R)$ is called the excess surface mass density. In equation (10), $\xi_{\text{1h}}^{\text{NFW}}$ is the halo–matter correlation function of the 1-halo term of the NFW profile,

$$\xi_{\text{1h}}^{\text{NFW}} = \frac{\rho_{\text{NFW}}}{\bar{\rho}_m} - 1, \quad (12)$$

where $\bar{\rho}_m = \rho_c \Omega_m$ is the mean matter density, ρ_c is the critical density, and Ω_m is the matter density of the universe (e.g. Melchior et al. 2017; McClintock et al. 2019b).

The relation between the tangential shear and the excess mass density can be derived from the critical surface mass density of the lens $\Sigma_{\text{cr}}(z_l, z_s)$ in comoving coordinates as

$$\Sigma_{\text{cr}}(z_l, z_s) = \frac{c^2}{4\pi G} \frac{D_A(z_s)}{D_A(z_l) D_A(z_l, z_s)} \frac{1}{(1+z_l)^2}, \quad (13)$$

where $D_A(z_l)$, $D_A(z_s)$, and $D_A(z_l, z_s)$ are the angular diameter distances to the lens, sources, and between the lens and sources, respectively. In practice, instead of computing the critical surface mass density, we estimate an effective critical surface density (Okabe et al. 2014; McClintock et al. 2019a) by integrating over the source distribution,

$$\langle \Sigma_{\text{cr}}^{-1}(z_l) \rangle = \frac{\int P(z_s) \Sigma_{\text{cr}}^{-1}(z_l, z_s) dz_s}{\int P(z_s) dz_s}, \quad (14)$$

where $P(z_s)$ is the probability distribution function of source galaxies that is defined in equation (3). Thus, we can finally relate the excess surface mass density to the weak lensing measurement by

$$\Delta \Sigma_{\text{1h}}^{\text{NFW}}(R) = \gamma_t(R) \langle \Sigma_{\text{cr}}^{-1}(z_l) \rangle^{-1}. \quad (15)$$

3.1.2 The 2-halo term

Galaxy clusters reside at the node of the cosmic web, with dense filament and massive nearby haloes. The mass measurement of a galaxy cluster is not perfectly consistent with the underlying matter density field, suggesting that the galaxies are not exactly tracking the underlying mass distribution (see e.g. Dekel & Lahav 1999; Jullo et al. 2012). The matter distribution around galaxy clusters shapes the mass profile at large scale (Hoekstra et al. 2011; Jauzac et al. 2012). We can express the excess surface mass density of the second dark matter halo by

$$\Delta \Sigma_{\text{2h}}(R) = \bar{\Sigma}_{\text{2h}}(< R) - \bar{\Sigma}_{\text{2h}}(R). \quad (16)$$

The excess mass density at the projected radius (R) is defined by

$$\bar{\Sigma}_{\text{2h}}(R) = 2\rho_{c,0} \Omega_{m,0} \int_0^\infty \xi_{\text{2h}} \left(\sqrt{R^2 + \chi^2} \right) d\chi, \quad (17)$$

where $\xi_{\text{2h}}(r)$ is the galaxy–matter cross-correlation function, $\rho_{c,0}$ is the critical density, and $\Omega_{m,0}$ is the matter density of the universe at this time. This function is obtained by multiplying the non-linear matter correlation function $\xi_{\text{nl}}(r)$ with the halo bias $b(M, z)$ given by

$$\xi_{\text{2h}}(r) = b(M, z) \xi_{\text{nl}}(r) \zeta(r), \quad (18)$$

where $\zeta(r)$ is the scale dependence of halo bias which is more significant at the radius $R \leq 3 h^{-1}$ Mpc, described in Tinker et al. (2005). In this study, we use the halo bias prescription derived from cosmological simulations by Tinker et al. (2010). The non-linear matter correlation function is the Fourier transform of the non-linear matter power spectrum P_{nl} ,

$$\xi_{\text{nl}}(r) = \frac{1}{2\pi} \int k^2 P_{\text{nl}}(k) j_0(kr) dk, \quad (19)$$

where $j_0(kr)$ is the zeroth order of spherical Bessel function of the first kind. We use the revised halo fit model (Takahashi et al. 2012) and the Code for Anisotropies in the Microwave Background (CAMB) program (Lewis & Challinor 2011) to compute the non-linear matter power spectrum by evaluating the mean redshift of stacked clusters.

3.2 Concentration–Mass relation

The NFW profile is described by two parameters; the concentration (c) and the total mass (M_{200c}). The results from the numerical simulations show that the concentration and the total mass (c – M) are related. Data from observations are also used to test the c – M relation (e.g. Okabe et al. 2010). The relation between the concentration and the total mass is an important tool to test the cosmological models and the physical processes in a galaxy cluster. There are many studies in different data sets to characterize this relation. Duffy et al. (2008), for example, studied the c – M relation of the NFW profile using N -body simulations in the Wilkinson Microwave Anisotropy Probe year 5 (WMAP5) cosmology, and found an additional dependency between halo masses and redshift, best modelled by a power law. The results show that the concentration decreases as a function of the total mass and redshift. Later, Dutton & Macciò (2014) studied the c – M relation in the Planck cosmology. They found that the c – M relation is higher than the study in the WMAP5 cosmology. They provided the following expression for the concentration mass relation, defined as a power law

$$\log_{10} c_{200c} = a + b \log_{10} (M_{200c} / [10^{12} h^{-1} M_{\odot}]), \quad (20)$$

where a and b are given by

$$a = 0.520 + (0.905 - 0.520) \exp(-0.617 z^{1.21}), \quad (21)$$

$$b = -0.101 + 0.026z. \quad (22)$$

For this analysis, the signal-to-noise ratio of our measurement is quite low. Consequently, we use this relation to reduce the number of free parameters in our model. However, we note that this c – M relation determined from a complete set of simulated clusters, might differ from one of our samples, especially at low mass, where we might miss some clusters. None the less, the previous study from Cibirka et al. (2017) on the CODEX clusters shows an excellent agreement between the simulation from Dutton & Macciò (2014) and observations.

4 ANALYSIS

4.1 Weak lensing estimator

As we discussed, the weak lensing analysis requires deep imaging data. The density of background galaxies of the DECaLS DR3 is not sufficient to measure the mass of individual clusters. Therefore, we turn to the stacking technique to recover the weak lensing signal. The stacking technique is the method in which the galaxy clusters

and their measured radial density profile can be combined according to observed properties (e.g. richness or X-ray luminosity). It helps to enhance the S/N of the lensing profile when we cannot recover the lensing signal of individual clusters. The stacked surface mass density profile can be written in terms of the summation of the tangential shear over N background galaxies i that are found within an annular region at radius R around the lenses as

$$\Delta \Sigma(R) = C(R) \frac{\sum_{i=1}^N w_i \gamma_{t,i}(R) \langle \Sigma_{\text{cr}}^{-1} \rangle^{-1}}{\sum_{i=1}^N (1+m) w_i}, \quad (23)$$

where $C(R)$ is called a boost factor and w_i is the weight chosen to minimize the variance of a shear estimator. We include a boost factor to account for contamination in our lensing source sample by galaxies that might be associated with the clusters (see e.g. Fischer et al. 2000; Simet et al. 2017). This effect is scale dependent, in contrast with the critical density rescaling $\langle \Sigma_{\text{cr}}^{-1} \rangle^{-1}$, due to the lack of photometric redshift information. For lensing sources with index i , around N lenses with index j , and sources with index k , around N_{rand} random points with index l , the correction factor is given by

$$C(R) = \frac{N_{\text{rand}} \sum_{i,j} w_{i,j}}{N \sum_{k,l} w_{k,l}}. \quad (24)$$

Compared to previous works, we adapt the method to estimate the correction factor by drawing 10 random positions in a 1.5 deg aperture from the cluster centres, instead of drawing random points in the full survey footprint. This is justified by the fact that cluster density is very low, and our survey footprint is very irregular. We found that the variation of the boost factor profile is less than 5 percent within the size of the aperture. More detail is given in Appendix C2. Overall, the boost factor effect is less than 1 per cent at $R > 1$ Mpc, where we perform our analysis.

4.2 Error estimation

4.2.1 Stacked samples covariance

There are many effects which cause statistical errors in the measurements, such as the intrinsic shape of source galaxies, the number of lens–source pairs and the fluctuations of the large-scale structure along the line of sight (e.g. Shirasaki et al. 2017). We use the Jackknife technique detailed in the following procedure to estimate the statistical errors for each of the three stacked cluster groups: (i) Randomly draw 10 positions within a 1.5 deg aperture from true cluster positions, (ii) employ the delete-1 Jackknife technique in each realization by removing one cluster from the stacked profile and average the lensing profiles for true and random clusters, and (iii) repeat the measurement for each Jackknife configuration. The covariance matrix of stacked clusters for the Jackknife technique can be written as

$$\mathbf{C} \equiv C_{ij} = \frac{N_{\text{JK}} - 1}{N_{\text{JK}}} \sum_{m=1}^{N_{\text{JK}}} (\Delta \Sigma_i^m - \overline{\Delta \Sigma}_i) (\Delta \Sigma_j^m - \overline{\Delta \Sigma}_j), \quad (25)$$

where i and j indicate the radial bins, $\Delta \Sigma^m$ is the excess surface mass density for each of the m th Jackknife configuration. In equation above, the mean excess surface mass density of the Jackknife configurations is defined by

$$\overline{\Delta \Sigma} \equiv \frac{1}{N_{\text{JK}}} \sum_{m=1}^{N_{\text{JK}}} (\overline{\Delta \Sigma}_{\text{true}}^m - \overline{\Delta \Sigma}_{\text{random}}^m), \quad (26)$$

where $\overline{\Delta \Sigma}_{\text{true}}$ is the mean excess surface mass density of true cluster positions and $\overline{\Delta \Sigma}_{\text{random}}$ is the mean excess surface mass density of

Table 1. The results from the mass measurements in three richness bins. The excess surface mass density profiles have been fitted with the theoretical model in two regions; the inner region ($1.0 \leq R < 5.5$ Mpc) modelled with the NFW profile only ($\Delta\Sigma_{1h}^{NFW}$), and the whole region ($1.0 \leq R < 30.0$ Mpc) modelled with the two halo terms ($\Delta\Sigma_{1h}^{NFW} + \Delta\Sigma_{2h}$). The chi-square goodness of fit test and the degree of freedom (dof) reveal the best fits between observed data and the theoretical profile.

Richness group	N_{cluster}	z_{mean}	$\lambda_{\text{opt, mean}}$	$M_{200c}^{1h} (10^{14} M_{\odot})$	χ^2_{1h} / dof	$M_{200c}^{1h+2h} (10^{14} M_{\odot})$	$\chi^2_{1h+2h} / \text{dof}$
[20, 30)	109	0.148	24.83 ± 2.98	$2.19^{+0.39}_{-0.37}$	1.17 / 4	$1.91^{+0.27}_{-0.27}$	6.91 / 10
[30, 50)	110	0.152	38.90 ± 5.86	$2.98^{+0.44}_{-0.42}$	3.70 / 4	$2.37^{+0.32}_{-0.32}$	9.58 / 10
[50, 110)	60	0.158	63.86 ± 11.65	$5.91^{+0.82}_{-0.79}$	7.15 / 4	$5.02^{+0.52}_{-0.50}$	13.52 / 10

random positions in each Jackknife configuration. Notwithstanding, the covariance matrix of the Jackknife is underestimated due to the noise level, we therefore multiply the inverse covariance matrix ($\mathbf{C}^{-1}$) by the Hartlap factor; $H = (N_{\text{JK}} - p - 2)/(N_{\text{JK}} - 1)$, where N_{JK} is the number of Jackknife configurations and p is the number of measured radial bins (Hartlap, Simon & Schneider 2007).

4.2.2 Individual cluster covariance

In addition, we measure the covariance of the excess surface mass density profile for a typical cluster in our sample to be used later in Section 5.2. To this end, we estimate the covariance matrix by

$$\mathbf{C} = \frac{1}{N-1} \sum_{i=1}^N (\Delta\Sigma_i - \overline{\Delta\Sigma}) \times (\Delta\Sigma_i - \overline{\Delta\Sigma})^T, \quad (27)$$

where $\Delta\Sigma$ is a two-dimensional matrix, in which rows and columns correspond to the radial bins, the individual cluster measurements, respectively. The vector $\overline{\Delta\Sigma}$ is the average of the excess surface mass density profile of all clusters (e.g. McClintock et al. 2019a). We assume that cluster measurements are uncorrelated, and therefore, that the covariance matrix is diagonal. This statement is supported by the fact that off-diagonal terms derived from equation (27) are extremely noisy.

4.3 MCMC method

The Markov Chain Monte Carlo (MCMC) method is a resampling technique based on probability distributions. We use the MCMC method from the EMCEE package written in PYTHON (Foreman-Mackey et al. 2013) to fit our model to the measured density profiles. We set the number of walkers, burn-in(s), and production samples to 48, 1000, and 10 000, respectively. In our analysis, we assume that the log-likelihood function of the observed data ($\Delta\Sigma^{\text{obs}}$) is given by

$$\ln \mathcal{L}(\Delta\Sigma^{\text{obs}} | \Delta\Sigma^{\text{model}}) \propto -\frac{1}{2} \mathbf{D}^T \mathbf{C}^{-1} \mathbf{D}, \quad (28)$$

where $\mathbf{D} = (\Delta\Sigma^{\text{obs}} - \Delta\Sigma^{\text{model}})$ is the difference between the observed and modelled excess surface mass density, and $\mathbf{C}$ is the covariance matrix described in Section 4.2 (e.g. McClintock et al. 2019a).

5 RESULTS

5.1 Samples of CODEX clusters

We split our CODEX clusters sample into three richness groups; $\lambda = 20$ –30, 30–50, and 50–110. In each group, we stack the profiles and fit them with the model defined in equation (5) in the radial

Figure 6. The distribution of the optical richness and cluster redshift of our weak lensing sample of CODEX clusters.

range $1.0 \leq R < 30.0$ Mpc. We use the MCMC method to estimate confidence intervals and set the uniform prior on the cluster mass parameter, $M_{200c} = [10^{13}, 10^{15}]$.

We find that the excess surface mass density at large radius (e.g. $R > 5$ Mpc) has a large scatter, which might affect our mass estimates. Therefore, we repeat the mass measurement in the inner region only ($1.0 \leq R < 5.5$ Mpc), and fit only the first halo term ($\Delta\Sigma_{1h}^{NFW}$). We report the best-fitting values associated with their 1σ uncertainties in Table 1. The results show that the mass of CODEX clusters increases as a function of the optical richness. Furthermore, we find consistent results between two fitting procedures, suggesting that the Tinker et al. (2010) bias model is consistent with the 1 h-term mass estimate. In Fig. 7, we plot the excess surface mass density profile from the weak lensing measurement (black dots) and the solid line shows our theoretical model.

5.2 Mass–richness relation of the CODEX clusters

In this section, we assess the robustness of our estimated mass–richness relation with an alternative but equivalent method. Instead of adjusting a theoretical lensing signal to cluster density profiles distributed in bins of richness, we adjust a lensing signal to each profile based on the cluster richness and a parametrized mass–richness relation. We define the relation between the expected mass, richness, and cluster redshift as

$$\langle M_{200c} | \lambda \rangle = M_0 \left(\frac{\lambda}{\lambda_0} \right)^{F_\lambda}, \quad (29)$$

where M_0 and F_λ are the free parameters of this relation. We set the pivot values $\lambda_0 = 40$, close to the mean optical richness of CODEX cluster samples. Our data are not sensitive to more complicated mass–richness models, we therefore exclude the redshift evolution term from this relation, because the narrow range in redshift of our clusters sample does not provide enough constraint to estimate the

Figure 7. The excess surface mass density profiles of CODEX clusters in three richness groups: 20–30, 30–50, and 50–110. The blue solid line shows the theoretical profile defined in equation (5) with the first halo term in green and second halo term in red dashed lines. The error bars show the square root of the diagonal terms of Jackknife covariance matrix.

Figure 8. Posterior distributions of the free parameters in our mass–richness relation for our CODEX clusters sample, estimated with the MCMC analysis described in Section 5.2. Vertical dashed lines indicate the 68 percent confidence levels and contour lines correspond to 1σ, 2σ, and 3σ confidence levels.

redshift scaling index with precision. In addition, previous studies on this scaling relation found a minimal redshift evolution (e.g. McClintock et al. 2019a).

We use the MCMC method with the following priors on the mass–richness relation parameters, $\log_{10}M_0 = [13.0, 15.0]$ and $F_\lambda = [-10.0, 10.0]$ with the initial values, $\log_{10}M_0 = 14.0$ and $F_\lambda = 0.1$. For consistency with previous measurements, we restrict our analysis to the inner region ($1.0 \leq R < 5.5$ Mpc) and fit each cluster with the NFW profile as described in equation (15). In Fig. 8, we plot the best-fitting estimate of the mass–richness relation parameters $\log_{10}M_0$ and F_λ . We estimate the mean mass of our CODEX cluster sample,

$$M_0 = 3.24^{+0.29}_{-0.27} \times 10^{14} M_\odot, \quad (30)$$

and the richness scaling index

$$F_\lambda = 1.00^{+0.22}_{-0.22}. \quad (31)$$

Figure 9. The scaling relation of CODEX clusters (blue shaded line) computed with individual cluster compared to the stacked galaxy clusters in three richness groups. The results from both methods are consistent with each other.

Clearly, the cluster mass and richness of our samples are strongly correlated, and consistent with a power-law relation given that the reduced chi-squared is $\chi^2/\text{dof} \approx 0.99$. We also fit the two halo terms model in the radial range $1.0 \leq R < 30.0$ Mpc and obtain the mean mass of the CODEX clusters, $M_0 = 2.79^{+0.24}_{-0.22} \times 10^{14} M_\odot$, and the richness scaling index, $F_\lambda = 0.98^{+0.20}_{-0.20}$.

Finally, in Fig. 9, we compare our estimated masses in bins of richness with the best fit mass–richness relation found above and find a good agreement between both measurements. This gives us confidence that our two methods are equivalent and our mass–richness relation in equation (29) is a good model of the data.

5.2.1 Accuracy of richness estimates

Our determination of the mass–richness relation relies on an accurate estimate of the cluster richness. However, a biased estimate of the richness may lead to a biased relation (Rozo et al. 2009). We must investigate how the observable richness is actually tracing the cluster mass.

In our analysis, we use the optical richness as a mass tracing parameter. In Capasso et al. (2019), the authors determine a correction factor (η) on the optical richness parameter of the CODEX clusters. This factor corrects the richness of clusters that are at the limit of the observational capabilities. This factor also enters in the calculation of the Poisson variance, and must be taken into account in the fit of

the mass–richness relation. Another term is the intrinsic scatter σ_{int} in the richness (e.g. Simet et al. 2017). It is constant for all clusters, whatever their richness is. Therefore, we can express the variance of the mass–richness relation as

$$\text{Var}(\ln M|\lambda) = \frac{\alpha^2}{\lambda} + \sigma_{\text{int}}^2. \quad (32)$$

The introduction of this variance in the fit will down-weight both low and high richness clusters, either because the precision on low richness values is Poisson noise dominated or because the precision on high richness values is intrinsically limited.

We include α and σ_{int} as free parameters in our model and use the MCMC technique to find their best-fitting values. We find that the low signal-to-noise ratio in the shear signal of each cluster prevents us from determining these values with good precision. In order to reach a 7 per cent precision as in Simet et al. (2017), we would need roughly four times more clusters. Therefore, in order to test their effect, we set $\alpha = 1$ and $\sigma_{\text{int}} = 0.22$. Doing so, we assume that our clusters at low redshift are not significantly affected by observational considerations. Also, these values were already determined in Capasso et al. (2019) for the CODEX clusters as well. Taking into account these two variance terms, we find a mean cluster mass

$$M_0 = 3.12^{+0.28}_{-0.26} \times 10^{14} M_{\odot}, \quad (33)$$

and a richness scaling index

$$F_{\lambda} = 1.01^{+0.22}_{-0.21}. \quad (34)$$

These results are in statistical agreement with the results determined without taking into account the variance terms, which means that the richness estimates in our low-redshift cluster sample are robust.

5.2.2 CODEX clusters comparison with redMaPPer clusters

Differences in the selection functions of the redMaPPer and CODEX clusters have already been detailed in Section 2.2. However, it is interesting to compare the mass–richness relation determined with our CODEX sample and with the redMaPPer clusters. As a reference for the redMaPPer clusters sample, we use the results from DES Year 1 analysis in McClintock et al. (2019a). They constrain the mass–richness relation for redMaPPer galaxy clusters in the redshift range $0.2 \leq z \leq 0.65$ and with richness values $\lambda \geq 20$. They obtain a richness scaling index $F_{\lambda} = 1.356 \pm 0.051$ (stat) and a redshift scaling index $G_z = -0.30 \pm 0.30$ (stat). In comparison, our estimate of the richness scaling index is smaller. This suggests that at low richness, CODEX clusters are more massive than redMaPPer clusters. We attribute this difference to the completeness and selection function of the CODEX clusters, which have been confirmed with X-ray observations, and therefore are less contaminated by possible line-of-sight confusions.

5.3 Weak lensing and dynamical analysis

As detailed in the introduction, there are many methods to estimate cluster masses. In this section, we compare the weak lensing masses from our analysis with the dynamical masses determined from the velocity dispersion of galaxy cluster members. Usually, dynamical analyses are based on the assumption that galaxy clusters are in a dynamical equilibrium state. The cross study between weak lensing analysis and dynamical analysis can be used to calibrate a cluster mass and study the dynamical equilibrium state in galaxy clusters. However, within the limit of the survey, we only compare the scaling

Figure 10. Comparison of scaling relations determined with weak lensing and dynamical analysis for the CODEX cluster sample.

relation between both methods in order to track the cluster mass as a function of richness.

We compare our measurements with the dynamical analysis performed by Capasso et al. (2019), assuming the clusters observed by the SPIDERS program in spectroscopy constitute a random subsample of the parent CODEX cluster sample used in our analysis. They measured a sample of 428 galaxy clusters up to redshift $z \sim 0.66$ and model the scaling relation as $\lambda \propto A_{\lambda} M_{200c}^{B_{\lambda}} (1+z)^{\gamma_{\lambda}}$, where $A_{\lambda} = 38.6^{+3.1}_{-4.1}$, $B_{\lambda} = 0.99^{+0.06}_{-0.07}$, and $\gamma_{\lambda} = -1.13^{+0.32}_{-0.34}$. In Fig. 10, we plot the weak lensing and the dynamically based scaling relations of the CODEX clusters. For both relations, we set the mean cluster redshift $\bar{z} = 0.15$. The width of the shaded areas corresponds to the 1σ confidence level. We found an excellent agreement between the two scaling relations. This result supports our claim that the SPIDER clusters constitute a random subsample of the parent CODEX sample, and that the spectroscopic selection function introduces no significant bias. It also suggests that the dynamical equilibrium state assumption involved in the dynamical mass determination is appropriate on average.

Furthermore, we compute the mean mass ratio (β ; $M_{\text{dyn}}/M_{\text{wl}}$) between the dynamical masses (M_{dyn}) and the weak lensing masses (M_{wl}) (e.g. Smith et al. 2016), using the results from the scaling relation performed by Capasso et al. (2019). We obtain a mean mass ratio $\beta = 0.99 \pm 0.03$ in statistical agreement with $\beta_X = 0.95 \pm 0.05$ obtained for the Local Cluster Substructure Survey (LoCuSS) at the redshift $0.15 < z < 0.3$ by Smith et al. (2016).

6 CONCLUSION

In this study, we perform a weak lensing analysis of CODEX clusters using the DECaLS DR3 data. Our cluster sample consists of 279 clusters in the optical richness range $20 \leq \lambda < 110$ and in the redshift range $0.1 \leq z \leq 0.2$. The stacked weak lensing profile of CODEX clusters is computed in the radial ranges; $1.0 \leq R < 5.5$ Mpc and $1.0 \leq R < 30.0$ Mpc, to avoid the miscentring effect at smaller scales.

We split our CODEX cluster sample into three optical richness bins: 20–30, 30–50, and 50–110. In each bin, we measure the stacked excess surface mass density profile ($\Delta\Sigma(R)$). Lacking photometric redshift information for each DECaLS source, we compute an effective critical density based on their redshift distribution. We determine this latter by matching sources to the COSMOS 2015 catalogue. We model the excess surface mass density profile with an NFW profile. To reduce the number of free parameters in the

fitting, we assume that the concentration–mass relation follows the prescription by Dutton & Macciò (2014). We use an MCMC algorithm to estimate the mean cluster masses in each optical richness bin as show in Table 1.

We perform a complementary analysis to assess the robustness of our mass estimates. We assume a power-law relation between the mean cluster mass and optical richness $\langle M_{200c} | \lambda \rangle = M_0 (\lambda/40)^{F_\lambda}$. By fitting an individual cluster, we adjust the free parameters involved in this relation and restrict the measurement to the inner region ($1.0 \leq R < 5.5$ Mpc), and obtain the mean cluster mass at the pivot richness $\lambda = 40$,

$$M_0 = 3.24^{+0.29}_{-0.27} \times 10^{14} M_\odot, \quad (35)$$

and the richness scaling index,

$$F_\lambda = 1.00^{+0.22}_{-0.22}. \quad (36)$$

We find a good agreement between this scaling relation, and the cluster masses determined in the three richness bins. This gives us confidence that our power-law model for the scaling relation is appropriate.

In addition, we compare our scaling relation with the one obtained by Capasso et al. (2019) based on a dynamical analysis. Both relations are in good statistical agreement, although the cluster samples are slightly different. This supports the claim that the SPIDERS subsample used in the dynamical analysis is a random subsample of the parent CODEX catalogue used in the weak lensing analysis. It also suggests that the dynamical equilibrium assumption involved in the dynamical analysis is appropriate on average.

We also compare the scaling relation of the CODEX clusters with the redMaPPer clusters measured by McClintock et al. (2019a). The scaling relation for CODEX clusters is shallower than the redMaPPer clusters, which highlights the different selection functions between the two samples. At similar low-optical richness, the CODEX clusters are more massive than the redMaPPer clusters.

Our results demonstrate that weak lensing analysis can be performed with the DECaLS data. We plan on updating the weak lensing catalogue with wider areas and deeper imaging data provided by the final release of the DECaLS catalogue. None the less, during this analysis, we found the low density of weak lensing sources in the DEV category given the imaging depth. We would need to extend our calibration to the other categories to increase the source density. Another option would be to run a weak lensing dedicated shape measurement tool.

Building on a better weak lensing catalogue, and the advent of forthcoming massive spectroscopic surveys on the same footprint, it becomes tempting to compare weak lensing and dynamics to high precision in order to study galaxy cluster physics, and test modified gravity models (e.g. Pizzuti et al. 2019).

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APPENDIX A: ELLIPTICITY CORRECTION

The ellipticity parameter was measured for each source. It is different from the usual ellipticity definition in the DECaLS DR3 catalogue which is given by

$$\varepsilon \equiv \sqrt{1 - (b/a)^2}, \quad (\text{A1})$$

where a and b are the semimajor and semiminor axis of an elliptical source (galaxy). For a gravitational analysis, the ellipticity is a complex number,

$$\varepsilon = \frac{a - b}{a + b} \exp(2i\phi) = \varepsilon_1 + i\varepsilon_2, \quad (\text{A2})$$

where ϕ is the position angle relative to the reference frame with a range of 0–180 deg. This ellipticity has been used in the weak lensing analysis. However, we must calibrate it before using in the measurement. We calibrated the DECaLS DR3 sources with the CS82 data. We define the relation between the observed and corrected ellipticities as

$$\varepsilon_{1,\text{corr}} = (1 + m)\varepsilon_{1,\text{obs}}, \quad (\text{A3})$$

$$\varepsilon_{2,\text{corr}} = (1 + m)\varepsilon_{2,\text{obs}} + c_2, \quad (\text{A4})$$

where $(1 + m)$ is defined in equation (2) and the c_2 component is defined as

$$c_2 = b_0 + (b_1 \times \text{magz}) + (b_2 \times \text{magz}^2). \quad (\text{A5})$$

The calibration parameters of the DECaLS DR3 catalogue with the CS82 catalogue are shown in Table A1 and the c_2 component is given by $b_0 = 0.25577$, $b_1 = -0.02266$, $b_2 = 0.00050$ with the magnitude cut $\text{magz} < 21.0$. In Fig. A1, we compare the ellipticity 1 (e_1) between the CS82 and DECaLS catalogue before (black solid lines) and after correction (blue solid lines) with the CS82 data for the EXP object in the DECaLS DR3 shear catalogue. In

Table A1. The calibration parameters of the DECaLS DR3 shear catalogue with the CS82 catalogue and Obiwan simulation.

Type	Number of objects	a_0 (CS82)	a_1 (CS82)	$1 + m$ (CS82)	$1 + m$ (Obiwan)	c_2 (CS82)	c_2 (Obiwan)
SIMP	25462647	1.23907	0.02817	0.697 ± 0.099	–	0.002 ± 0.002	–
EXP	24923051	1.12193	-0.00011	0.851 ± 0.014	0.896 ± 0.045	0.002 ± 0.002	0.000 ± 0.001
DEV	5404940	1.18554	0.00946	0.771 ± 0.078	–	0.004 ± 0.003	–
COMP	75429	1.18554	0.00946	0.773 ± 0.108	–	0.007 ± 0.004	–

Figure A1. Comparisons of the ellipticity 1 (e_1) for the EXP object in the DECaLS DR3 shear catalogue before (black solid lines) and after correction (blue solid lines) with the CS82 data. The contour plots present the confidence levels at 1σ , 2σ , and 3σ , respectively.

addition, the data from DECaLS DR3 catalogue were tested with the Obiwan simulations.³ This simulation simulated ELG galaxies with Sersic profiles on top of real DECam images, and re-run the Tractor tool to produce catalogues. After matching the simulated positions and the Tractor positions within a 5 arcsec radius, we obtained approximately 100 000 galaxies for the calibration. From the fitting, we obtained best-fitting values for the EXP objects, $a_0 = 1.33320$ and $a_1 = 0.00656$. For the c_2 component, we obtained $b_0 = 0.31341$, $b_1 = -0.02914$, and $b_2 = 0.00067$, with the cut in magnitude $mag_z < 21.3$.

APPENDIX B: MISCENTRING EFFECT

By stacking the weak lensing profile, the cluster centre should be correctly defined to provide the true mass profile. In this work, we choose the brightest cluster galaxy (BCG) as the cluster centre. However, the centre of mass distribution in galaxy clusters can be shifted from the BCG, due to physical processes in cluster cores. In this section, we assess the impact of miscentring, and demonstrate that our radial cut at $R > 1$ Mpc, safely mitigate any bias due to this effect. Note that the redMaPper algorithm computed a probability in each galaxy to be the BCG and selects the most likely as the BCG for that cluster. However, the miscentring rate of the redMaPper galaxy clusters is about $f_{\text{mis}} = 0.25$ (Rozo & Rykoff 2014; Rykoff et al. 2014).

To model the miscentring effect on the cluster mass distribution, we adopt the expression given by

$$\Delta\Sigma(R) = (1 - f_{\text{mis}})\Delta\Sigma_{\text{1h}}^{\text{NFW}}(R) + f_{\text{mis}}\Delta\Sigma_{\text{mis}}^{\text{NFW}}(R) + \Delta\Sigma_{2\text{h}}(R), \quad (\text{B1})$$

where $\Delta\Sigma_{\text{1h}}^{\text{NFW}}$ is the excess surface mass density of NFW profile, $\Delta\Sigma_{\text{mis}}^{\text{NFW}}$ is the miscentring profile, $\Delta\Sigma_{2\text{h}}$ is the excess surface mass density profile of the second dark matter halo and f_{mis} is the miscentring factor. Formally, the second halo term should also be miscentred, but the effect is so weak that we decided to only apply this effect to the first halo term.

The miscentring profile is given by the projected excess surface mass density of the NFW profile which can be written by

$$\Delta\Sigma_{\text{mis}}^{\text{NFW}}(R|P(R_{\text{mis}})) = \int_0^\infty \Sigma(R|R_{\text{mis}}) P(R_{\text{mis}}) dR_{\text{mis}}, \quad (\text{B2})$$

³<https://obiwan.readthedocs.io>

Figure B1. The excess surface mass density profile from our CODEX cluster sample for the optical richness bin $\lambda = 50\text{--}110$ (black dots). The blue solid line shows the theoretical profile defined in equation (B1), by assuming the miscentring factor $f_{\text{mis}} = 0.25$, $\sigma_{\text{mis}} = 0.21$, and $M_{200c} = 5.02 \times 10^{14} M_\odot$. The dotted lines show each term in following equation contributing to the profile. The yellow line shows the theoretical profile defined by two terms as in equation (5) with the same cluster mass. The grey shaded area was excluded from our analysis due to the lack of the sources and high contamination in that region.

where $P(R_{\text{mis}})$ is the miscentring distribution chosen by the Rayleigh distribution function with the miscentring radius (R_{mis}) and parameter (σ_{mis}) as

$$P(R_{\text{mis}}) = \frac{R_{\text{mis}}}{\sigma_{\text{mis}}^2} \exp\left[-\frac{1}{2}\left(\frac{R_{\text{mis}}}{\sigma_{\text{mis}}}\right)^2\right]. \quad (\text{B3})$$

Accordingly, the excess surface mass density of miscentring term of the NFW profile is

$$\Sigma(R|R_{\text{mis}}) = \frac{1}{2\pi} \int_0^{2\pi} \Sigma(r) d\theta, \quad (\text{B4})$$

where $r = \sqrt{R^2 + R_{\text{mis}}^2 - 2RR_{\text{mis}}\cos(\theta)}$ is the projected radius at the coordinates (R, θ) related to the miscentring radius (see e.g. Yang et al. 2006; Johnston et al. 2007; George et al. 2012; McClintock et al. 2019a). In Fig. B1, we plot the stacked excess surface mass density of the CODEX cluster sample for the optical richness bin $\lambda = 50\text{--}110$ as in Section 5.1. We assess the miscentring effect with $f_{\text{mis}} = 0.25$ and $\sigma_{\text{mis}} = 0.21$ Mpc (i.e. McClintock et al. 2019a; Zhang et al. 2019). The lack of sources and high contamination in the inner region yield a very noisy signal at $R < 1$ Mpc (grey shaded area). Consequently, we decided to exclude this radial range to avoid any bias in our mass estimates.

In our analysis, we adjust a theoretical profile made of only two terms ($\Delta\Sigma_{\text{1h}}^{\text{NFW}} + \Delta\Sigma_{2\text{h}}$) as shown in equation (5). It is sufficient to reproduce the weak lensing signal in the radius range $R > 1$ Mpc. As a result, we decided not to include the miscentring effect.

APPENDIX C: SYSTEMATIC TESTS

C1 Testing on the non-lensing mode

In this section, we perform a systematic test on the ellipticity parameters of the DECaLS DR3 shear catalogue. The non-lensing mode of a shear component (cross shear) has been computed by rotating the ellipticities 45 deg. In theory, gravitational lensing does not produce a cross shear component. Therefore, we can use the cross shear component to reveal biases in the shape measurement operation. We compute the tangential shear (γ_t) and the cross

shear ($\gamma_{\times}$) from the real and imaginary parts of the ellipticity measurements

$$\gamma_l = -\text{Re}[\gamma e^{-2i\phi}] \text{ and } \gamma_{\times} = -\text{Im}[\gamma e^{-2i\phi}]. \quad (\text{C1})$$

We split our CODEX cluster sample in richness bins as in Section 5.1; $\lambda = 20\text{--}30$, $30\text{--}50$, and $50\text{--}110$. We plot the cross shear

Figure C1. The cross shear profiles per radial bin of the stacked clusters in three richness groups as described in Section 5.1. The error bars estimated from the Jackknife covariance matrix and the dof is equal to 12 for 12 radial bins.

component in Fig. C1. It is statistically consistent with zero at all radii and for our three richness bins.

C2 The dilution effect by lens–source galaxies

As we discussed in Section 4.1, the correction factor $C(R)$ is used to correct the contamination in the weak lensing signal produced by the overdensity of galaxies in the cluster centre (Simet et al. 2017). This effect dilutes the amplitude of the shear signal, especially, in the inner region of a galaxy cluster. In this test, we stack CODEX cluster samples and extend the shear measurement to smaller radius in the range $0.1 \leq R < 30$ Mpc. The results in Fig. C2 show that in the inner region, the dilution goes up to ≈ 4 per cent. However, in the outer region (ex. $R > 1$ Mpc), the correction factor is less than 1 per cent. Our measurements are therefore very little affected by the lens–source dilution effect.

Figure C2. The correction factor of CODEX cluster samples as a function of cluster radius.

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